

**SOLUTIONS MANUAL TO ACCOMPANY**

**SYSTEM**

**DYNAMICS**

Third Edition

Modeling and  
Simulation of  
Mechatronic Systems

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**DONALD L. MARCOLIS**

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**Solutions Manual to Accompany System Dynamics:  
Modeling and Simulation of Mechatronic Systems  
Third Edition**



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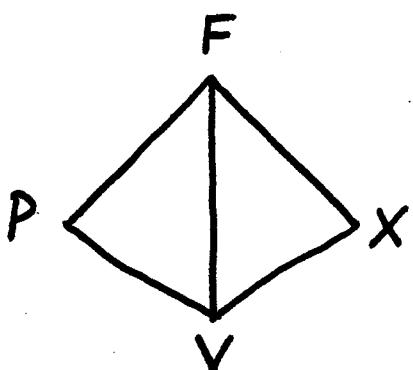
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1

1-1 to 1-5 These are mainly discussion questions.

2-1

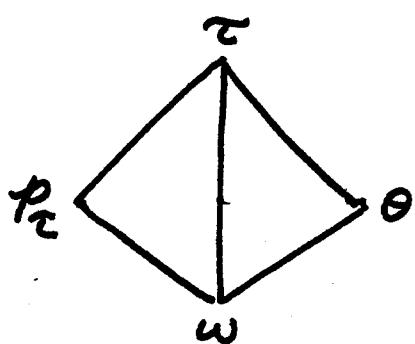


$$[F] - N$$

$$[Y] - m/s$$

$$[P] - N.s$$

$$[X] - m$$



$$[\tau] - N.m$$

$$[\omega] - rad/s$$

$$[P_C] - N.m.s$$

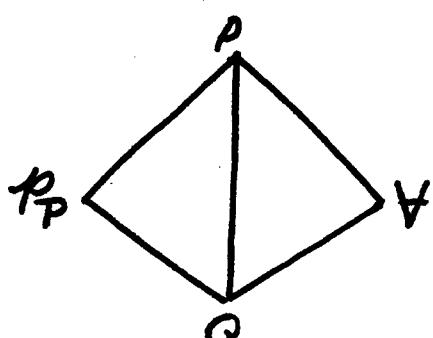
$$[\theta] - rad$$

$$[P] - N/m^2$$

$$[Q] - m^3/s$$

$$[P_P] - N.s/m^2$$

$$[\nabla] - m^3$$

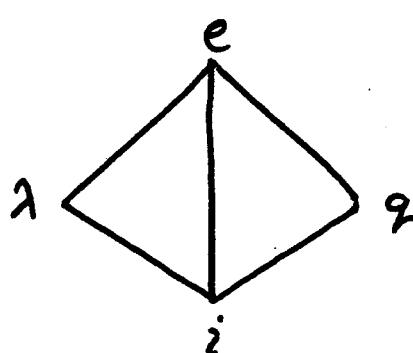


$$[e] - v$$

$$[i] - a$$

$$[\lambda] - v.s$$

$$[q] - a.s = c$$



2-2  $\frac{\tau}{\omega}$  Electric Motor  $\frac{e}{i}$  2  
(a)

$\frac{\tau}{\omega}$  Hydraulic Pump  $\frac{P}{Q}$   
(b)

$\frac{\tau}{\omega_1}$  Shaft  $\frac{\tau}{\omega_2}$   
(c)

$\frac{F}{V_1}$  Shock Absorber  $\frac{F}{V_2}$   
(d)

$\frac{e_1}{i_1}$  Transistor  $\frac{e_2}{i_2}$   
(e)

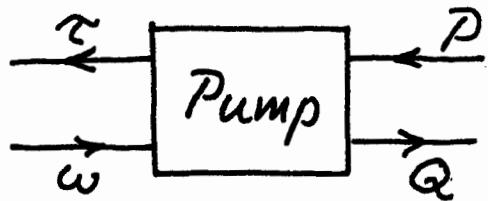
$\frac{e}{i}$  Speaker  
(f)

$\frac{\tau}{\omega}$  Crank  $\frac{F}{V}$   
(g)

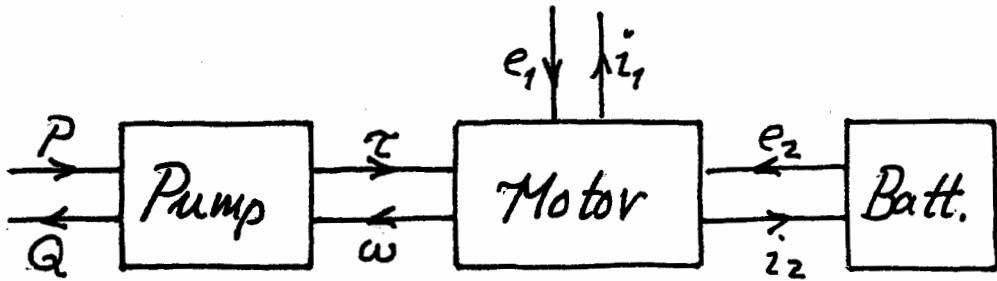
$\frac{F}{V}$  Wheel  $\frac{\tau}{\omega}$   $\frac{e_f}{i_f}$   
(h)  $\frac{\tau}{\omega}$  Motor  $\frac{e_a}{i_a}$   
(i)

2-3

$$\frac{\tau}{\omega} \text{ Pump } \frac{P}{Q}$$



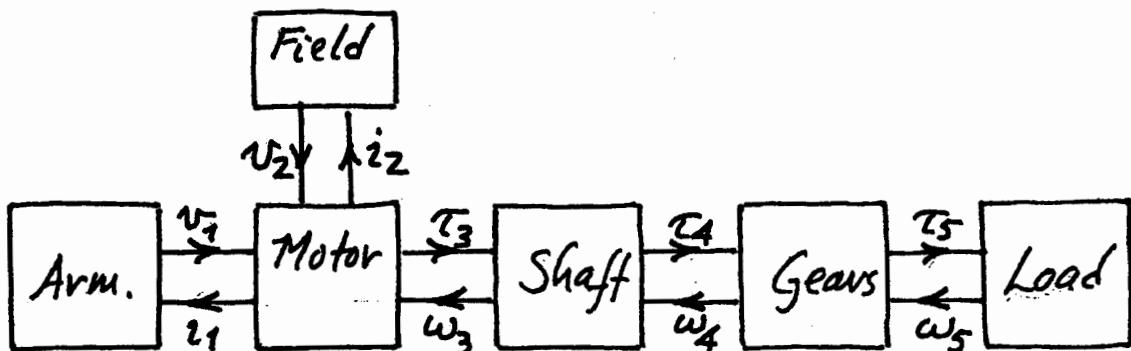
2-4



2-5

Field Supply

Arm. Supp.  $\frac{v_1}{i_1}$  Motor  $\frac{\tau_3}{\omega_3}$  Shaft  $\frac{\tau_4}{\omega_4}$  Gears  $\frac{\tau_5}{\omega_5}$  Load



2-6

throttle

 $\downarrow \theta$  $\downarrow \mu$  $\downarrow g$ Engine  $\xrightarrow{\omega_1}$  Clutch  $\xrightarrow{\omega_2}$  Gear  $\xrightarrow{\omega_3}$ D-Shaft  $\xrightarrow{\omega_4}$  Diff

Wheel

 $\downarrow \omega_5$  $F_2$  $F_3$ 

Road

 $F_1$ 

Mass

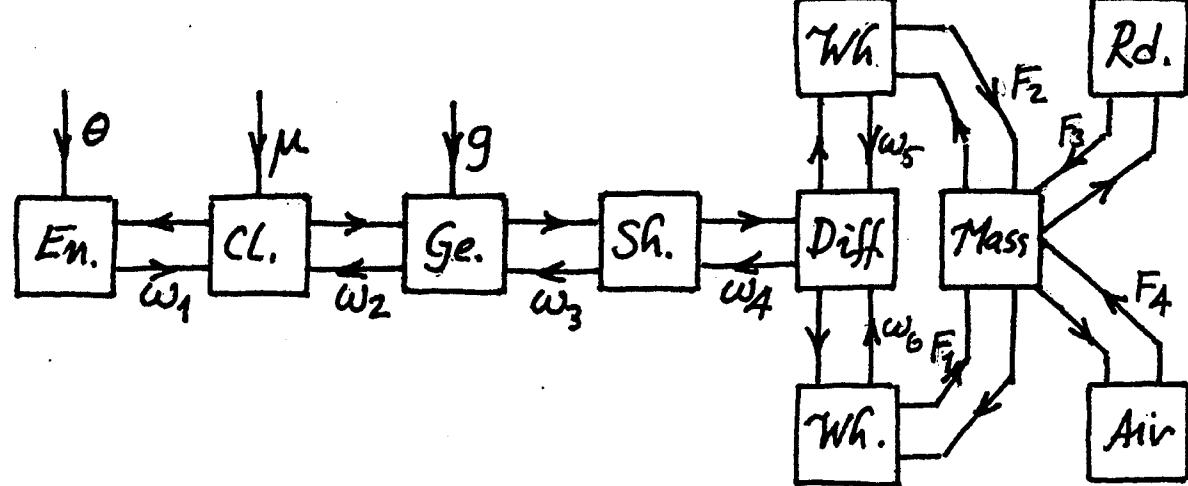
 $F_4$ 

Air

Wheel

 $\downarrow \omega_6$  $F_5$ 

Wheel

2-7 Inputs:  $P, e_1, e_2$ Outputs:  $Q, i_1, i_2$ 

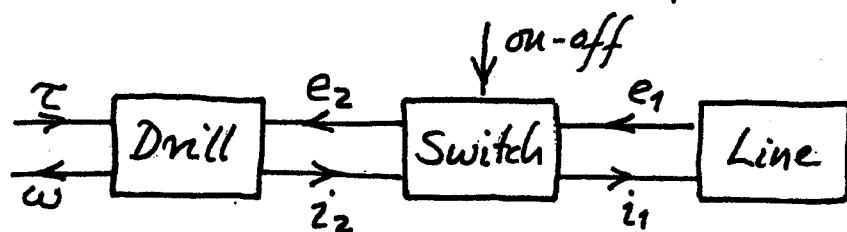
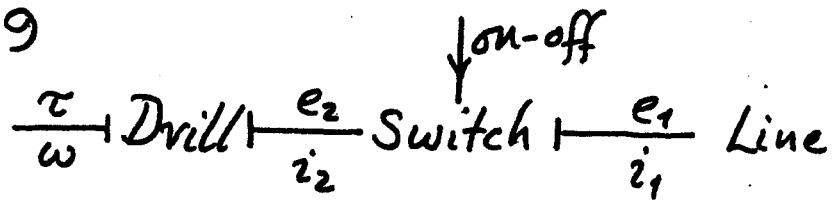
2-8

$$\begin{aligned} \text{Power} \times \text{Time} &= \text{Energy} \\ P \cdot t &= mgh \end{aligned}$$

$$100 \cdot t = 10 \cdot (9.81) \cdot 30$$

$$t = 29.43 \text{ s}$$

2-9



2-10

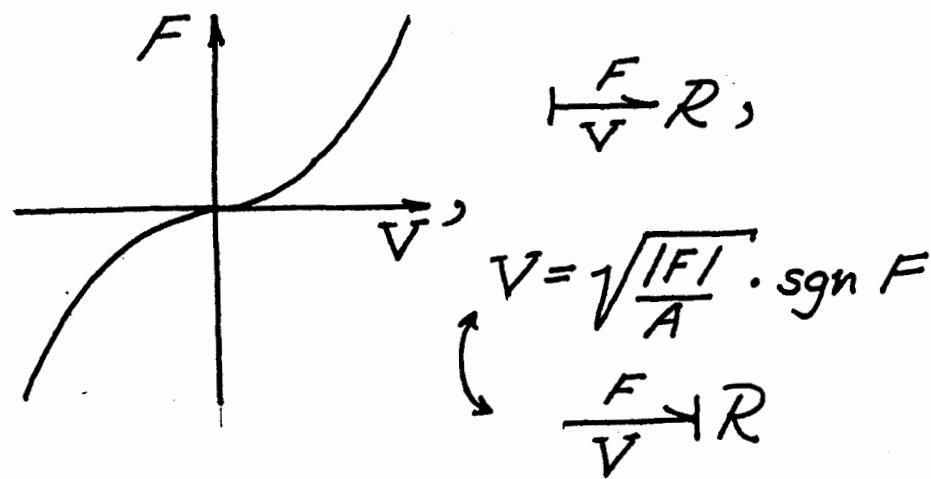
$$\tau \omega = PQ$$

$$\omega = \frac{P}{\tau} \cdot Q = \frac{7.0 \times 10^6}{5} Q$$

$$\omega = 1.4 \times 10^6 Q$$

$$\left[ \frac{\text{rad}}{\text{s}} \right] = \left[ \frac{1}{\text{m}^3} \right] \cdot \left[ \frac{\text{m}^3}{\text{s}} \right]$$

3-1

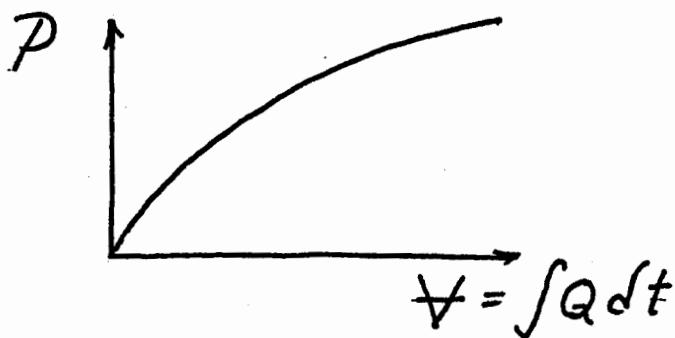


$$3-2 \quad hA = V = \int Q dt,$$

$$P = \rho gh = \frac{\rho g}{A} \int Q dt$$

$$\therefore C = A / \rho g$$

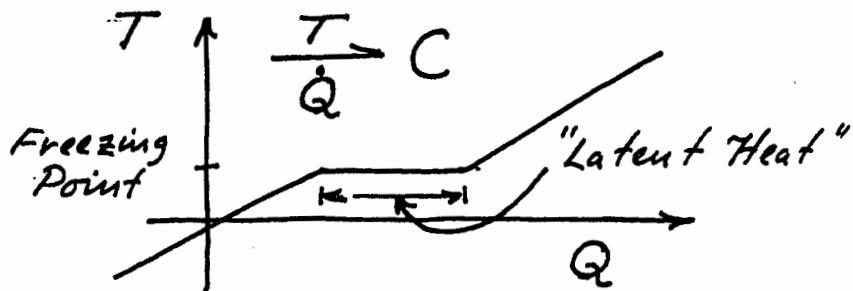
3-3



3-4

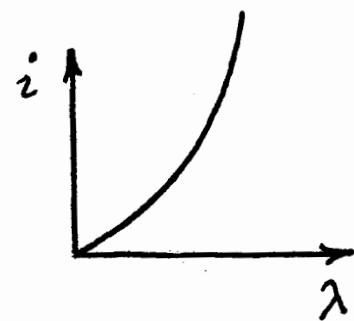
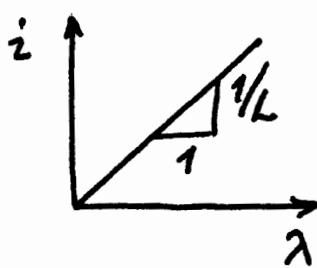
$$\frac{F}{x} \rightarrow C, \quad F = \left( \frac{3EI}{L^3} \right) x.$$

3-5



$$3-6 \quad L i = \lambda = \int e dt$$

7



$$i = i(\lambda)$$

$$\text{or } \lambda = \lambda(i)$$

$$\frac{di}{dt} = \frac{d i(\lambda)}{d\lambda} \cdot \frac{d\lambda}{dt}$$

$$\frac{d\lambda}{dt} = e = \frac{d\lambda(i)}{di} \cdot \frac{di}{dt}$$

$$= \frac{d i(\lambda)}{d\lambda} \cdot e$$

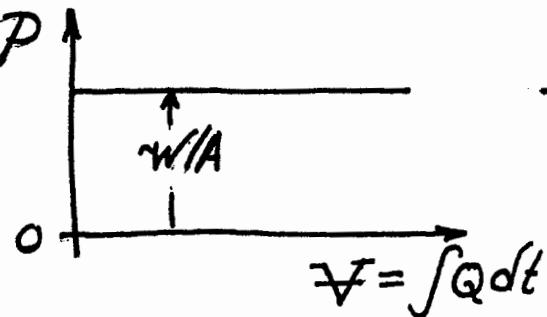
$$3-7 \quad \bar{F} = m \bar{a} = m \dot{\bar{v}} \quad \begin{array}{c} I \\ \overbrace{P_1 P_2}^{\uparrow} \downarrow P_3 \end{array}$$

$$P_1 A - P_3 A = \rho A L \cdot \frac{dQ_2/A}{dt}$$

$$\text{or } P_1 - P_3 = \left( \frac{\rho L}{A} \right) \cdot \frac{dQ_2}{dt} = P_2$$

$$P_2 = \int (P_1 - P_3) dt = \frac{\rho L}{A} \cdot Q_2$$

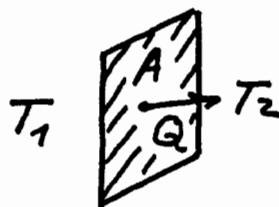
3-8



$$\frac{P}{Q} = C$$

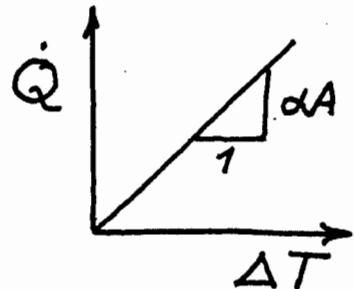
$$\nabla = \int Q dt$$

3-9



$$\frac{T_1}{Q} \quad \frac{R}{1} \quad \frac{T_2}{Q}$$

8



$$\dot{Q} = \alpha A (T_1 - T_2)$$

3-10

$$\tau = I\alpha, P_{\tau} = \int \tau dt = I\omega$$

$$I = \frac{1}{2} m R^2 = \frac{1}{2} \rho \cdot \pi R^2 t \cdot R^2 \\ = \frac{0.28 \pi \cdot 1 \cdot (5)^4}{2 \cdot 386} = 0.712 \text{ kg s}^2 \text{ m}$$

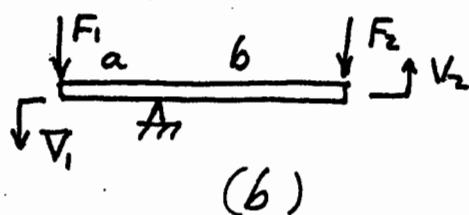
3-11

$$\frac{F}{V} \tau F \frac{P}{Q}, \text{ Area} = A$$

$$F = AP$$

$$AV = Q$$

3-12



$$\frac{F_1}{V_1} \tau F \frac{F_2}{V_2}$$

$$a F_1 = b F_2$$

$$\frac{V_1}{a} = \frac{V_2}{b}$$

$$(c) \frac{\tau_1}{\omega_1} \tau F \frac{\tau_2}{\omega_2}$$

$$\omega_1 \nu_1 = \omega_2 \nu_2, \quad \left. \begin{array}{l} \tau_1 / \nu_1 = \tau_2 / \nu_2, \\ \tau_1, \tau_2 \text{ radii of gears} \end{array} \right\}$$

$$3-13 \quad \text{Ang. Momentum} = \bar{H} \quad 9$$

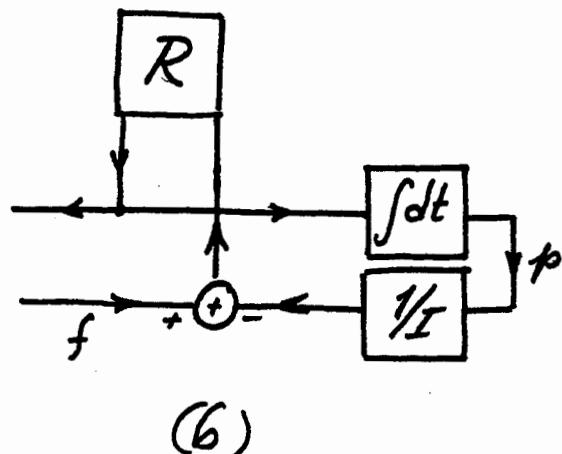
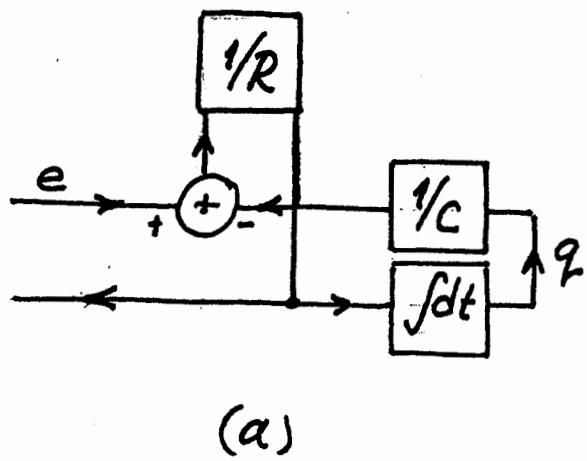
$|H| \approx J\Omega$ , torques associated with  $F_1$  and  $F_2$  cause change in direction of  $\bar{H}$  not magnitude. Consider  $F_1$  first; let shaft length be  $L$ . Torque is then  $F_1 L$ ,  $\dot{\tau} = \dot{H}$  means that tip of  $\bar{H}$  vector must move up with angular rate  $V_2/L$ .  $|H| = J\Omega \cdot V_2/L = F_1 L$

so

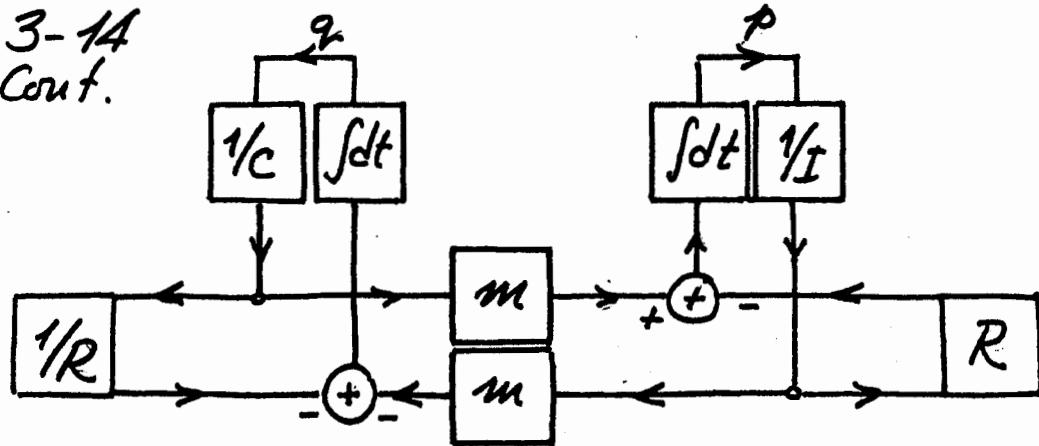
$$F_1 = \left( \frac{J\Omega}{L^2} \right) V_2 \quad \left. \begin{array}{l} \\ \end{array} \right\} \frac{F_1}{V_1} GY \frac{F_2}{V_2}$$

Similarly  $F_2 = \left( \frac{J\Omega}{L^2} \right) V_1$

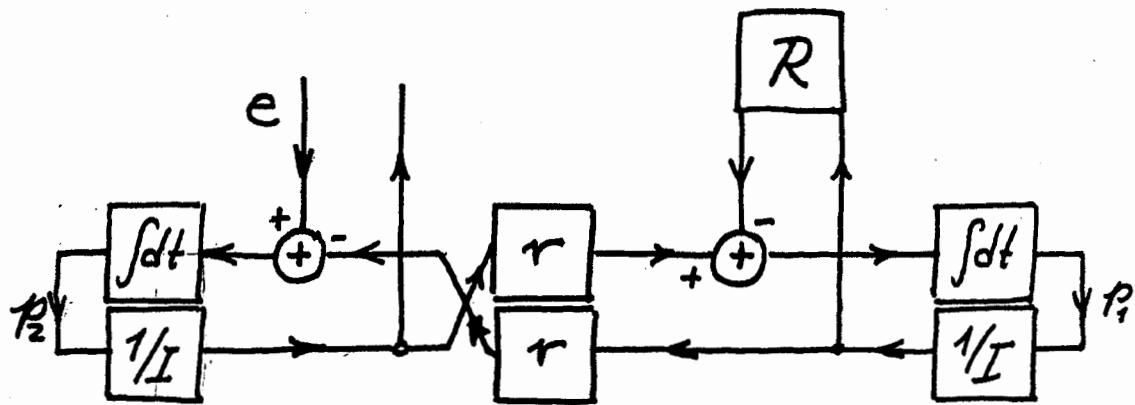
3-14



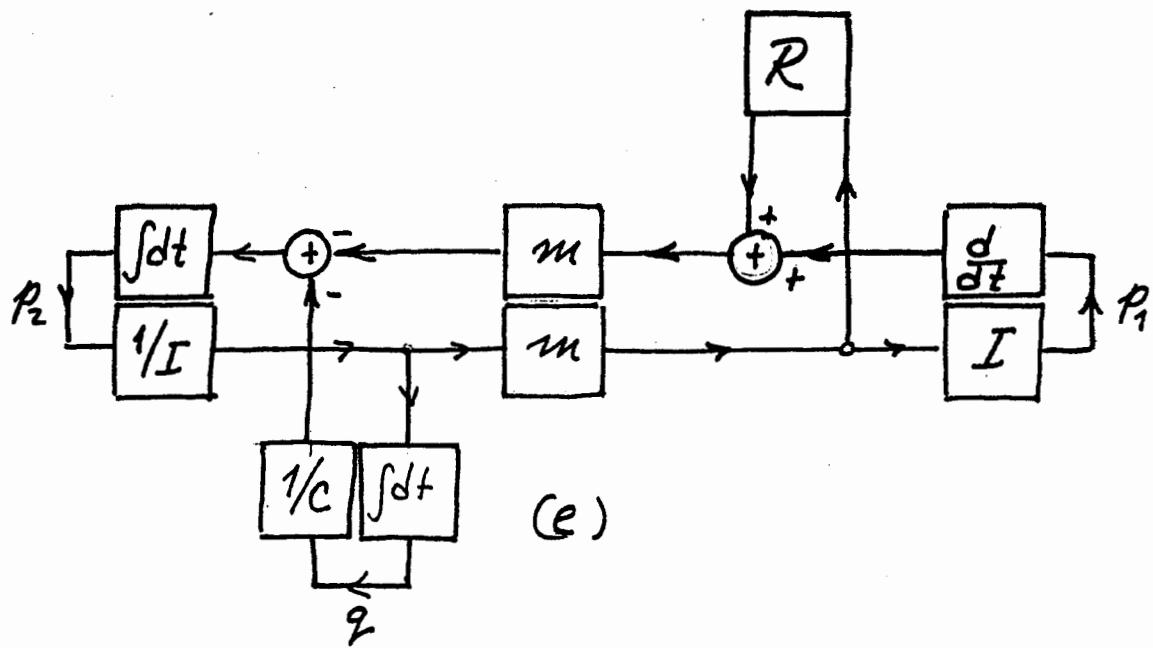
3-14  
Cont.



(C)

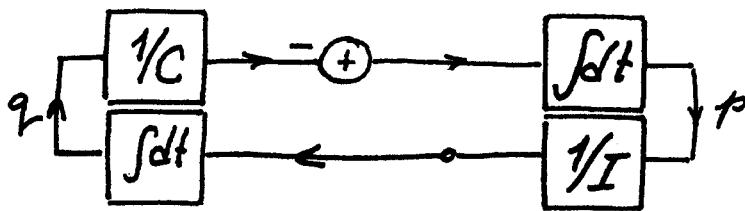


(d)



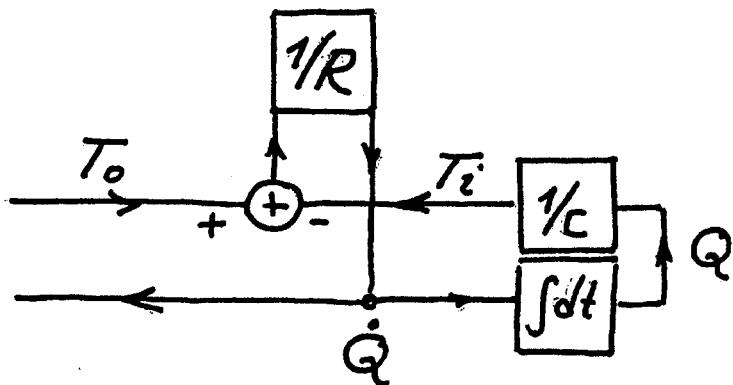
(e)

3-15



11

3-16



3-17

$$\frac{\tau}{\omega} \rightarrow TF \frac{F}{V} \quad \tau = r F \\ r\omega = V$$

$$3-18 \quad \frac{e}{i} \rightarrow G \ddot{y} \frac{F}{V} \rightarrow I$$

$$e = \tau V = \tau \frac{p}{I} = \tau \frac{\int F dt}{I} \\ = \frac{\tau}{I} \int \tau i dt = \frac{\tau^2}{I} \int i dt = \frac{\tau^2}{I} \cdot q$$

$$\text{so } \frac{1}{C} \leftrightarrow \frac{\tau^2}{I}$$

3.19

12

$$P = P_0 \frac{V_0^r}{V^r} = \frac{P_0 V_0^r}{(V_0 - A_p x)^r} = \left[ \frac{P_0}{1 - \frac{A_p x}{V_0}} \right]^r$$

$P$  is absolute pressure:

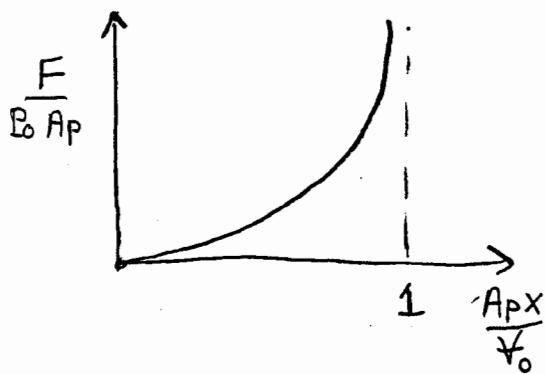
$P - P_0$  is gage pressure in cylinder,

$$(P - P_0) A_p = F$$

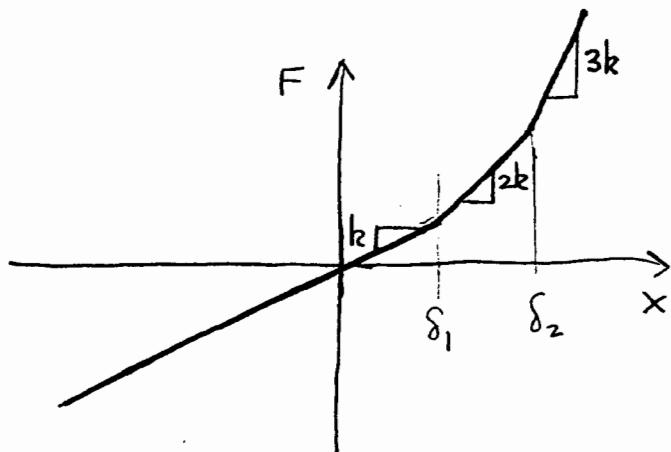
or

$$F = \left\{ \frac{P_0}{\left[ 1 - \frac{A_p x}{V_0} \right]^r} - P_0 \right\} A_p$$

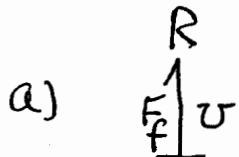
$$F = P_0 A_p \left[ \left( \frac{1}{\left( 1 - \frac{A_p x}{V_0} \right)^r} - 1 \right) \right]$$



3.20



3.21

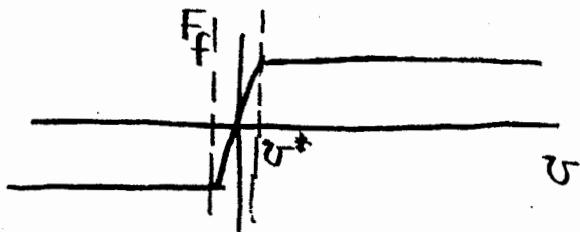


The only possible causality for the friction model shown in the problem is "effort" out, "flow" in.

For any specified velocity,  $F_f$  can be computed, but if  $F_f$  is specified,  $v$  is indeterminant.

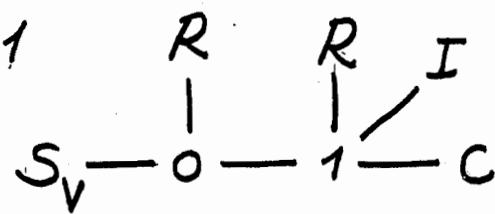
- (b) If used simply as  $\bar{F}_f = \mu N$ , then  $F_f$  will be applied when  $v=0$ , which is not correct. When  $v=0$ , the mass "sticks", and the friction force exactly balances all other forces on the mass. When the other forces exceed the "stick" force, then  $\bar{F}_f$  returns to  $F_f = \mu N$ .

A possible change in the constitutive law might be,



For  $v^*$  very small, the fundamental character of friction is maintained.

4-1



14

