

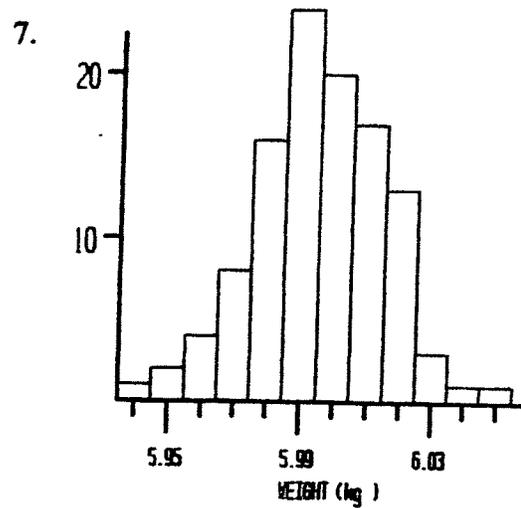
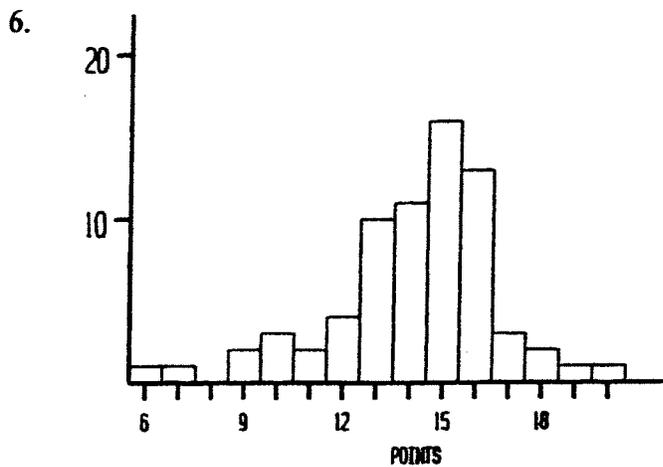
Chapter 5 FUNDAMENTALS OF STATISTICS

1. 0.86, 0.63, 0.15, 0.48

2, 3, Number	Boundaries	Precision	g.p.e.	r.e.
(a) 8.24	8.235 < 8.24 < 8.45	0.01	0.005	0.0006
(b) 522	521.5 < 522 < 522.5	1	0.5	0.001
(c) 6.3×10	625 < 630 < 635	10	5	0.002
(d) 0.02	0.015 < 0.02 < 0.025	0.01	0.005	0.3

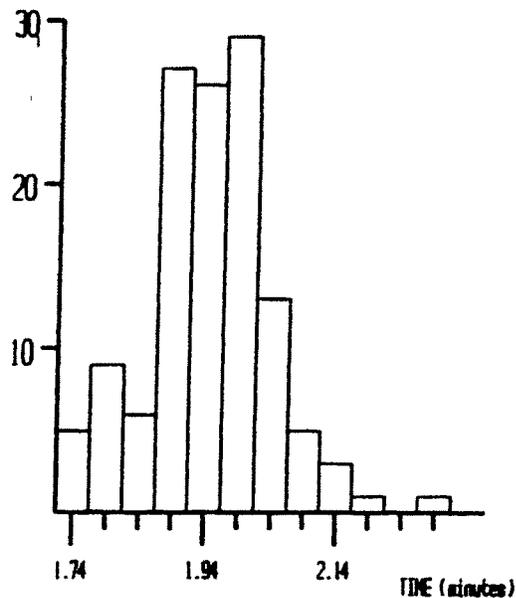
4. 2.84×10^2 , 22, 0.64, 0.8937, 0.9

5. 66.4, 379.1, 5, 4.652, 6.2×10^2

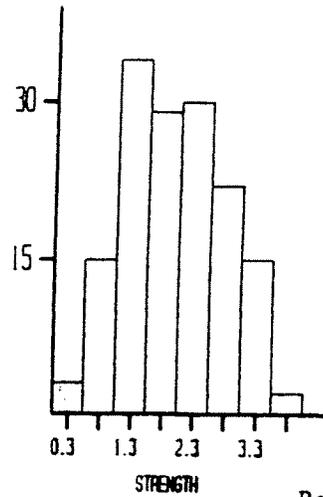


8.

<u>Cell Boundaries</u>	<u>Cell Midpoint</u>	<u>Frequency</u>
1.72-1.76	1.74	5
1.77-1.81	1.79	9
1.82-1.86	1.84	6
1.87-1.91	1.89	27
1.92-1.96	1.94	26
1.97-2.01	1.99	29
2.02-2.06	2.04	13
2.07-2.11	2.09	5
2.12-2.16	2.14	3
2.17-2.21	2.19	1
2.22-2.26	2.24	0
2.27-2.31	2.29	1



9.	Cell Boundaries	Cell Midpoints	Frequency
	0.05-0.54	0.3	3
	0.55-1.04	0.8	15
	1.05-1.54	1.3	34
	1.55-2.04	1.8	29
	2.05-2.54	2.3	30
	2.55-3.04	2.8	22
	3.05-3.54	3.3	15
	3.55-4.04	3.8	2



10.

Scores	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
6	1	1/70 = 0.014	0+1 = 1	1/70 = 0.014
7	1	1/70 = 0.014	1+1 = 2	2/70 = 0.029
8	0	0/70 = 0	2+0 = 2	2/70 = 0.029
9	2	2/70 = 0.029	2+2 = 4	4/70 = 0.057
10	3	3/70 = 0.043	4+3 = 7	7/70 = 0.100
11	2	2/70 = 0.029	7+2 = 9	9/70 = 0.129
12	4	4/70 = 0.057	9+4 = 13	13/70 = 0.186
13	10	10/70 = 0.143	13+10 = 23	23/70 = 0.329
14	11	11/70 = 0.157	23+11 = 34	34/70 = 0.486
15	16	16/70 = 0.229	34+16 = 50	50/70 = 0.714
16	13	13/70 = 0.186	50+13 = 63	63/70 = 0.900
17	3	3/70 = 0.043	63+3 = 66	66/70 = 0.943
18	2	2/70 = 0.029	66+2 = 68	68/70 = 0.971
19	1	1/70 = 0.014	68+1 = 69	69/70 = 0.986
20	1	1/70 = 0.014	69+1 = 70	70/70 = 1.000
	<u>70</u>	<u>1.00</u>		

Graph not shown, but similar to Problem 13

11.

Weights	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
5.94	1	1/110 = 0.9%	0+1 = 1	1/110 = 0.9%
5.95	2	2/110 = 1.8	1+2 = 3	3/110 = 2.7
5.96	4	4/110 = 3.6	3+4 = 7	7/110 = 6.4
5.97	8	8/110 = 7.3	7+8 = 15	15/110 = 13.6
5.98	16	16/110 = 14.5	15+16 = 31	31/110 = 28.2
5.99	24	24/110 = 21.8	31+24 = 55	55/110 = 50.0
6.00	20	20/110 = 18.2	55+20 = 75	75/110 = 68.2
6.01	17	17/110 = 15.5	75+17 = 92	92/110 = 83.6
6.02	13	13/110 = 11.8	92+13 = 105	105/110 = 95.4
6.03	3	3/110 = 2.7	105+3 = 108	108/110 = 98.2
6.04	1	1/110 = 0.9	108+1 = 109	109/110 = 99.1
6.05	1	1/110 = 0.9	109+1 = 110	110/110 = 100.0%
	<u>110</u>	<u>99.9%</u>		

Graph not shown, but similar to Problem 13

12.

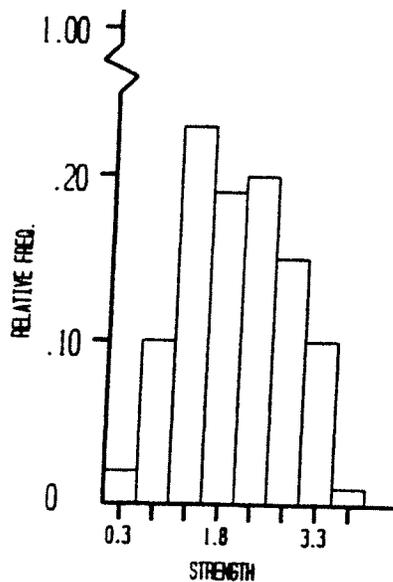
Cell Midpoint	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
1.74	5	$5/125 = 0.040$	$0+5 = 5$	$5/125 = 0.040$
1.79	9	$9/125 = 0.072$	$5+9 = 14$	$14/125 = 0.112$
1.84	6	$6/125 = 0.048$	$14+6 = 20$	$20/125 = 0.160$
1.89	27	$27/125 = 0.216$	$20+27 = 47$	$47/125 = 0.376$
1.94	26	$26/125 = 0.208$	$47+26 = 73$	$73/125 = 0.584$
1.99	29	$29/125 = 0.232$	$73+29 = 102$	$102/125 = 0.816$
2.04	13	$13/125 = 0.104$	$102+13 = 115$	$115/125 = 0.920$
2.09	5	$5/125 = 0.040$	$115+5 = 120$	$120/125 = 0.960$
2.14	3	$3/125 = 0.024$	$120+3 = 123$	$123/125 = 0.984$
2.19	1	$1/125 = 0.008$	$123+1 = 124$	$124/125 = 0.992$
2.24	0	$0/125 = 0$	$124+0 = 124$	$124/125 = 0.992$
2.29	1	$1/125 = 0.008$	$124+1 = 125$	$125/125 = 1.000$
	<u>125</u>	<u>1.000</u>		

Graph not shown, but similar to Problem 13

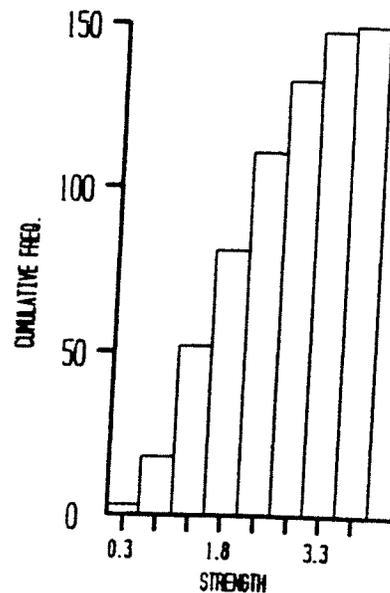
13.

Cell Midpoint	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
0.3	3	$3/150 = 0.020$	$0+3 = 3$	$3/150 = 0.020$
0.8	15	$15/150 = 0.100$	$3+15 = 18$	$18/150 = 0.120$
1.3	34	$34/150 = 0.227$	$18+34 = 52$	$52/150 = 0.347$
1.8	29	$29/150 = 0.193$	$52+29 = 81$	$81/150 = 0.540$
2.3	30	$30/150 = 0.200$	$81+30 = 111$	$111/150 = 0.740$
2.8	22	$22/150 = 0.147$	$111+22 = 133$	$133/150 = 0.888$
3.3	15	$15/150 = 0.100$	$133+15 = 148$	$148/150 = 0.987$
3.8	2	$2/150 = 0.013$	$148+2 = 150$	$150/150 = 1.000$
	<u>150</u>	<u>1.000</u>		

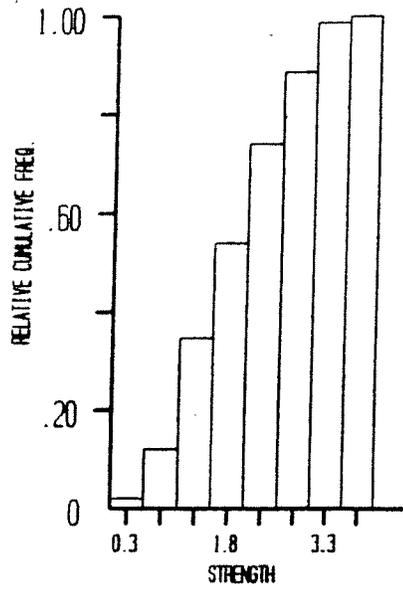
13a



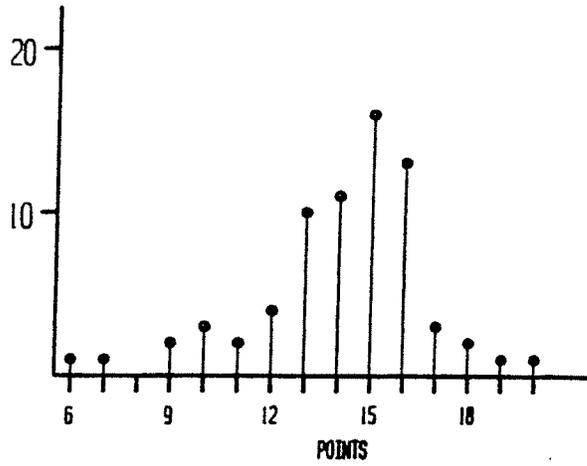
13b



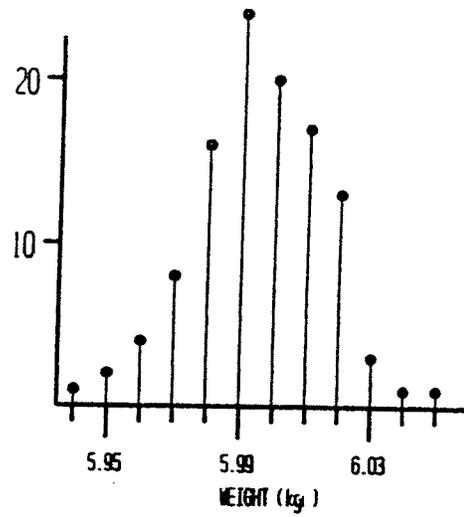
13c



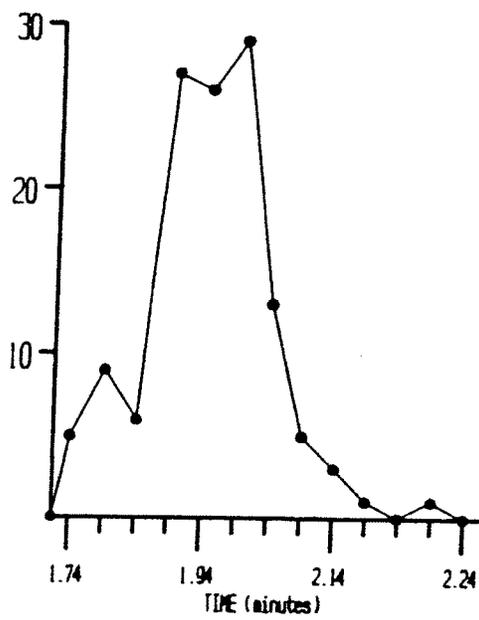
14a



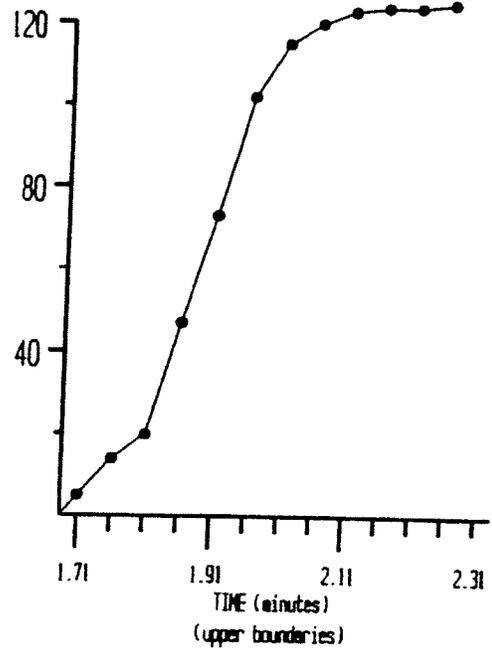
14b



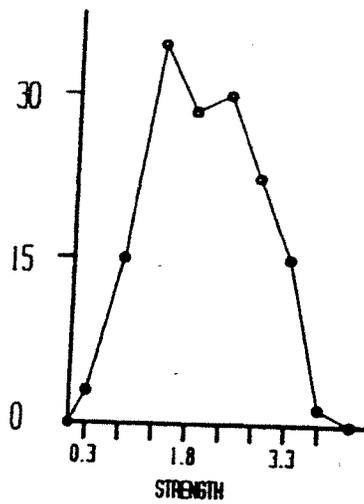
15a



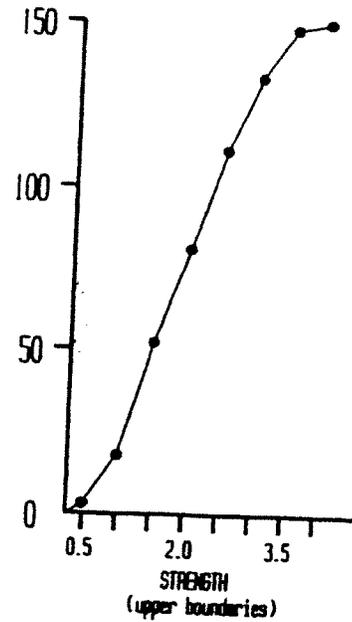
15b



16a



16b



$$17. \bar{X} = \Sigma x/n = \frac{115 + 113 + 121 + 115 + 116}{5} = 116 \text{ volts}$$

$$18. \bar{X} = \frac{\Sigma x}{n} = \frac{25.6 + 24.8 + 22.6 + 21.3 + 19.6 + 18.5 + 16.2 + 15.5}{8} = 20.5 \text{ m}$$

x	f	fx
148	2	296
139	3	417
130	8	1,040
121	11	1,331
112	27	3,024
103	35	3,605
94	43	4,042
85	33	2,805
76	20	1,520
67	12	804
58	6	348
49	4	196
40	2	80
	<u>206</u>	<u>19,508</u>

$$\bar{X} = \frac{\Sigma fx}{n}$$

$$= \frac{19,508}{206}$$

$$= 95 \text{ db}$$

x	f	fx
3.5	6	21.0
3.8	9	34.2
4.1	18	73.8
4.4	14	61.6
4.7	13	61.1
5.0	5	25.0
	<u>65</u>	<u>276.7</u>

$$\bar{X} = \frac{\Sigma fx}{n}$$

$$= \frac{276.7}{65}$$

$$= 4.3 \text{ kg}$$

$$21. \bar{X}_w = \frac{\Sigma w\bar{X}}{\Sigma w}$$

$$= \frac{(3)(3320) + (2)(3180)}{3 + 2}$$

$$= 3264 \text{ h}$$

$$22. \bar{x}_w = \Sigma w\bar{x} / \Sigma w$$

$$= \frac{(24)(1.75) + (18)(1.79) + (29)(1.68)}{24 + 18 + 29}$$

$$= 1.73 \text{ m}$$

$$23. \text{ a. } 8, 11, 15, 18, 22; \text{ Md} = 15$$

$$\text{ b. } 28, 33, 35, 36, 38, 43; \text{ Md} = \frac{35 + 36}{2} = 35.5$$

$$24. \text{ a. } \text{Md} = L + \left(\frac{\frac{n}{2} - cf}{f} \right) i = 1.915 + \left(\frac{\frac{125}{2} - 47}{26} \right) 0.05 = 1.94$$

$$\text{ b. } \text{Md} = 1.55 + \left(\frac{\frac{150}{2} - 52}{29} \right) 0.5 = 1.95$$

$$\text{ c. } \text{Md} = 90 + \left(\frac{\frac{206}{2} - 77}{43} \right) 9 = 95 \text{ db}$$

$$\text{ d. } \text{Md} = 4.0 + \left(\frac{\frac{65}{2} - 15}{18} \right) .3 = 4.3$$

$$\text{ e. } \text{Md} = 1.60 + \left(\frac{\frac{88}{2} - 39}{12} \right) 0.3 = 1.73$$

$$\text{ f. } \text{Md} = 1450 + \left(\frac{\frac{77}{2} - 19}{22} \right) 300 = 1716$$

$$25. 55, \text{ none, } 14 \text{ and } 17$$

$$26. 15, 5.99, 1.99, 1.3, 94, 4.1$$

$$27. \text{ a. } R = H - L = 25 - 14 = 11$$

$$\text{ b. } R = 45 - 39 = 6$$

$$\text{ c. } R = H - L = 20 - 6 = 14$$

$$\text{ d. } R = 6.05 - 5.94 = 0.11$$

$$28. s = \sqrt{\frac{n\Sigma x^2 - (\Sigma x)^2}{n(n-1)}} = \sqrt{\frac{5(7152350) - (5980)^2}{5(5-1)}} = 8.2 \text{ vib/sec}$$

$$29. s = \sqrt{\frac{4(0.024) - (.308)^2}{4(4-1)}} = 0.004 \text{ mm}$$

30.

Mid-point	Freq.		
(x)	(f)	(fx)	(fx ²)
.5	1	.5	0.3
.8	16	12.8	10.2
1.1	12	13.2	14.5
1.4	10	14.0	19.6
1.7	12	20.4	34.7
2.0	18	36.0	72.0
2.3	16	36.8	84.6
2.6	3	7.8	20.3
	<u>88</u>	<u>141.5</u>	<u>256.2</u>

$$s = \sqrt{\frac{n \sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{88(256.2) - (141.5)^2}{88(88-1)}}$$

$$= .57\%$$

31a.

Mid-point	Freq.		
(x)	(f)	(fx)	(fx ²)
0.3	3	0.9	0.27
0.8	15	12.0	9.60
1.3	34	44.2	57.46
1.8	29	52.2	93.96
2.3	30	69.0	158.70
2.8	22	61.6	172.48
3.3	15	49.5	163.35
3.8	2	7.6	28.88
	<u>150</u>	<u>297.0</u>	<u>684.70</u>

$$s = \sqrt{\frac{n \sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{150(684.7) - (297.0)^2}{150(150-1)}}$$

$$= 0.8$$

31b

Mid-point	Freq.		
(x)	(f)	(fx)	(fx ²)
148	2	296	43,808
139	3	417	57,963
130	8	1,040	135,200
121	11	1,331	161,051
112	27	3,024	338,688
103	35	3,605	371,315
94	43	4,042	379,948
85	33	2,805	238,425
76	20	1,520	115,520
67	12	804	53,868
58	6	348	20,184
49	4	196	9,604
40	2	80	3,200
	<u>206</u>	<u>19,508</u>	<u>1,928,774</u>

$$s = \sqrt{\frac{n \sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{206(1,928,774) - (19,508)^2}{206(206-1)}}$$

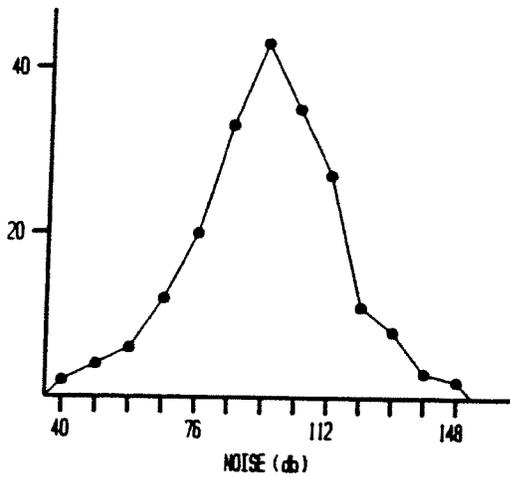
$$= 20 \text{ db}$$

Mid-point (\bar{x})	Freq. (f)	($f\bar{x}$)	($f\bar{x}^2$)
1000	6	6000	6.00×10^6
1300	13	16900	21.97×10^6
1600	22	35200	56.32×10^6
1900	17	32300	61.37×10^6
2200	11	24200	53.24×10^6
2500	8	20000	50.00×10^6
	<u>77</u>	<u>134.6×10^3</u>	<u>248.9×10^6</u>

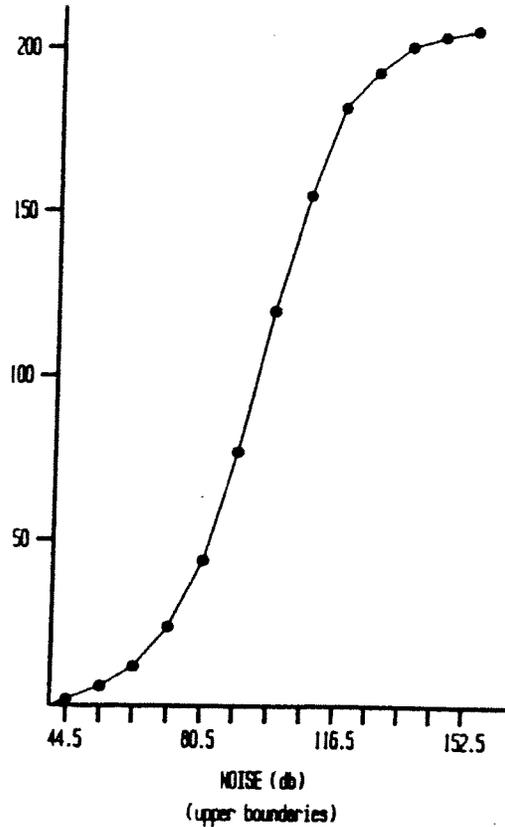
$$\bar{x} = \Sigma f\bar{x} / n = 134.6 \times 10^3 / 77 = 1748 \text{ inspections}$$

$$s = \sqrt{\frac{n \Sigma f\bar{x}^2 - (\Sigma f\bar{x})^2}{n(n-1)}} = \sqrt{\frac{77(248.9 \times 10^6) - (134.6 \times 10^3)^2}{77(77-1)}} = 423$$

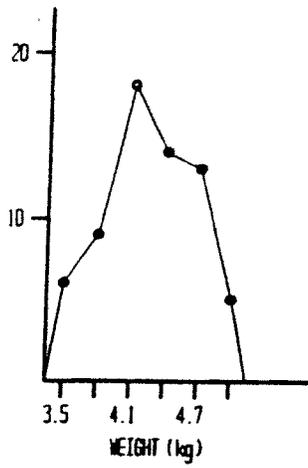
33a



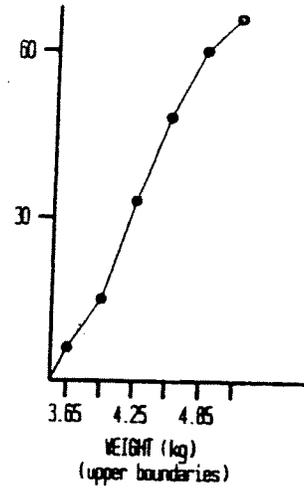
33b



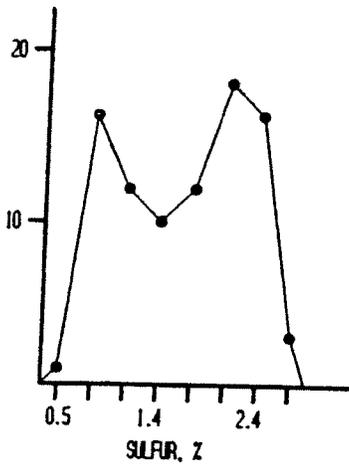
34a



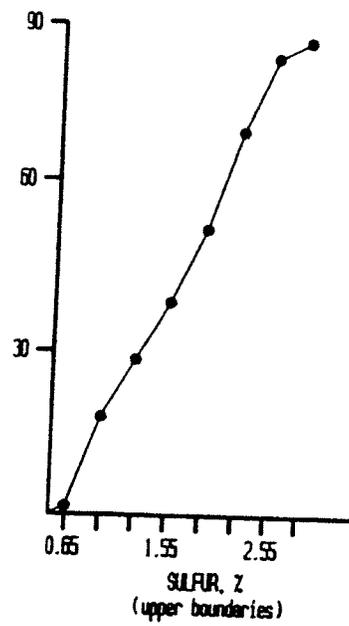
34b



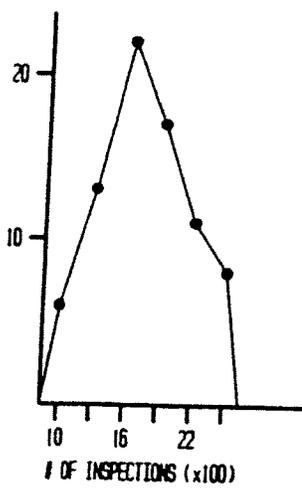
35a



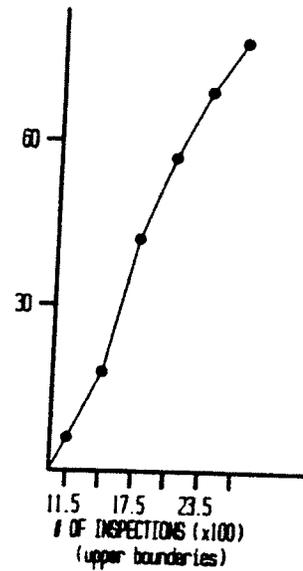
35b



36a



36b



Cell Mid- point	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
40	2	$2/206 = 0.010$	$0+2 = 2$	$2/206 = 0.010$
49	4	$4/206 = 0.019$	$2+4 = 6$	$6/206 = 0.029$
58	6	$6/206 = 0.029$	$6+6 = 12$	$12/206 = 0.058$
67	12	$12/206 = 0.058$	$12+12 = 24$	$24/206 = 0.117$
76	20	$20/206 = 0.097$	$24+20 = 44$	$44/206 = 0.214$
85	33	$33/206 = 0.160$	$44+33 = 77$	$77/206 = 0.374$
94	43	$43/206 = 0.209$	$77+43 = 120$	$120/206 = 0.583$
103	35	$35/206 = 0.170$	$120+35 = 155$	$155/206 = 0.752$
112	27	$27/206 = 0.131$	$155+27 = 182$	$182/206 = 0.883$
121	11	$11/206 = 0.053$	$182+11 = 193$	$193/206 = 0.937$
130	8	$8/206 = 0.039$	$193+8 = 201$	$201/206 = 0.976$
139	3	$3/206 = 0.015$	$201+3 = 204$	$204/206 = 0.990$
148	2	$2/206 = 0.010$	$204+2 = 206$	$206/206 = 1.000$
	<u>206</u>	<u>1.000</u>		

Cell Mid- point	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
3.5	6	$6/65 = 0.092$	$0+6 = 6$	$6/65 = 0.092$
3.8	9	$9/65 = 0.138$	$6+9 = 15$	$15/65 = 0.231$
4.1	18	$18/65 = 0.277$	$15+18 = 33$	$33/65 = 0.508$
4.4	14	$14/65 = 0.215$	$33+14 = 47$	$47/65 = 0.723$
4.7	13	$13/65 = 0.200$	$47+13 = 60$	$60/65 = 0.923$
5.0	5	$5/65 = 0.077$	$60+5 = 65$	$65/65 = 1.000$
	<u>65</u>	<u>0.999</u>		

Cell Mid- point	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
0.5	1	$1/88 = 0.011$	$0+1 = 1$	$1/88 = 0.010$
0.8	16	$16/88 = 0.182$	$1+16 = 17$	$17/88 = 0.156$
1.1	12	$12/88 = 0.136$	$17+12 = 29$	$29/88 = 0.330$
1.4	10	$10/88 = 0.114$	$29+10 = 39$	$39/88 = 0.443$
1.7	12	$12/88 = 0.136$	$39+12 = 51$	$51/88 = 0.580$
2.0	18	$18/88 = 0.205$	$51+18 = 69$	$69/88 = 0.784$
2.3	16	$16/88 = 0.182$	$69+16 = 85$	$85/88 = 0.966$
2.6	3	$3/88 = 0.034$	$85+3 = 88$	$88/88 = 1.000$
	<u>88</u>	<u>1.000</u>		

Cell Mid- point	Freq.	Relative Freq.	Cumulative Freq.	Relative Cumulative Freq.
1000	6	$6/77 = 0.078$	$0+6 = 6$	$6/77 = 0.078$
1300	13	$13/77 = 0.169$	$6+13 = 19$	$19/77 = 0.247$
1600	22	$22/77 = 0.286$	$19+22 = 41$	$41/77 = 0.532$
1900	17	$17/77 = 0.221$	$41+17 = 58$	$58/77 = 0.753$
2200	11	$11/77 = 0.143$	$58+11 = 69$	$69/77 = 0.896$
2500	8	$8/77 = 0.104$	$69+8 = 77$	$77/77 = 1.000$
	<u>77</u>	<u>1.001</u>		

41a	X	f	$(X_i - \bar{X})$	$f(X_i - \bar{X})^3$	$f(X_i - \bar{X})^4$
	6	1	-8.13	-537.37	4,368.80
	7	1	-7.13	-362.47	2,584.39
	8	0	-6.13	0	0
	9	2	-5.13	-270.01	1,385.16
	10	3	-4.13	-211.33	872.81
	11	2	-3.13	- 61.33	191.96
	12	4	-2.13	- 38.65	82.33
	13	10	-1.13	- 14.43	16.30
	14	11	-0.13	- 0.02	0
	15	16	0.87	10.54	9.17
	16	13	1.87	85.01	158.97
	17	3	2.87	70.92	203.54
	18	2	3.87	115.92	448.62
	19	1	4.87	115.50	562.49
	20	1	5.87	202.26	1,187.28
		<u>70</u>		<u>-895.46</u>	<u>12,071.82</u>

$$\bar{X} = 14.13 \quad s = 2.53$$

$$a_3 = \frac{\Sigma f(X_i - \bar{X})^3/n}{s^3} = \frac{-895.46/70}{2.53^3} = -0.79$$

$$a_4 = \frac{\Sigma f(X_i - \bar{X})^4/n}{s^4} = \frac{12071.82/70}{2.53^4} = 4.21$$

Distribution is very peaked and quite skewed to the left.

41b.	X	f	$(X_i - \bar{X})$	$f(X_i - \bar{X})^3$	$f(X_i - \bar{X})^4$
	-6	1	-5.54	-170.03	941.97
	-5	2	-4.54	-187.15	849.68
	-4	4	-3.54	-177.45	628.16
	-3	8	-2.54	-131.10	332.99
	-2	16	-1.54	- 58.44	89.99
	-1	24	-0.54	- 3.78	2.04
	0	20	.46	1.95	.90
	1	17	1.46	40.45	59.06
	2	13	2.46	193.53	476.08
	3	3	3.46	124.26	429.96
	4	1	4.46	88.72	395.68
	5	1	5.46	162.77	888.73
		<u>110</u>		<u>-116.27</u>	<u>5,171.72</u>

Note: X is coded from 6.00.

$$\bar{X} = -0.46 \quad \text{True } \bar{X} = 5.9954 \quad s = 1.97$$

$$a_3 = \frac{\Sigma f(X_i - \bar{X})^3/n}{s^3} = \frac{-116.27/110}{1.97^3} = -0.14$$

$$a_4 = \frac{\Sigma f(X_i - \bar{X})^4/n}{s^4} = \frac{5171.72/110}{1.97^4} = 3.11$$

Distribution is slightly skewed to the left and not quite as peaked as normal.

41c	X	f	$(X_i - \bar{X})$	$\frac{f(X_i - \bar{X})^3}{10^3}$	$\frac{f(X_i - \bar{X})^4}{10^3}$
	1.74	5	-.2032	-41.9509	8.5244
	1.79	9	-.1532	-32.3608	4.9577
	1.84	6	-.1032	- 6.5946	.6806
	1.89	27	-.0532	- 4.0654	.2163
	1.94	26	-.0032	- .0009	nil
	1.99	29	.0468	2.9726	.1391
	2.04	13	.0968	11.7915	1.1414
	2.09	5	.1468	15.8179	2.3221
	2.14	3	.1968	12.8663	4.5001
	2.19	1	.2468	15.0326	3.7101
	2.24	0	.2968	0	0
	2.29	1	.3468	41.7097	14.4649
		<u>125</u>		<u>+25.218 x 10³</u>	<u>40.6567 x 10³</u>

$$\bar{X} = 1.9432$$

$$s = .096249$$

$$a_3 = \frac{\sum f(X_i - \bar{X})^3/n}{s^3} = \frac{25.218 \times 10^3/125}{.096249^3} = +0.23$$

$$a_4 = \frac{\sum f(X_i - \bar{X})^4/n}{s^4} = \frac{40.6567 \times 10^3/125}{.096249^4} = 3.79$$

Distribution is slightly skewed to the right and somewhat peaked.

41d.	X	f	$(X_i - \bar{X})$	$\frac{f(X_i - \bar{X})^3}{10^3}$	$\frac{f(X_i - \bar{X})^4}{10^3}$
	0.3	3	-1.68	-14.2249	23.8978
	0.8	15	-1.18	-24.6455	29.0816
	1.3	34	-0.68	-10.6907	7.2697
	1.8	29	-0.18	- .1691	.0304
	2.3	30	.32	.9830	.3146
	2.8	22	.82	12.1301	9.9467
	3.3	15	1.32	34.4995	45.5394
	3.8	2	1.82	12.0571	21.9439
		<u>150</u>		<u>9.9395</u>	<u>138.0242</u>

$$\bar{X} = 1.98$$

$$s = 0.8053512$$

$$a_3 = \frac{\sum f(X_i - \bar{X})^3/n}{s^3} = \frac{9.9395/150}{.8053512^3} = +.13$$

$$a_4 = \frac{\sum f(X_i - \bar{X})^4/n}{s^4} = \frac{138.0242/150}{.8053512^4} = 2.19$$

Slightly skewed to the right and flatter than normal.

41e	X	f	$(X_i - \bar{X})$	$f(X_i - \bar{X})^3$	$f(X_i - \bar{X})^4$
	3.5	6	-0.7569	-2.6018	1.96927
	3.8	9	-0.4569	-.8584	.3922
	4.1	18	-0.1569	-.0695	.0109
	4.4	14	0.1431	.0410	.0059
	4.7	13	0.4431	1.1310	.5011
	5.0	5	0.7431	2.0517	1.5246
		65		-0.306	4.4040

$$\bar{X} = 4.2569$$

$$s = 0.4212961$$

$$a_3 = \frac{\sum f(X_i - \bar{X})^3/n}{s^3} = \frac{-0.306/65}{0.4212961^3} = -0.06$$

$$a_4 = \frac{\sum f(X_i - \bar{X})^4/n}{s^4} = \frac{4.4040/65}{0.4212961^4} = 2.15$$

Distribution is essentially symmetrical and much flatter than normal.

41f	X	f	$(X_i - \bar{X})$	$f(X_i - \bar{X})^3 \times 10^6$	$f(X_i - \bar{X})^4 \times 10^9$
	1000	6	-748	-2511	1878
	1300	13	-448	-1169	523
	1600	22	-148	-71	11
	1900	17	+152	60	9
	2200	11	+452	1015	459
	2500	8	+752	3402	2558
		77		+ 726 x 10 ⁶	5438 x 10 ⁹

$$\bar{X} = 1748$$

$$s = 423$$

$$a_3 = \frac{\sum f(X_i - \bar{X})^3/n}{s^3} = \frac{726 \times 10^6/77}{423^3} = +0.10$$

$$a_4 = \frac{\sum f(X_i - \bar{X})^4/n}{s^4} = \frac{5438 \times 10^9/77}{423^4} = 2.21$$

Distribution is essentially symmetrical and much flatter than normal.

42. Max. of 134.5 db (x_i)

from 17 $\bar{X} = 94.7$

$\sigma = 19.925$

$$z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{134.5 - 94.7}{19.925}$$

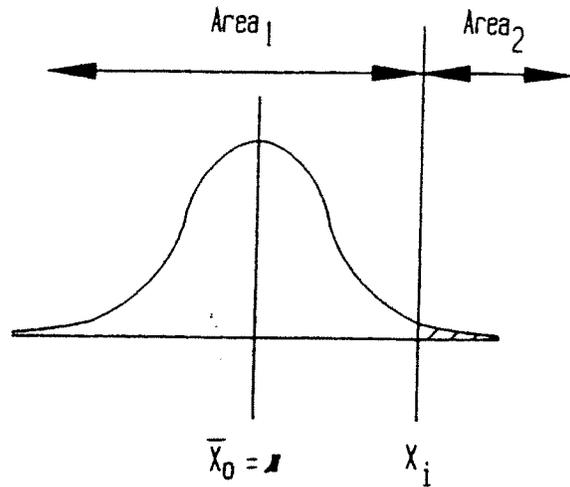
$$z_1 = 2.00$$

$$\text{Area}_1 = 0.9773$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.00 - 0.9773$$

$$\text{Area}_2 = 0.0227 \text{ or } 2.8\%$$



43. Min. of 3.65 (x_i)

Max. of 4.85 (x_i)

from 18 $\bar{X} = 4.25$

$\sigma = .4213$

$$z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{3.65 - 4.26}{.4213}$$

$$z_1 = -1.45$$

$$\text{Area}_1 = 0.0734$$

$$z_2 = \frac{x_i - \mu}{\sigma}$$

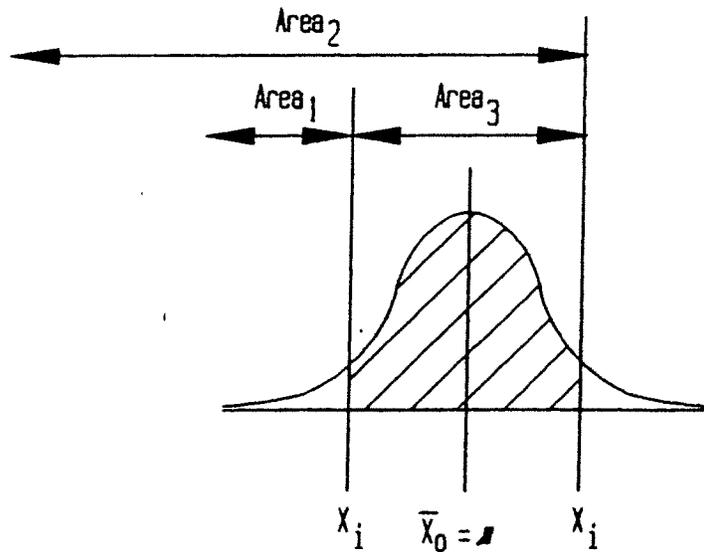
$$z_2 = \frac{4.85 - 4.26}{.4213}$$

$$z_2 = 1.40 \quad \text{Area}_2 = 0.9192$$

$$\text{Area}_3 = \text{Area}_2 - \text{Area}_1$$

$$\text{Area}_3 = 0.9192 - 0.0735$$

$$\text{Area}_3 = 0.8457 \text{ or } 84.6\%$$



44. Max. of 2.25 (X_1)

From 28 $\bar{X} = 1.65$

$\sigma = 0.617$

$$z_1 = \frac{X_1 - \mu}{\sigma}$$

$$z_1 = \frac{2.25 - 1.65}{0.617}$$

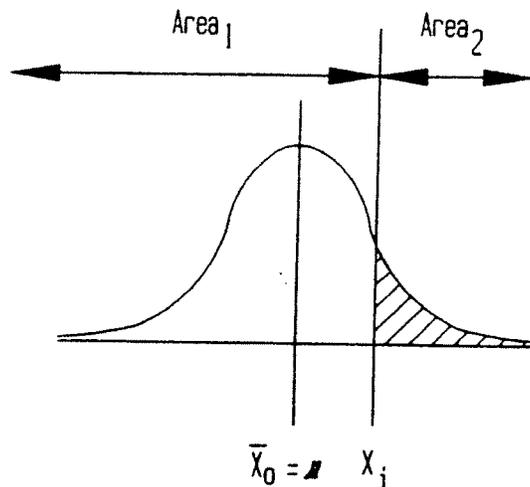
$$z_1 = 0.97$$

$$\text{Area}_1 = 0.8340$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.8340$$

$$\text{Area}_2 = 0.166 \text{ or } 16.6\%$$



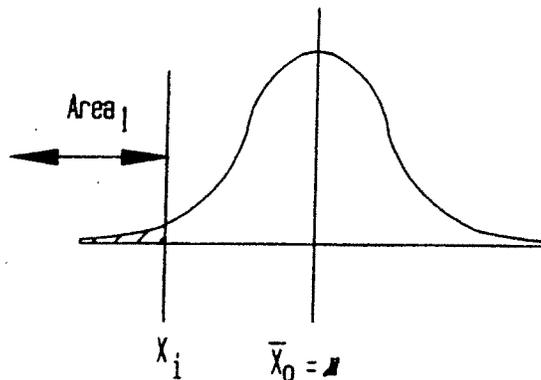
45a $z = \frac{X_1 - \mu}{\sigma}$

$$z = \frac{8.30 - 9.07}{0.40}$$

$$z = -1.93 \text{ Rounded}$$

From Table A₁

$$\text{Area}_1 = 0.0268 \text{ or } 2.68\%$$



45b $z_1 = \frac{X_1 - \mu}{\sigma}$

$$z_1 = \frac{10.00 - 9.07}{0.40}$$

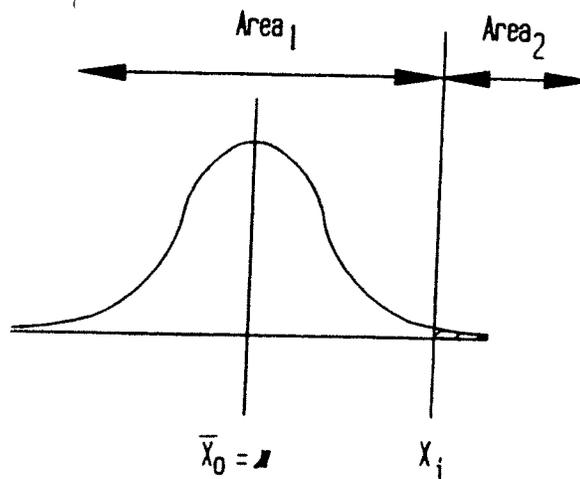
$$z_1 = +2.33 \text{ Rounded}$$

$$\text{Area}_1 = 0.9901$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.9901$$

$$\text{Area}_2 = 0.0099 \text{ or } 0.99\%$$



45c $z_1 = \frac{X_i - \mu}{\sigma}$

$$z_1 = \frac{8.00 - 9.07}{0.40}$$

$$z_1 = -2.68$$

$$\text{Area}_1 = 0.0037$$

$$z_2 = \frac{X_i - \mu}{\sigma}$$

$$z_2 = \frac{10.10 - 9.07}{0.40}$$

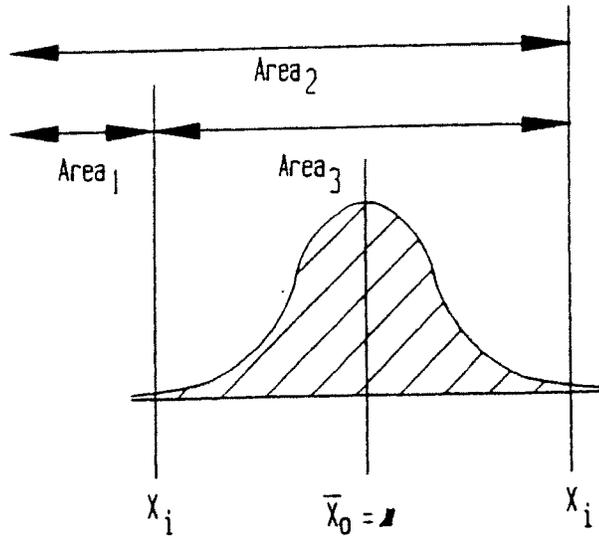
$$z_2 = +2.58$$

$$\text{Area}_2 = 0.9951$$

$$\text{Area}_3 = \text{Area}_2 - \text{Area}_1$$

$$\text{Area}_3 = 0.9951 - 0.0037$$

$$\text{Area}_3 = 0.9914 \text{ or } 99.14\%$$

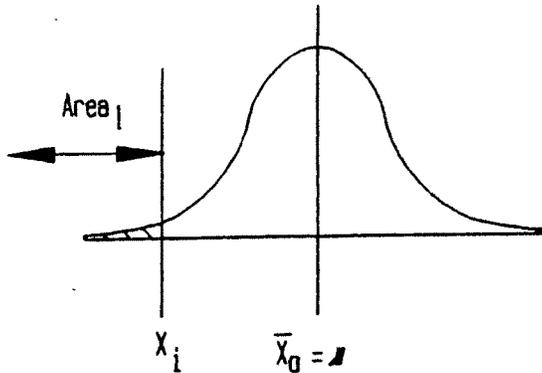


46a. $z_1 = \frac{X_i - \mu}{\sigma}$

$$z_1 = \frac{13 - 16}{1.5}$$

$$z_1 = -2.00$$

$$\text{Area}_1 = 0.0228 \text{ or } 2.28\%$$



46b. $z_1 = \frac{X_i - \mu}{\sigma}$

$$z_1 = \frac{20 - 16}{1.5}$$

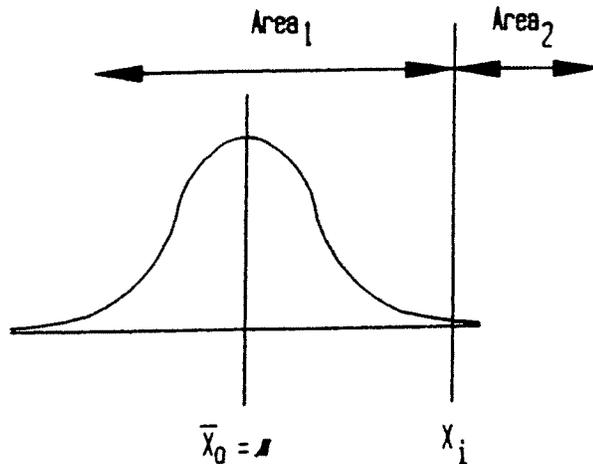
$$z_1 = +2.67$$

$$\text{Area}_1 = 0.9962$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.9962$$

$$\text{Area}_2 = 0.0038 \text{ or } 0.38\%$$



46c $Area_1 = 0.0228$

$$z_2 = \frac{X_i - \mu}{\sigma}$$

$$z_2 = \frac{20.5 - 16}{1.5}$$

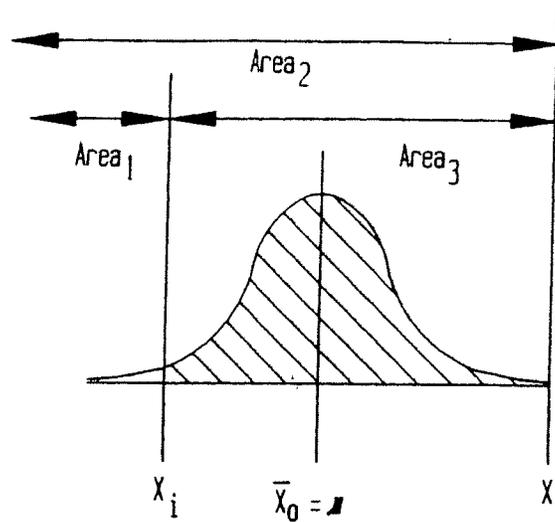
$$z_2 = +3.00$$

$$Area_2 = 0.99865$$

$$Area_3 = Area_2 - Area_1$$

$$Area_3 = 0.99865 - 0.0228$$

$$Area_3 = 0.9759 \text{ or } 97.59\%$$



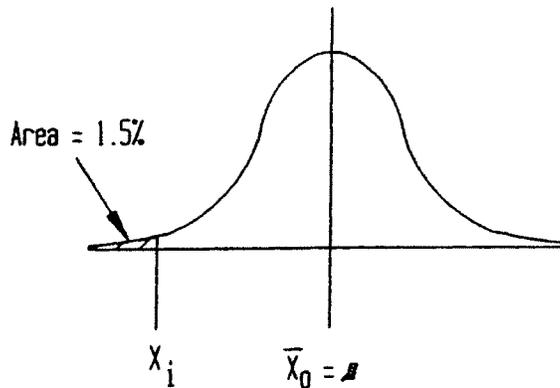
47. From Table A

For 1.5%, $z_1 = -2.17$

$$z_1 = \frac{X_i - \mu}{\sigma}$$

$$-2.17 = \frac{0.567 - \bar{X}_0}{0.018}$$

$$\bar{X}_0 = .606 \text{ g}$$

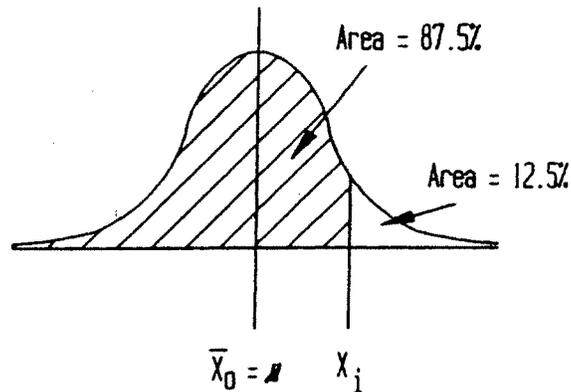


48. If rework % is 12.5%, Area to the left is 87.5% and has a Z value of +1.15.

$$z_1 = \frac{X_i - \mu}{\sigma}$$

$$1.15 = \frac{25.38 - \bar{X}_0}{0.01}$$

$$\bar{X}_0 = 25.37 \text{ mm}$$



49a Not normal

49b Normal

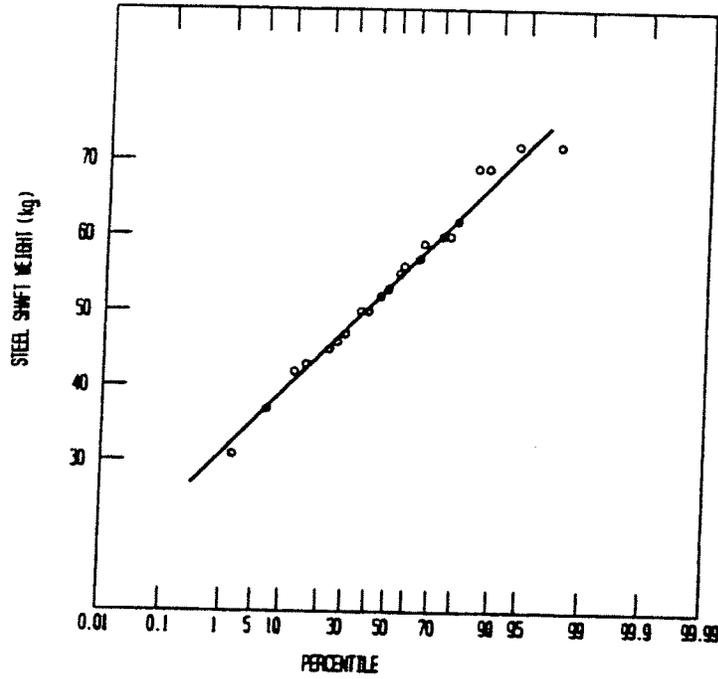
49c Not normal

49d Not normal, but symmetrical

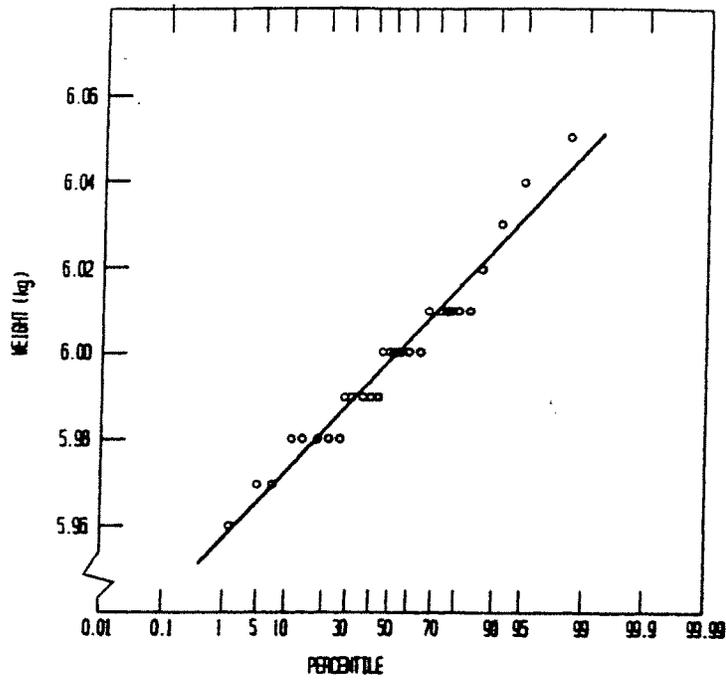
49e Not normal, but symmetrical

49f Not normal, but symmetrical

50a	\bar{X}	i	PP	\bar{X}	i	PP
	31	1	2.3	55	12	52.3
	37	2	6.8	56	13	56.8
	42	3	11.4	57	14	61.4
	43	4	15.9	59	15	65.9
	45	5	20.5	60	16	70.5
	46	6	25.0	60	17	75.0
	47	7	29.5	62	18	79.5
	50	8	34.1	69	19	84.1
	50	9	38.6	69	20	88.6
	52	10	43.2	72	21	93.2
	53	11	47.7	72	22	97.7

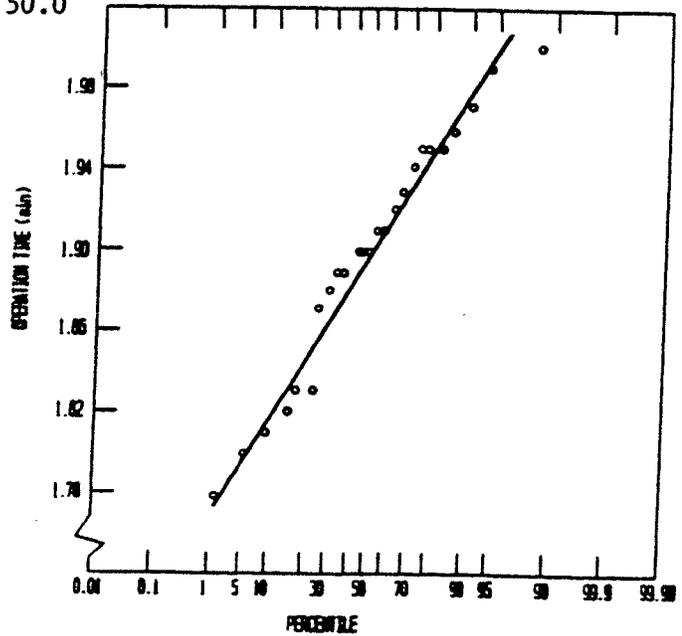


50b	\bar{X}	i	PP	\bar{X}	i	PP
	5.96	1	1.7	6.00	16	51.7
	5.97	2	5.0	6.00	17	55.0
	5.97	3	8.3	6.00	18	58.3
	5.98	4	11.7	6.00	19	61.7
	5.98	5	15.0	6.00	20	65.0
	5.98	6	18.3	6.01	21	68.3
	5.98	7	21.7	6.01	22	71.7
	5.98	8	25.0	6.01	23	75.0
	5.99	9	28.3	6.01	24	78.3
	5.99	10	31.7	6.01	25	81.7
	5.99	11	35.0	6.01	26	85.0
	5.99	12	38.3	6.02	27	88.3
	5.99	13	41.7	6.03	28	91.7
	6.00	14	45.0	6.04	29	95.0
	6.00	15	48.3	6.05	30	98.3

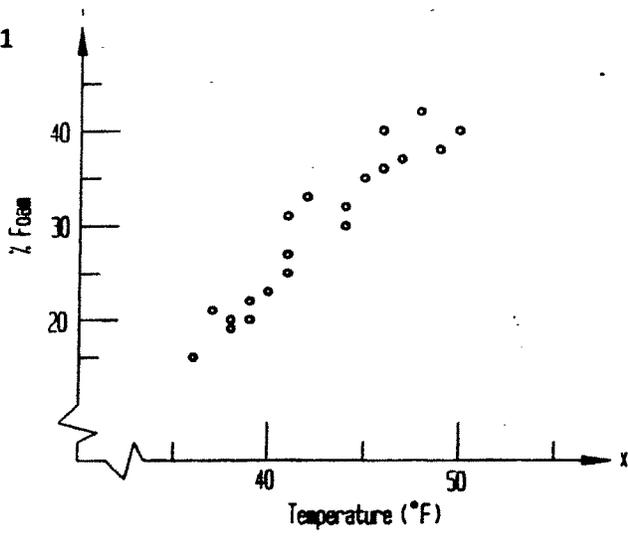


50c

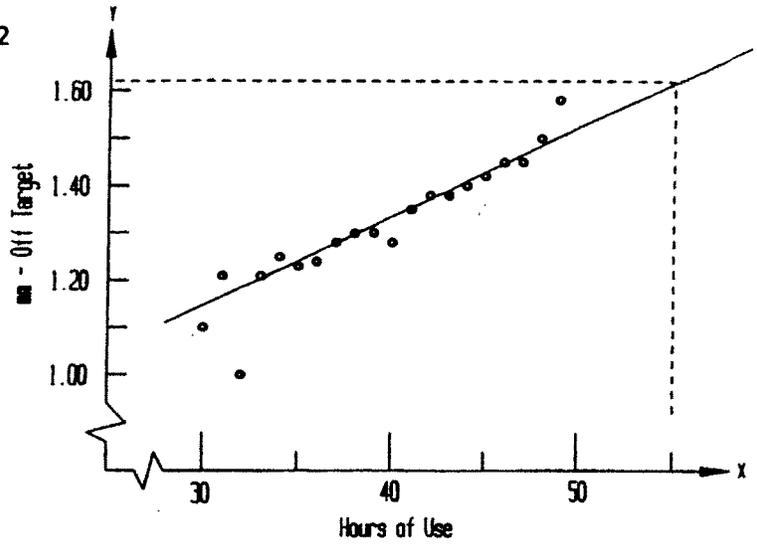
\bar{X}	i	PP	\bar{X}	i	PP
1.78	1	2.0	1.91	14	54.0
1.80	2	6.0	1.91	15	48.0
1.81	3	10.0	1.92	16	62.0
1.82	4	14.0	1.93	17	66.0
1.83	5	18.0	1.94	18	70.0
1.83	6	22.0	1.95	19	74.0
1.87	7	26.0	1.95	20	78.0
1.88	8	30.0	1.95	21	82.0
1.89	9	34.0	1.96	22	86.0
1.89	10	38.0	1.97	23	90.0
1.90	11	42.0	1.99	24	94.0
1.90	12	46.0	2.00	25	98.0
1.90	13	50.0			



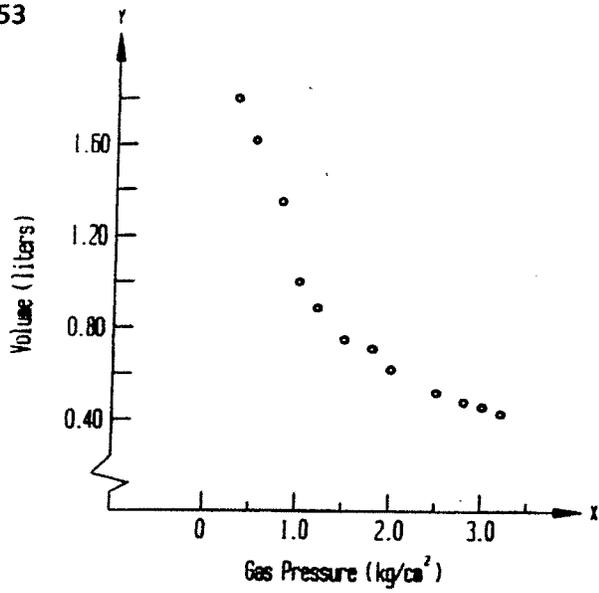
51



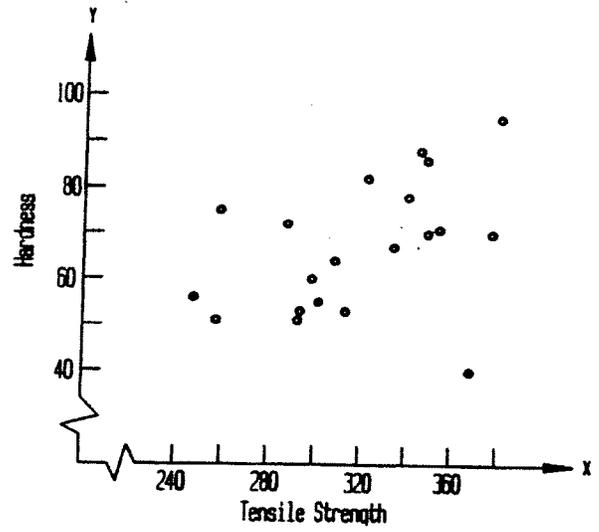
52



53



54



55

