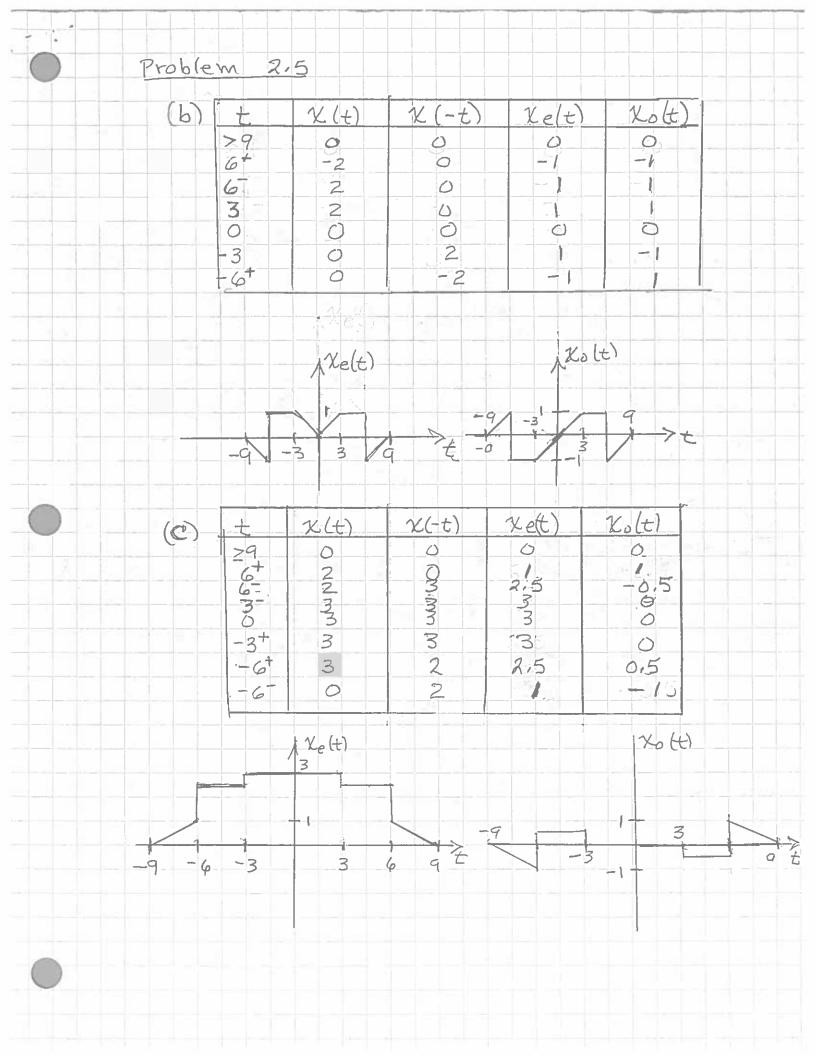


Solution P2.4 $(a) y(t) = -2\Re(-t/2 + 2) + 4$ = 7 C = -t/2 + 2 = 7 t = -2C + 4 = 7 C = -t/2 + 2 = 7 t = -2C + 4 = 7 C = -2C + 4(b) $\chi(t) = -\frac{1}{2}y(2t+4)+2 \Rightarrow \tau = -2t+4$ $= t = \frac{1}{2}\tau+2$

Problem 2.5 (a) $\chi_{e(t)} = \frac{1}{2} \chi(t) + \chi(-t)$ (2.13) $\chi_{0}(t) = 1/2 [\chi(t) - \chi - t)] (2.14)$ X(t) X(-t) Xe(t) Xo(t) t 0 0 3/2 1/2 1,25 0.25 73 73 0 0 3 2 1 to5 15 1 0-0.25 \bigcirc 1.25 1.5 -1.5 20 3/2 -3 -1/2 O \bigcirc 2-3 0 1.51 Kelt) Axott) 1 +1/2 -3 -3 +-1/2 3 3 verify Xolt) + Xelt) = X(t)



Problem 2.5 (d) $\mathcal{K}(-t)$ Ko(t) t>8+ 3+3+-3+-3+-4+-8+ 48^{-} Ke(t) X(+) 0000 -1 -1 -2 m m m m 1.55 1.5 1,5 ON NN N -00 -1.5 0 0 -0,5 0.5 0 -2 \odot 1 xxelt) 2 AX o(t) 2 -4 -3 7 8 -8 34 -1-- 2'

Problem 2.6 $(a) \chi(t) = -4t \implies \chi(-t) = 4t$ x(t)=-x(-t) . x(t) is odd (b) $\chi(t) = e^{-|t|} \Rightarrow \chi(-t) = e^{-|t|} = e^{-|t|}$ $\chi(t) = \chi(-t)$ ·· $\chi(t)$ is even (C) $\chi(t) = 5\cos 3t \Rightarrow \chi(-t) = 5\cos 3(-t)$ -= 5 Cos-3t = 5 Cos 3t $\chi(t) = \chi(-t)$. $\chi(t)$ is even (d) $\chi(t) = sin(3t + 3T) = sin(3[t + T/2])$ $\chi(t) = -\cos(3t)$ $\chi(t) = \chi(-t)$: $\chi(t)$ is even (e) $\chi(t) = \mu(t) - \mu(-t) = \chi(-t) = \mu(-t) - \mu(t)$ = - [u(t) - u(-t)]K(t) = - X(-t) :. K(t) is odd $(f) \chi(t) = - u(t-1) + u(-t-1)$ $\chi(-t) = -u(-t-1) + u(t-1)$ $\chi(-t) = -\chi(t)$, $\delta = \chi(t)$ is odd

PROBLEM 2.7 (a) $\int_{T}^{T} \chi_{o}(t) = \int_{T}^{0} \chi_{o}(t) H \int_{0}^{T} \chi_{o}(t) dt$; $\chi_{o}(t) = -\chi_{o}(-t)$ $\left. : \int_{-T}^{0} \chi_{o}(t) dt = - \int_{-T}^{0} \chi_{o}(-t) dt \right|_{t=-T} = \int_{-T}^{0} \chi_{o}(t) dT = - \int_{-T}^{T} \chi_{o}(t) dT$ $\int_{-T}^{T} \chi_{o} tt dt = 0$ (b) $\int_{T}^{T} \chi_{o} tt dt = \int_{-T}^{T} [\chi_{o} tt] dt = \int_{T}^{T} [\chi_{o} tt] dt = \int_{T}^{T} \chi_{o} tt dt$ and $A_x = \lim_{T \to \infty} \frac{1}{2T} \int_T \chi(t) dt = \lim_{T \to \infty} \frac{1}{2T} \int_T \chi_e(t) dT$

(c) $x_0(0)=-x_0(-0)=-x_0(0)$. The only number with a=-a is a=0 so this implies $x_0(0)=0$. $x(0)=x_c(0)+x_0(0)=x_c(0)$.

PROBLEM 2.8

6

(a) Let z(t) be the sum of two even functions $x_1(t)$ and $x_2(t)$. To show that z(t) is even, we need to show that z(t) = z(-t) for all t. This is easy to show, since $z(t) = x_1(t) + x_2(t)$ and $z(-t) = x_1(-t) + x_2(-t)$ (since to get z(-t) we just plug in -t everywhere for t, which amounts to just plugging in -t in $x_1(t)$ and $x_2(t)$). Now since $x_1(t)$ and $x_2(t)$ are even, by definition $x_1(t) = x_1(-t)$ and $x_2(t) = x_2(-t)$ so $x_1(t) + x_2(t) = x_1(-t) + x_2(-t)$ so z(t) = z(-t).

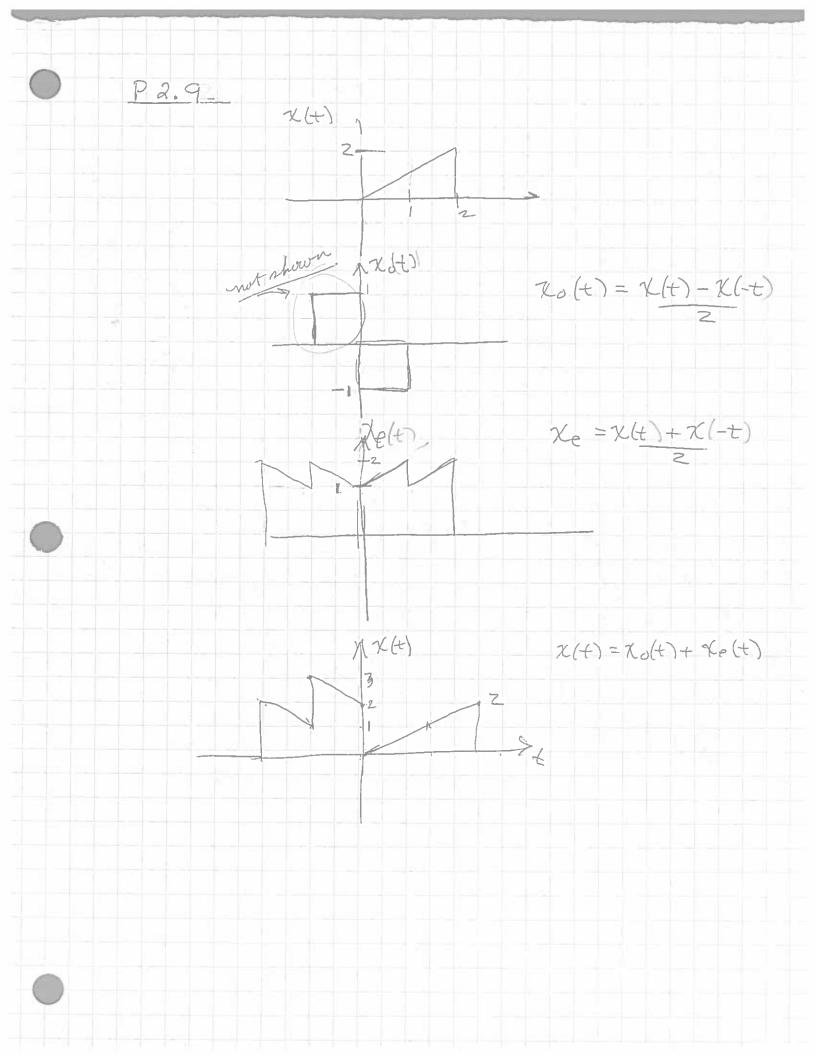
(b) Let $x_1(t)$ and $x_2(t)$ be two odd functions. Then $x_1(-t) + x_2(-t) = -x_1(t) + (-x_2(t)) = -(x_1(t) + x_2(t))$ which shows that $x_1(t) + x_2(t)$ is odd.

(c) Let $z(t) = x_1(t) + x_2(t)$ as in part a, where now $x_1(-t) = x_1(t)$ and $x_2(-t) = -x_2(t)$. We need to show that $z(t) \neq z(-t)$, $z(t) \neq -z(-t)$. Consider that $z(-t) = x_1(-t) + x_2(-t) = x_1(t) - x_2(t)$. In order to have z(t) be even, we would therefore need to have $x_1(t) + x_2(t) = x_1(t) - x_2(t)$ for all t, which is equivalent to having $x_2(t) = -x_2(t)$ for all t, which is not possible for nonzero $x_2(t)$. Similarly, in order to have z(t) be odd, we would need to have $z(t) = -z(t) \implies x_1(t) + x_2(t) = x_2(t) - x_1(t)$, which is not possible for nonzero $x_1(t)$. So the sum of an even and odd function must be neither even nor odd.

(d) Let $z(t) = x_1(t)x_2(t)$ where $x_1(t) = x_1(-t)$ and $x_2(t) = x_2(-t)$. Then $z(-t) = x_1(-t)x_2(-t) = x_1(t)x_2(t) = z(t)$ which shows that z(t) is even.

(e) Let $z(t) = x_1(t)x_2(t)$, where $x_1(t) = -x_1(-t)$ and $x_2(t) = -x_2(-t)$. Clearly z(t) is even because $z(-t) = x_1(-t)x_2(-t) = (-x_1(t))(-x_2(t)) = x_1(t)x_2(t) = z(t)$, which is the definition of evenness.

(f) Let $z(t) = x_1(t)x_2(t)$, where $x_1(t) = -x_1(-t)$ and $x_2(t) = x_2(-t)$. Clearly z(t) is odd because $z(-t) = x_1(-t)x_2(-t) = (-x_1(t))x_2(t) = -x_1(t)x_2(t) = -z(t)$, which is the definition of oddness.



PROBLEM 2.10

(a) $\sin(t) = \sin(t + n2\pi)$ for any integer n, so $7\sin(3t) = 7\sin(3t + n2\pi) = 7\sin\left(3(t + n\frac{2\pi}{3})\right)$; therefore x(t) is periodic with fundamental period $T_0 = \frac{2\pi}{3}$ and fundamental frequency $\omega_0 = \frac{2\pi}{T_0} = 3$. (b) $\sin(8(t + \frac{2\pi}{8}) + 30) = \sin(8t + 2\pi + 30) = \sin(8t + 30).$ $\omega_0 = 8$ and $T_0 = \frac{2\pi}{8} = \frac{\pi}{4}$. (c) $e^{jt} = \cos(t) + j\sin(t)$ is periodic with fundamental period 2π , so e^{j2t} is periodic with fundamental period $\frac{2\pi}{2} = \pi$, and fundamental frequency $\omega_0 = 2$. (2) Cos 2+ + sin 5t $T_{1} = 2 \overline{\underline{T}} = T_{1}, T_{2} = 2 \overline{\underline{T}} \xrightarrow{T_{1}} T_{2} = 2 \overline{\underline{T}} \xrightarrow{T_{2}} T_{2} = 2 \overline{\underline{T}} \xrightarrow{T_{2}} T_{2} = 2 \overline{\underline{T}} \xrightarrow{T_{1}} T_{2} = 2 \overline{T} \xrightarrow{T_{1}} T_{2} =$ To-RoTiso To = RTT(s), (periodic) (e) $e^{-j(10t+17/3)} = e^{-jT/3}e^{-j10t} = c_{00}TT/3 - j.5inTT/3)e^{-j10t}$ = (0,5+ 10.866) e- Hot To = 2TT = TT_5(2), periodic (F) edist_ edist efist & efzot are both periodic $T_1 = 2TT$ $T_2 = 2TT$ $= \frac{T_1}{20} = \frac{2/15}{T_2} = \frac{2/15}{10} = \frac{20}{15}$ ratio of integera $\frac{20}{15} = 4 \implies \frac{1}{20} = 3 \quad \text{in } T_0 = 3T_1 = 2T_1 \text{ and } T_1 = 2T_1 \text{ and }$ $\frac{211}{15} = 3$, $\frac{211}{215} = 4$

$$\begin{array}{c} P_{2,11} \\ (A) \ \chi(t) = loc \ 3t + \ \text{din5t} \\ (b) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{Tt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{Tt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} + \ \text{ain} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{cost} \ \text{qt} \\ (c) \ \chi(t) = \ \text{qt} \ \chi(t) = \ \text{qt} \\ (c) \ \chi(t) = \ \text{qt} \ \chi(t) = \ \text{$$

1

and a summer of the state of the

 $\frac{3.12}{(a1 \times (t))} = 5 \sin(15t - 60^{\circ}) + 2 \sin(7t)$ X, (t) = 5 sin (15t - 60°) is periodice W, = 15 rad/s $\chi_2(t) = 2 \text{ sul7t}$ 11 11 $\omega_2 = 7 \text{ sud}/5$ $T_1 = \frac{2\pi}{15} \quad T_2 = \frac{2\pi}{7} \quad \frac{T_4}{T_2} = \frac{7}{15} \times \frac{\pi}{15} \text{ atro of inleger}$ $k_0 = 15 \implies T_0 = 15T_1 = aTT a$ (b) X, (t)= 5 ain 5th is periodic W:=5:-TK2= 15/5=3/5 T1/13=7/51 lendenon=5 $T_0 = 5T_1 = 2T$ (C) $K_1(t)$ is periodec $T_1 = 2tT = 2$ $\chi_2 \neq 15$ periodec $T_2 = \frac{2tT}{3}$ TI = Z = B not vational ... Sum not T2 2TT/3 TT not vational ... Sum not To cos ATT to periodic uy TI = 2TT/ATT = 1/2 (d) $\stackrel{>}{\stackrel{>}{=}} reet(\frac{t+W_2}{0.2})$ is periodec with $T_1 = 0.5 \pm m = -\infty$ 4 sin (5# + #1/4) is periodic w/ Tz = 21 = 14 517/2 :5 $\frac{T_1}{T_2} = \frac{1}{1/2} = \frac{$

PROBLEM 2.13

(a) For x₁(t) + x₂(t) to be periodic we need some number T such that x₁(t+T) + x₂(t+T) = x₁(t) + x₂(t) for all t. This can only be true if x₁(t+T) = x₁(t) and x₂(t+T) = x₂(t), which can only be true if T = k₁T₁ and T = k₂T₂ (T is an integer multiple of both the periods). So we need there to be some integers k₁ and k₂ such that k₁T₁ = k₂T₂ ⇒ T₁/T₂ = k₂/k₁.
(b) Put k₂/k₁ in its most reduced form n/m by canceling any common terms in the numerator and denominator; then T₀ = nT₂ = mT₁.

Problem 2.14

(a)

>> syms t >> xa=5*exp(-t/2); >> ezplot(xa), grid

(c)

>> syms t
>> xc=5*exp(t/2);
>> ezplot(xc),grid

(e)

>> syms t
>> xe=5*(1-exp(-2*t));
>> ezplot(xe), grid

(g)

>> syms t >> xg=5*exp(-2*t)*2*sin(2*t); >> ezplot(xg),grid (b) >> syms t >> xb=5*exp(-2*t); >> ezplot(xb),grid

(d)

>> syms t
>> xd=5*(1-exp(-t/2));
>> ezplot(xd), grid

(f)

>> syms t >> xf=5*2*sin(2*t); >> ezplot(xf),grid

(h)

>> syms t >> xh=5*exp(-0.5*t)*2*sin(2*t); >> ezplot(xh),grid Problem 2.15

PROBLEM 2.16

(a)

(b) $\cos(\theta + \phi) = \operatorname{Re}\{e^{j(\theta + \phi)}\} = \operatorname{Re}\{e^{j\theta}e^{j\phi}\}$ $\sin(\theta + \phi) = \operatorname{Im} \{ e^{j(\theta + \phi)} \} = \operatorname{Im} \{ e^{j\theta} e^{j\phi} \}$ = Im{($\cos\theta + j\sin\theta$)($\cos\phi + j\sin\phi$) $= \operatorname{Re}\{(\cos\theta + j\sin\theta)(\cos\phi + j\sin\phi)\}\$ $= \operatorname{Im}\{(\cos\theta\cos\phi + j\sin\theta\cos\phi)\}$ $= \operatorname{Re}\{\cos\theta\cos\phi + j\sin\theta\cos\phi\}$ + $i \cos\theta \sin\phi - \sin\theta \sin\phi$ + $j\cos\theta\sin\phi - \sin\theta\sin\phi$ } $=\cos\theta\sin\phi+\sin\theta\cos\phi$ $=\cos\theta\cos\phi-\sin\theta\sin\phi$

(d) (c) $\cos\theta\cos\phi = \operatorname{Re}\left\{e^{j\theta}\frac{e^{j\phi}+e^{-j\phi}}{2}\right\} = \operatorname{Re}\left\{\frac{e^{j(\theta+\phi)}+e^{j(\theta-\phi)}}{2}\right\}$ $\sin\theta\cos\phi = \operatorname{Im}\left\{e^{j\theta}\frac{e^{j\theta}+e^{-j\theta}}{2}\right\}$ $= \operatorname{Im}\left\{\frac{e^{j(\theta+\phi)} + e^{j(\theta-\phi)}}{2}\right\}$ $=\operatorname{Re}\left\{\frac{e^{j(\theta+\phi)}}{2}+\frac{e^{j(\theta-\phi)}}{2}\right\}=\frac{\cos(\theta+\phi)}{2}+\frac{\cos(\theta-\phi)}{2}$ $=\frac{1}{2}\left[\sin(\theta+\phi)+\sin(\theta-\phi)\right]$

(a) x(t) = 3 Cos (2t) + sin(2t) $\chi(t) = \frac{3}{2} \left(e^{\frac{3}{2}t} + e^{\frac{3}{2}t} \right) + \frac{1}{2} \left(e^{\frac{3}{2}t} - e^{-\frac{3}{2}t} \right)$ = 3-1/2) e^{12t} + 3+12)e^{-12t} $= \frac{\sqrt{10^{1}}}{2} \frac{1}{100} \left(\frac{1}{3}\right) e^{\frac{1}{2}t} + \frac{\sqrt{101}}{2} \left(\frac{4}{10} + \frac{1}{3}\right) e^{\frac{1}{2}t} + \frac{1}{2} e^{\frac{1}{2}t}$

> tan (1/3) =-0.32 rad tan (+1/3) =+0.32 rad $K(t) = \frac{\sqrt{107}}{2} e^{\frac{1}{2}0.32} \frac{1}{2} \frac{1}{2} e^{\frac{1}{2}} e^{\frac{1}{2}}$

X(+)= VIOT Cos (2+-0.32 rad) = 3.16 Cor (2t-18.33°)

Problem 2.1.6 (Continued) (b) $\chi(t) = 4 \cos(4\pi t) + 3 \sin(4\pi t)$ $= 4\left(\underbrace{e^{\frac{4}{7}} + e^{-j4\pi t}}_{2}\right) + 3\left(\underbrace{e^{\frac{1}{7}} + \pi t}_{2j}\right)$ $=(2-3/2i)e^{24\pi t} + (2+3/2i)e^{-24\pi t}$ $(2^{-3}/_{2}j) = (2)^{2} + (3/_{2})^{2} / tan(\frac{-1}{2}) = \frac{5}{2} / tan(\frac{-3}{4})$ = 5, 030.64 $\begin{aligned} \chi(t) &= \frac{5}{3}e^{-\frac{1}{2}0.64} + \frac{5}{2}e^{-\frac{1}{2}0.64} - \frac{1}{2}4\pi t \\ &= 5 + \frac{2}{5}e^{-\frac{1}{2}(4\pi t - 0.64)} + \frac{1}{2}e^{-\frac{1}{2}(4\pi t - 0.64)} \end{aligned}$ $\chi(t) = 5 \cos(4\pi t - 0.64 \tan d)$ 02 5 Cos (417t-36.87°) (C) X(t) = A Cos (wot) + B sin(wot) = A e Just - Just Betwar - just = A-1B E Jwot + A+11B = Jwot = VA2+B2 / Tam B etwot + VA2+B,27 / tan (B) e Juot $= \sqrt{A^2 + B^2} e^{\frac{1}{A} - B} e^{\frac{1}{A} - B} = \frac{1}{A} e^{\frac{1}{A} - B} e^{$ $2 \tan\left(\frac{B}{A}\right) = -\tan\left(\frac{-B}{A}\right)$ $(X(t) = VA^{2}+B^{2} G G (Wot - tan B/A) - J(Wot - tan B/A) + C$ = VA2+B2 Cos (Wot - Tan (B/A))

PROBLEM 2.17) s(at-b) sin²(t-c) dt $S(at-b) = S(a(t-b|a)) = \frac{1}{a}S(t-\frac{b}{a})$ $\int_{-\infty}^{\infty} \frac{\xi(t-b)a}{a} \sin^{2}(t-c) = \sin^{2}(\frac{b}{a}-c) \xi(t-b)a}{-\infty}$ = { sin2 (b/a-c) $\frac{P_{ROBLEM 2.18}}{(a)} y(t) = \int \chi(\tau) [S(\tau+5) - S(\tau-5)] d\tau$ $\chi(\tau)s(\tau-a) = \chi(a)s(\tau-a)$ $\frac{1}{2} \cdot \frac{1}{2} (t) = \chi(t) \frac{1}{2} \cdot \frac{1}{$ (b) $y(t) = \frac{1}{2} \left(\chi(t) e^{3T/2t} \frac{1}{5} (7t-3) dt \right)$
$$\begin{split} & \{2t-3\} = \frac{1}{2} \delta(t-3/2) \\ & \frac{1}{2} \delta(t-3/2) \chi(t) e^{3 \pi t/2} = \frac{1}{2} \chi(3/2) e^{3 \pi t/4} \end{split}$$
 $:: y(t) = \frac{1}{4} \chi(\frac{3}{2}) e^{\frac{3}{3}T_{4}} \left(\frac{1}{8(t-3/2)} dT \right)$ Y(+) = 1/4 X(3/2) e 2311/4.

PROBEM 2.49
(a) Lett
$$T = at$$
, then $\int \delta(at) dt = \int \delta(t) dT$
 $= \frac{1}{a} \int \delta(t) dT \Rightarrow \delta(at) = \frac{1}{a} \delta(t), a > 0$
for $a < 0, at = T \Rightarrow -|a| t = T$
 $\Rightarrow dt = -dT$
 $at = -dT$

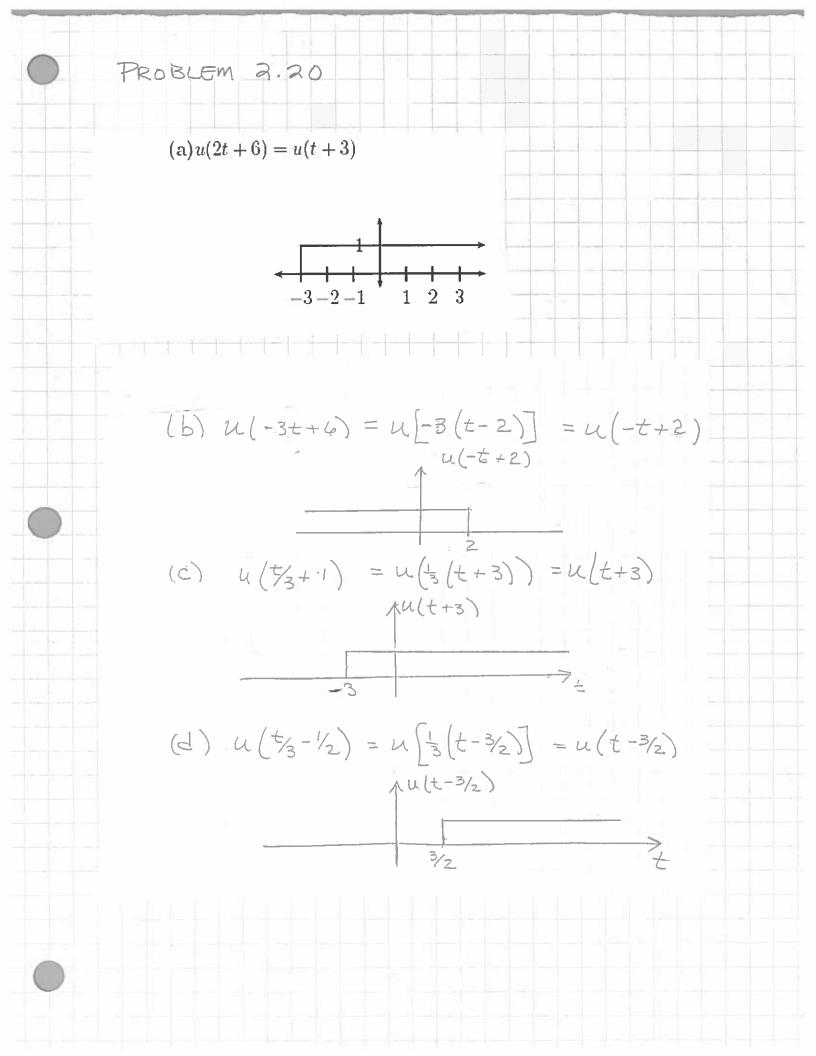
function: $\delta(t-t_0)$ is nonzero only at $t = t_0$, so $x(t)\delta(t-t_0) = x(t_0)\delta(t-t_0)$ and $\int_{-\infty}^{\infty} x(t)\delta(t-t_0)dt = x(t_0)$.

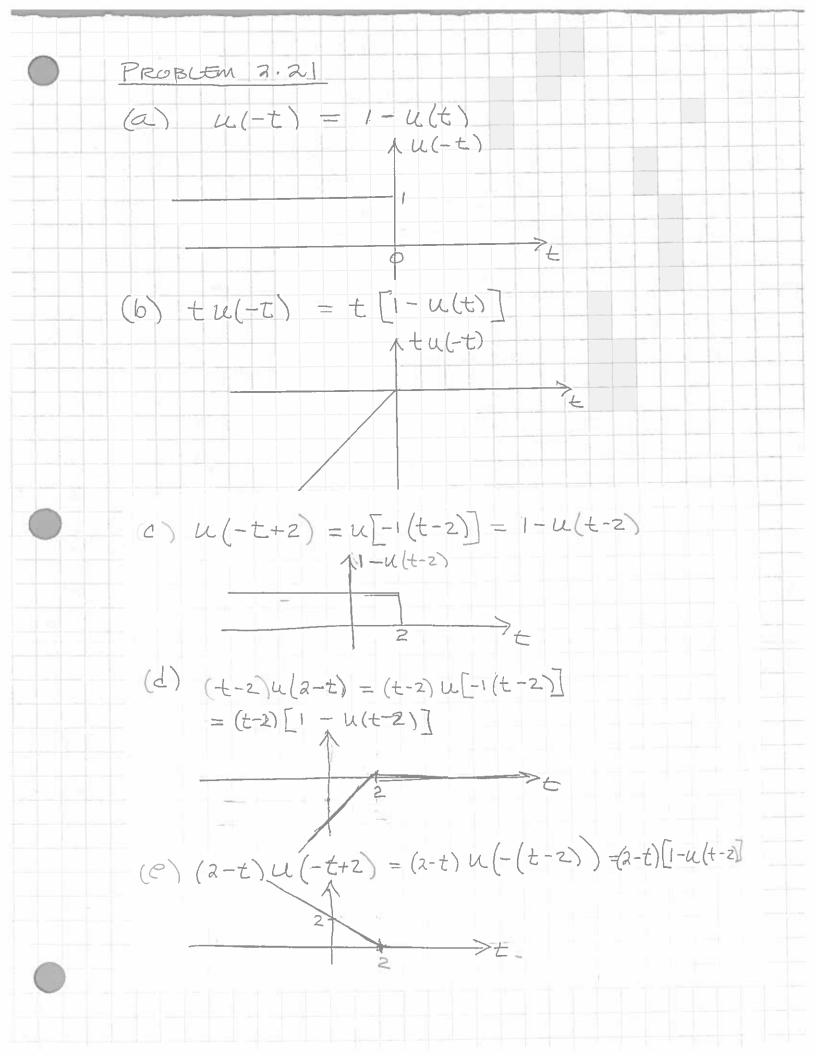
i) $\int_{-\infty}^{\infty} \cos(2t)\delta(t)dt = \cos(2\cdot 0)\int_{-\infty}^{\infty} \delta(t)dt = 1.$

ii) $\delta(t - \frac{\pi}{4})$ is a time-shifted version of $\delta(t)$, and is nonzero only at $t = \frac{\pi}{4}$. So:

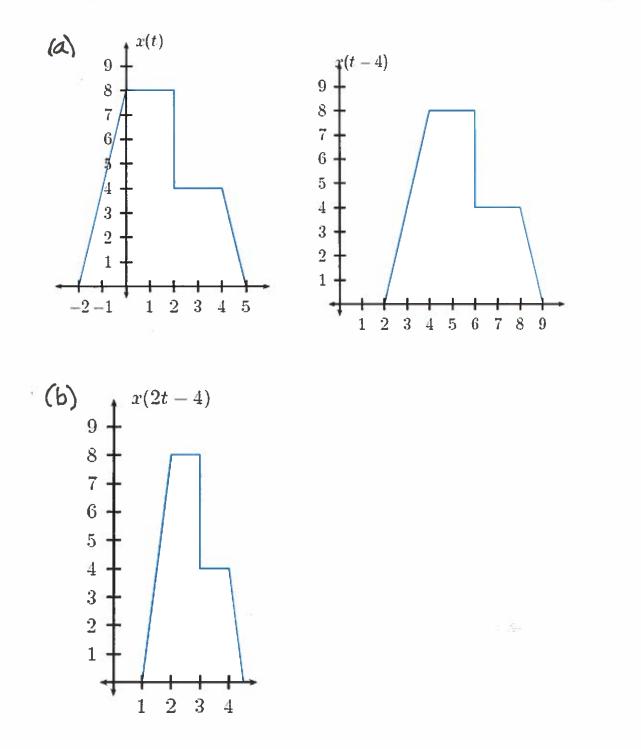
$$\int_{-\infty}^{\infty} \sin(2t)\delta(t-\frac{\pi}{4})dt = \int_{-\infty}^{\infty} \sin(2\cdot\frac{\pi}{4})\delta(t-\frac{\pi}{4})dt$$
$$= \sin(\frac{\pi}{2})\int_{-\infty}^{\infty}\delta(t-\frac{\pi}{4})dt = \sin(\frac{\pi}{2}) = 1$$

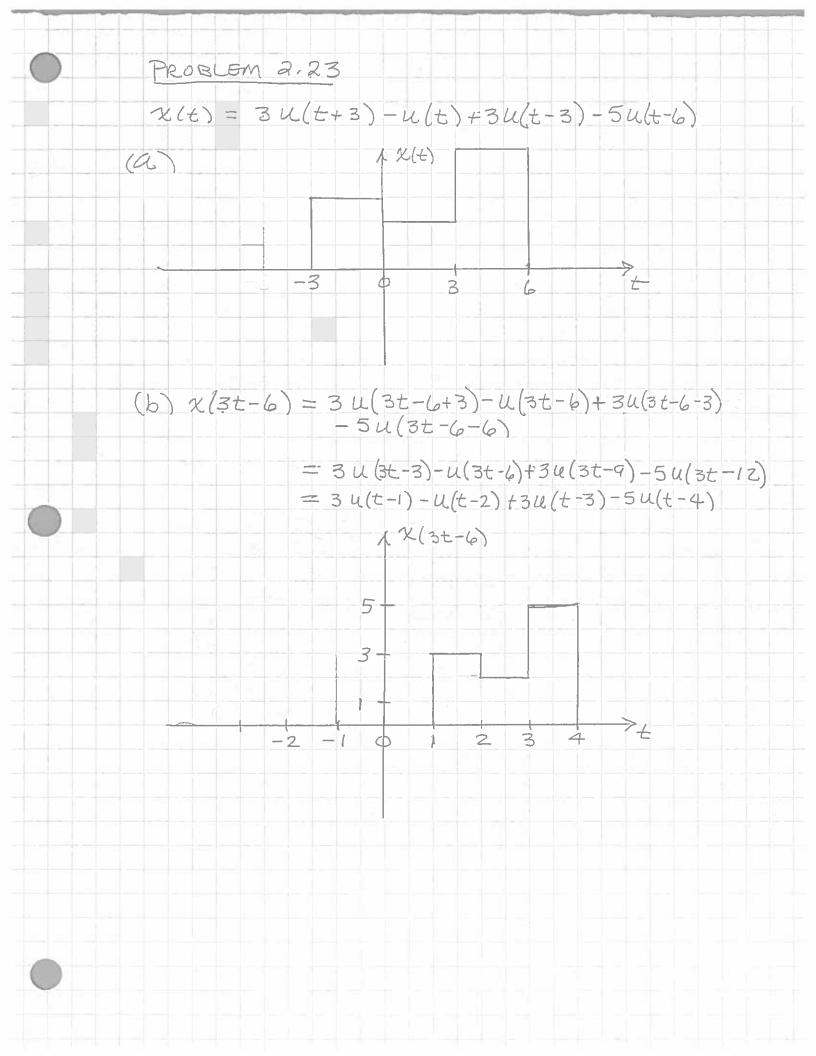
 $\frac{2.19}{(c)(iii)} \int sin(at) s(t-7/6) dt$ $= \int_{-\infty}^{\infty} \sin(2\pi/6) S(t-\pi/6) dt = \sin(\pi/3) \left(S(t-\pi/6) dt\right)$ $= \operatorname{Ain}(TV_3) = 0.866$ $(iv) \int \sin\left[\left(t - \pi T_{4}\right)\right] s\left(t - \frac{\pi}{2}\right) dt = \int \sin\left(\frac{\pi}{2} - \pi T_{4}\right) s\left(t - \pi T_{2}\right) dt$ $= \sin\left(\frac{\pi}{4}\right) \int s\left(t - \pi T_{2}\right) dt = 0.707$ $(V) \int Sm(t-T_{6}) S(at-aT_{3}) dt = \int Sin(t-T_{6}) S[z(t-T_{3})] dt$ $= \int \delta m \left(\frac{\pi}{3} - \frac{\pi}{6} \right) \delta \left[2 \left(t - \frac{\pi}{3} \right) \right] dt = \frac{1}{2} \delta m \left(\frac{\pi}{6} \right) = 0.25$

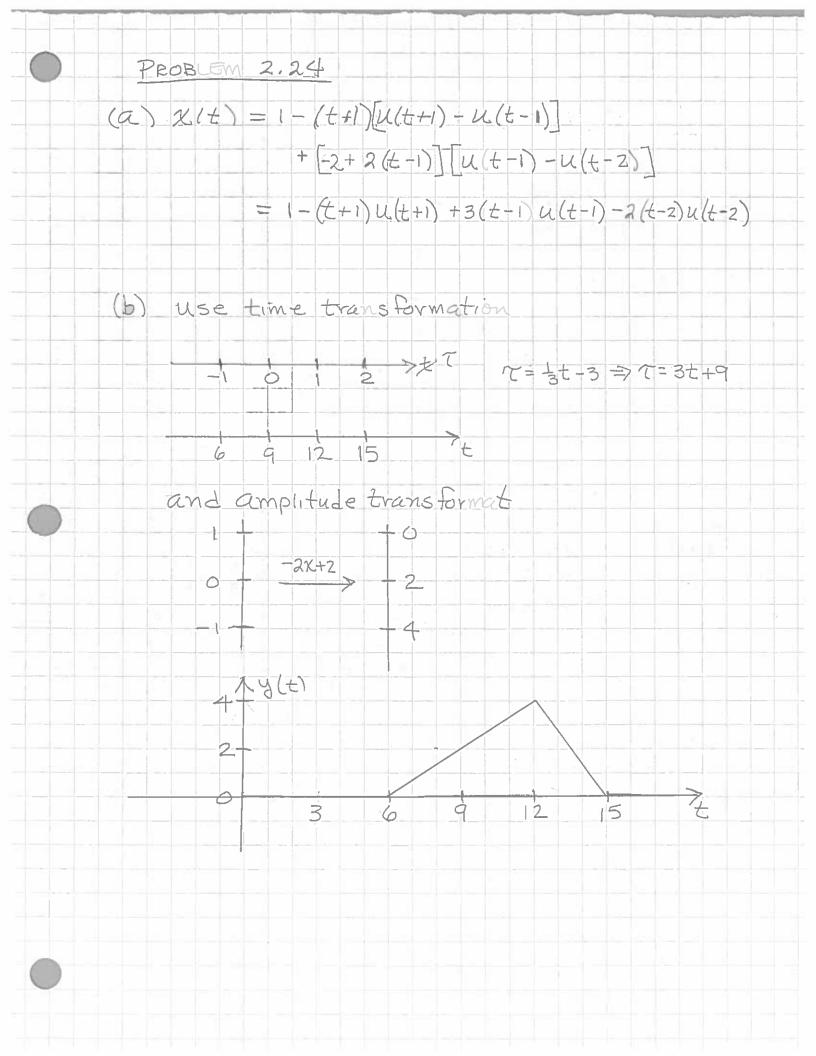




 $\begin{aligned} x(2t-4) &= 4 [(2t-2)u(2t-2) - (2t-4)u(2t-4) - u(2t-6) - (2t-8)u(2t-8) - (2t-9)u(2t-9)] \\ &= 4 [(2t-2)u(t-1) - (2t-4)u(t-2) - u(t-3) - (2t-8)u(t-4) - (2t-9)u(t-4.5)] \end{aligned}$



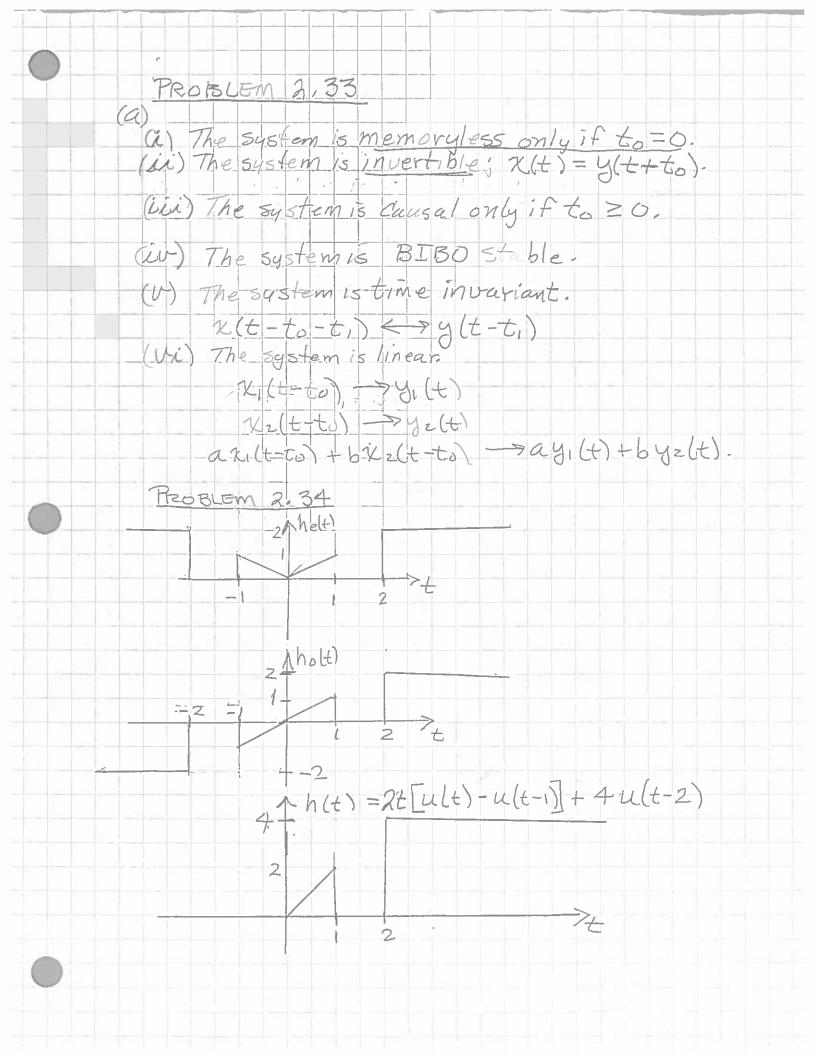




PROBLEM 2.25 (a) $\chi_{t}(t) = 2tutt) - \frac{1}{t-1}u(t-1) + 2(t-2)u(t-2)$ (b) \$<0, X, 1t)=0" 0<+<1, 7, (+)=2t" 1<2~2, X, tt)= 2t-4t+4=4-2t 2<t, x, t)=4-2t+2t-4=0" (c) $\chi(t) = \sum_{i=1}^{\infty} \chi_i(t-kT_0) = \sum_{i=1}^{\infty} \chi_i(t-2k)$ PROBLEM 2.26 $(a) \chi_{1}(t) = 3[t u(t) - (t-i)u(t-i)]$ -3[(t-2)u(t-2)-(t-3)u(t-3)] $(t<0) \quad \chi_1(t) = 0$ (ozt <1), X ((+) = 3t ~ $(1 < t < 2), \chi_1(t) = 3t - 3t + 3 = 3V$ (2<t<3), X1(+)= 3t -3t+3 -3t+6 = -3t+9 -(t>3), 2,(+)=3t-3t+3-3t+6+3t-9=0, (b) X2(t) is periodic with To = 4 $\chi_2(t) = \overset{\infty}{\underset{N=-\infty}{\overset{\times}{\overset{\times}}} \chi_1(t+4n)$ $= \frac{2}{3} \left[(t+4n)u(t+4n) - (t-1+4n)u(t-1+4n) \right]$ -3(t-2+4n)u(t-2+4n)-(t-3+4n)u(t-3+4n)]

PROBLEM 2.27 (a) $y_2(t) = T_2[T_1[x(t)]]$, $y_3(t) = T_3[T_1[x(t)]]$ ytt)= T2[T, [2(4)]] + T4 [T3[T, [2(2)]] + T5[2(2)] $(b) y(t) = T_3 \{ T_2 [T, [xt]] \} + \overline{y} \{ I_2 [T, [xt]] \} + \overline{T_3} [T, [xt]] \}$ (c) $y_3(t) = T_3[T_4[T_5[\chi(t)]]$ $y_4(t) = T_2[T_4[T_5[\chi(t)]]$ $Y_5(t) = T_1[T_5[X(t)]]$ $y(t)' = y_3(t) + y_4(t) + y_5(t)$ $Y(t) = [T_3[T_4[T_5[X(t)]] + T_2[T_4[T_5[X(t)]]]$ $= T + T [T_5 [x(t)]]$ $(d) \quad \underbrace{H(t)} = \underbrace{Y_3(t) \times \underbrace{Y_4(t) \times \underbrace{Y_5(t)}}_{}$ $J(t) = T_3 \left[T_4 \left[T_5 \left[\chi(t) \right] \right] \times T_2 \left[T_4 \left[T_5 \left[\chi(t) \right] \right] \times T_1 \left[T_5 \left[\chi(t) \right] \right] \right]$ PROBLEM 2.28 $m(tt) = T_2 \{ \chi(t) - T_4 [\chi(t)] \}$ y(+)=B[m(+)+T,[X(+)]} $y(t) = T_3 \{ T_2 [x(t) - T_4 [y(t)] + T_1 [x(t)] \}$ PROBLEM 2.29 $m(t) = T_2[X(t) - T_3[Y(t)] - T_4[Y(t)]]$ $Y(t) = T_{i}[m(t)]$ $y(t) = T_1 \{T_3[x(t)] - T_3[y(t)]\} T_4[y(t)] \}$

PROBLEM 2.30 (a) (i) The system has memory the output, y(t) depends on inputs 2(t) over a period of time. (ii) The system is not invertible. The input at time to cannot be determined from knowledge of the output at to. (Lin) The sigstem is stable. a bounded input will result in a bounded output. (iv) The system is time-invariant, (V) The system is linear. (b) The system is causal if y(to) depends on Values of X(t) for t ≤ to only. Therefore for causality to +1-α ≤ to ⇒ α≥1. PROBLEM 2.31 $(a) \quad y(t) = \cos \left[x(t-2) \right]$ US The system has memory (ii) The system is not invertible (ini) The system is causa (iv) / Cos(x) / ≤ 1 for al (x. : stable. $\begin{array}{l} (v) \quad y(t-t_0) = \chi(t-t_0-z) := time \ invariant, \\ (v_i) \quad y(t) = cos \left[\chi(t) + \chi_2(t)\right] \neq cos \chi(t) + cos \chi_2(t), \\ \vdots \quad not \ linear. \end{array}$ Problem 2.32 $(a) \times_{2}(t) = 2 \cdot u(t+1) - u(t) - u(t-1)$ = 2 [u(t+1) - u(t)] + [u(t) - u(t-1)] $= 2 \chi_{1}(t+1) + \chi_{1}(t)^{L}$ $= 2 \chi_{1}(t+1) + \chi_{1}(t)^{L}$ $(b) \chi_{1}(t) = u(t) + u(t-1) - 2u(t-2) => 4(t+1)$ $- \chi_{1}(-t)' - \chi_{1}(-t-1) = K_{2}(t)$ 2个化(生) 0127E -2-107 -117E $y_{2}(t) = y_{1}(-t-1) = y_{1}[-(t+1)]$



PROBLEM 2.35 (a) ii) memoryless Lii) y=1 for x==1, not invotible (iii) causal y=1%) (iv) stable (v) time invariant (vi) 12,+221 7 12,14/21 not linear (b) (i) <u>memoryliss</u> (ii) y=0 for 2 = 0, not inmitible (iii) <u>caneal</u> (iv) stable (v) time invariant (vi) y z,=1 7 y z,=z, not linear (C) (i) Memoryless: y(t) determined by current input. (in) not invertibles y(t) = I for all Xtt) <-1. (iii) Causal. (iv) stable: [y(t)] <] (U) time invariant. (Vi) not linear: y(t) = 1 for all values of K(t) <-1. (d)(i) Memoryless (ii) not invertible: y(t)=4 for all X(t) >2. (iii) Cousal (iv) Stable: 04y(+)44 (U) time invariant (Vi) not linear: y(+)= 4 for all K(+) = 2