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**Online Instructor's Manual**  
*to accompany*

# Quality Control

**Eighth Edition**

**Dale H. Besterfield Ph.D., P.E.**



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Columbus, Ohio



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## PREFACE

This manual has been published to simplify the instructor's tasks of developing learning activities and evaluating performance. It is based on the experience of the author and is meant to serve as a guide. Each instructor will need to modify this information for the particular course objectives and the ability level of the students.

For those teachers who are familiar with the *Seventh Edition* of the textbook, information on the major changes to the *Eighth Edition* is provided. This information should simplify the transition to the latest edition.

A typical course outline for a three-semester hour course is shown on Page 3. The learning activities are based on 45 class meetings of 50 minutes each. Since it is difficult to cover all of the material in a typical three-semester hour course, this outline concentrates on the quantifiable aspects of quality control. The instructor may wish to place greater emphasis on the first three chapters, which are non-quantifiable and build a transition to the statistical aspects of quality..

Solutions for the problems start on Page 4. The author has found it advantageous to post the solutions. This action allows students to determine if their methods and answer are correct.

Typical multiple-choice test questions are given and an asterisk indicates the correct answer. These questions can be modified in a number of ways depending on the creativity of the instructor. Answers to test problems are also given. Since the tables in the body of the text and in the Appendix are needed to solve the problems, an open-book type examination should be considered. The instructor may also consider providing copies of the tables and using a closed-book format. Regardless, the multiple-choice questions can be given in the closed-book format. The author has found that allowing the students 3x5 cards for formulas and other information is a great learning experience.

## Major Changes to the Eighth Edition

### General

1. Problems to exercises.
2. Objectives added to each chapter.
3. Where appropriated changed product to product or service.
4. Where appropriated changed company to organization
5. Footnotes are provided for more advanced topics.
6. Changed exercise notation to include the chapter such as 1-1, ..., 1-6; 2-1, ..., 2-8, etc.

### Chapter 1

1. Added ASQ definition of quality.
2. Changed slide projector to plasma TV in Table 1-1.
3. Modified Figure 1-1.
4. Added exercises.

### Chapter 2

1. Added Lean to Figure 2-1 along with other modifications.
2. Added time line to annual quality improvement program.
3. Added that performance measures should not be used as a “whip.”
4. Clarified Figure 2-7 with a footnote.
5. Revised Figure 2-8 and Table 2-4

### Chapter 3

1. Moved scatter diagram to Chapter 4

### Chapter 4

1. Changed weekly wage numbers for example on range
2. Added coefficient of variation to other measures
3. Added least squares calculations to scatter diagram.

### Chapter 5

1. Added additional statistical information to six sigma.
2. Added exponential moving average chart with exercises.
3. Added ARL

### Chapter 6

1. Added footnotes as links to recent literature on  $T^2$  multivariate chart and deviation chart.

## Chapter 7

1. Added mean and standard deviation formulas to hypergeometric, binomial, and Poisson distributions.
2. Added exercises 17 and 18 and renumbered the rest.
3. Eliminated examples and exercises concerning approximation techniques because they are obsolete.

## Chapter 8

1. Added information on sample size and confidence limits.

## Chapter 9

1. Changed meaning of AQL

## Chapter 10

1. Latest standards revision.

## Chapter 11

1. Added a section on test design with footnotes to advanced material.

## Chapter 12

1. Added footnotes to information on use of these techniques for innovative design.

## TYPICAL COURSE OUTLINE

| <u>Meeting</u> | <u>Topic</u>                                 | <u>Chapter</u> |
|----------------|--|----------------|
| 1              | Introduction to Quality                      | 1              |
| 2 and 3        | TQM - Principle practices                    | 2              |
| 4              | TQM - Tools & Techniques                     | 3              |
| 5 thru 9       | Fundamentals of Statistics                   | 4              |
| 10 thru 15     | Control Charts for Variables                 | 5              |
| 16             | Examination I                                |                |
| 17 and 18      | Additional SPC Techniques for Variables      | 6              |
| 19 thru 23     | Fundamentals of Probability                  | 7              |
| 24 thru 28     | Control Charts for Attributes                | 8              |
| 29             | Examination II                               |                |
| 30 thru 39     | Lot-by-Lot Acceptance Sampling by Attributes | 9              |
| 40 thru 43     | Acceptance Sampling Plan Systems             | 10             |
| 44             | Reliability (non quantitative)               | 11             |
| 45             | Examination III                              |                |

## Chapter 3. TQM—TOOLS AND TECHNIQUES

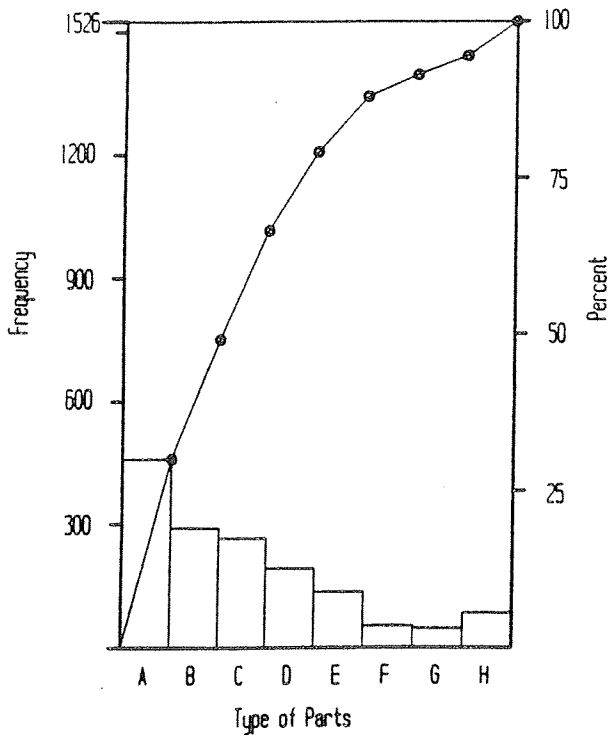
### 1. Replacement Parts: (6-month period)

|                    | <u>Frequency</u> | <u>Percent</u> | <u>Cumulative<br/>Frequency</u> | <u>Cumulative<br/>Percent</u> |
|--------------------|------------------|----------------|---------------------------------|-------------------------------|
| A. front burners   | 460              | .30            | 460                             | .30                           |
| B. rear burners    | 290              | .19            | 750                             | .49                           |
| C. oven regulators | 265              | .17            | 1015                            | .66                           |
| D. oven door       | 193              | .13            | 1208                            | .79                           |
| E. burner control  | 135              | .09            | 1343                            | .88                           |
| F. timer           | 53               | .03            | 1396                            | .91                           |
| G. drawer rollers  | 46               | .03            | 1442                            | .94                           |
| H. All others      | <u>84</u>        | <u>.06</u>     | 1526                            | 1.00                          |
|                    | 1526             | 1.00           |                                 |                               |

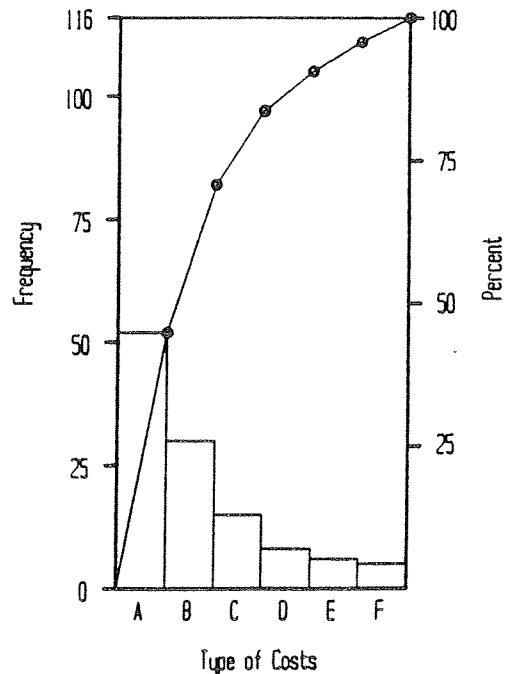
### 2. Downtime Costs: (3-month period) in thousands of dollars

|                       | <u>Frequency</u> | <u>Percent</u> | <u>Cumulative<br/>Frequency</u> | <u>Cumulative<br/>Percent</u> |
|-----------------------|------------------|----------------|---------------------------------|-------------------------------|
| A. lost cooling       | 52               | .45            | 52                              | .45                           |
| B. back pressure reg. | 30               | .26            | 82                              | .71                           |
| C. adjust feed worm   | 15               | .13            | 97                              | .84                           |
| D. valve replacement  | 8                | .07            | 105                             | .91                           |
| E. jam copperhead     | 6                | .05            | 111                             | .96                           |
| F. All others         | <u>5</u>         | <u>.04</u>     | 116                             | 1.00                          |
|                       | 116              | 1.00           |                                 |                               |

(1)



(2)



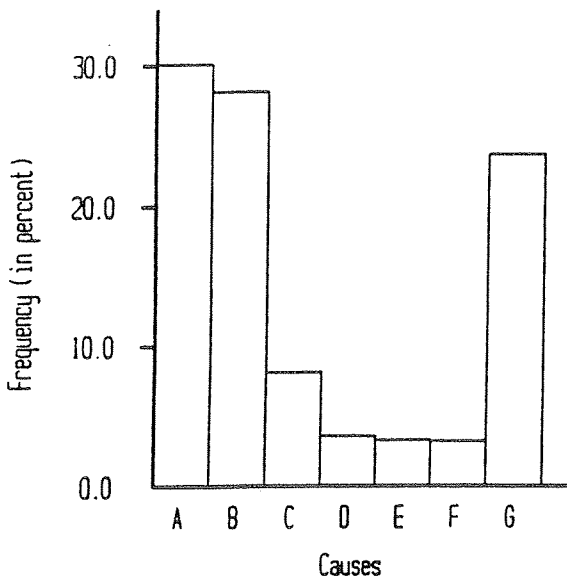


|   |                                   |             |
|---|-----------------------------------|-------------|
| 3 | Cause of accident                 | in percent  |
|   | a. right-of-way violation         | 30.1        |
|   | b. driving too fast for condition | 28.1        |
|   | c. following too closely          | 8.1         |
|   | d. improper turn                  | 3.6         |
|   | e. driving left of center         | 3.3         |
|   | f. improper overtaking            | 3.2         |
|   | g. all other                      | <u>23.6</u> |
|   |                                   | 100.0       |

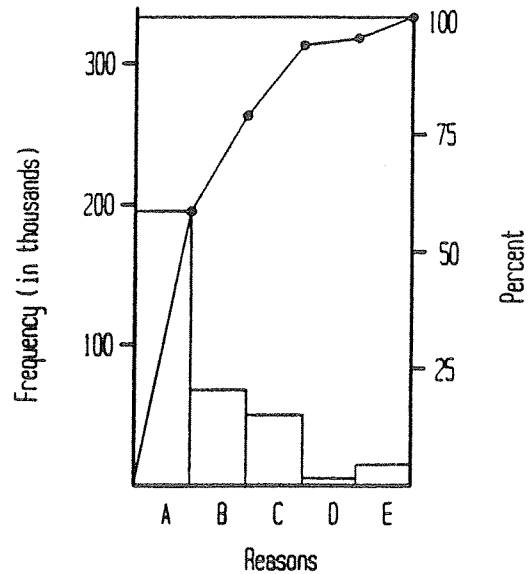
4. Reason for Shipment Return: (quarter)  
in thousands

|                    | <u>Frequency</u> | <u>Percent</u> | <u>Cumulative<br/>Frequency</u> | <u>Cumulative<br/>Percent</u> |
|--------------------|------------------|----------------|---------------------------------|-------------------------------|
| A. refused         | 195              | .585           | 195                             | .59                           |
| B. wrong address   | 68               | .20            | 263                             | .79                           |
| C. wrong selection | 50               | .15            | 313                             | .94                           |
| D. order canceled  | 5                | .02            | 318                             | .96                           |
| E. All other       | <u>15</u>        | <u>.045</u>    | 333                             | 1.00                          |
|                    | 333              | 1.00           |                                 |                               |

(3)

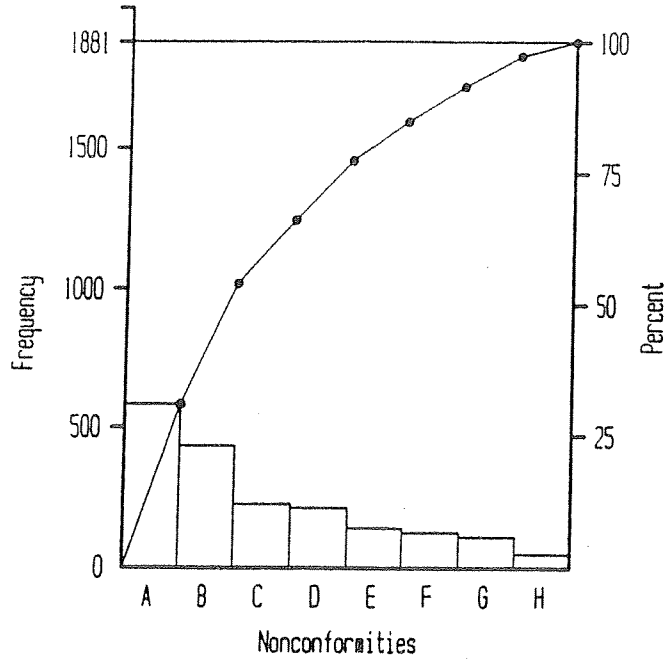


(4)

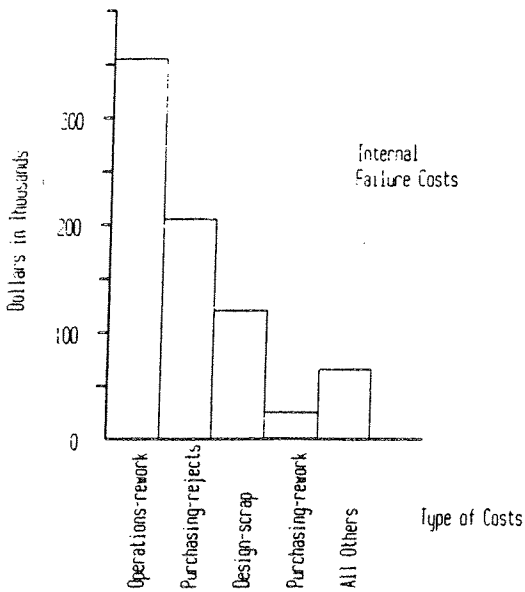


5. Paint Nonconformities: (1-month)

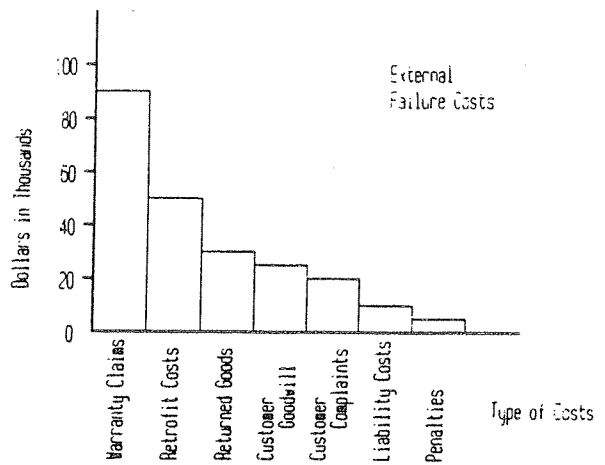
|                | <u>Frequency</u> | <u>Percent</u> | <u>Cumulative Frequency</u> | <u>Cumulative Percent</u> |
|----------------|------------------|----------------|-----------------------------|---------------------------|
| A. light spray | 582              | .31            | 582                         | .31                       |
| B. runs        | 434              | .23            | 1016                        | .54                       |
| C. drips       | 227              | .12            | 1243                        | .66                       |
| D. blisters    | 212              | .11            | 1455                        | .77                       |
| E. splatter    | 141              | .07            | 1596                        | .84                       |
| F. bad paint   | 126              | .07            | 1722                        | .91                       |
| G. overspray   | 109              | .06            | 1831                        | .97                       |
| H. All others  | 50               | .03            | 1881                        | 1.00                      |
|                | <u>1881</u>      | <u>1.00</u>    |                             |                           |



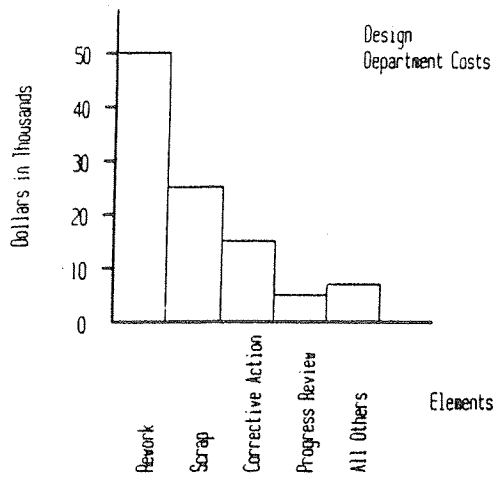
6.



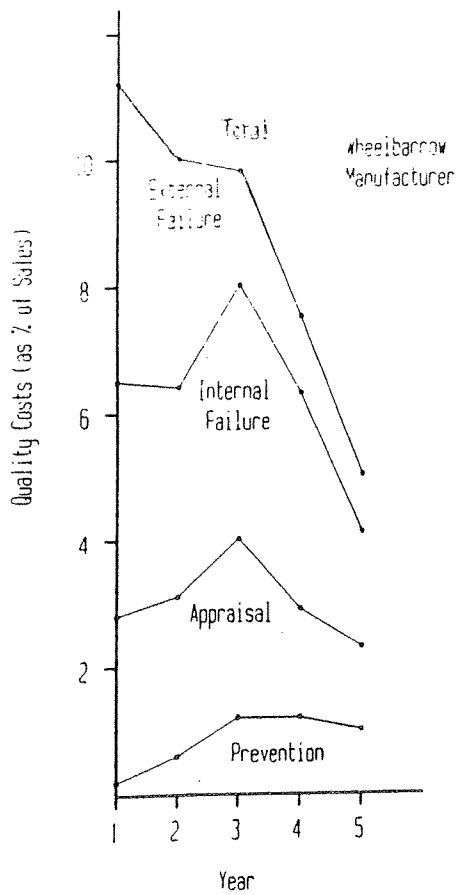
7.



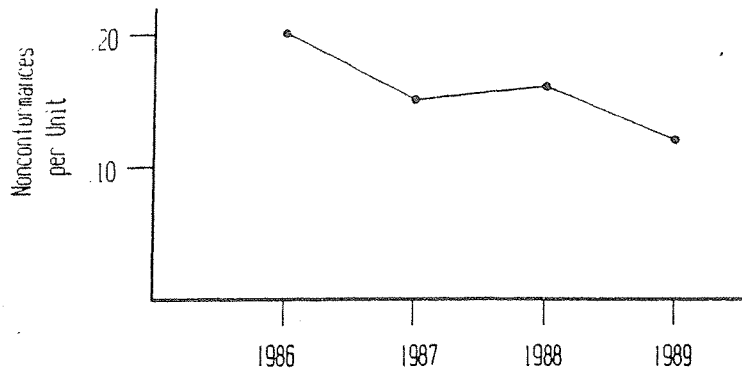
8.



9.



10.



There is a downward trend over the four years.

11-13. See pages 79-82 for examples.

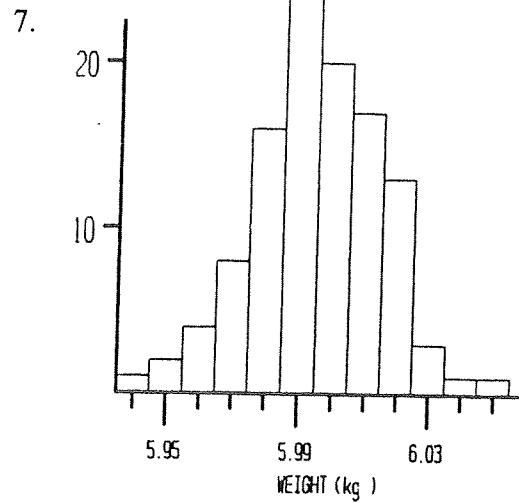
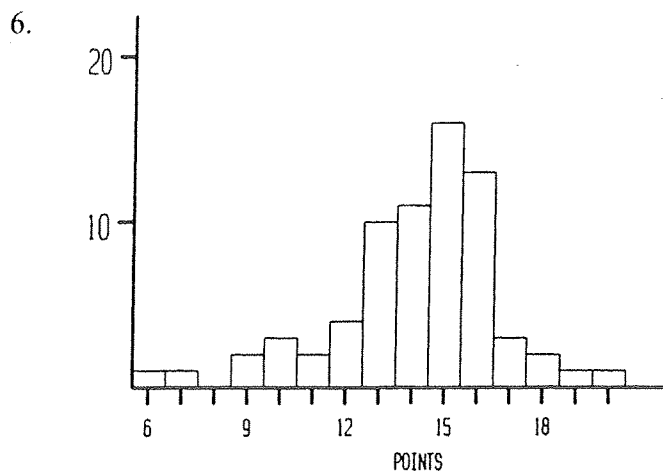
# Chapter 4. FUNDAMENTALS OF STATISTICS

1. 0.86, 0.63, 0.15, 0.48

| 2, 3. | Number          | Boundaries           | Precision | g.p.e. | r.e.   |
|-------|-----------------|----------------------|-----------|--------|--------|
| (a)   | 8.24            | 8.235 < 8.24 < 8.45  | 0.01      | 0.005  | 0.0006 |
| (b)   | 522             | 521.5 < 522 < 522.5  | 1         | 0.5    | 0.001  |
| (c)   | $6.3 \times 10$ | 625 < 630 < 635      | 10        | 5      | 0.002  |
| (d)   | 0.02            | 0.015 < 0.02 < 0.025 | 0.01      | 0.005  | 0.3    |

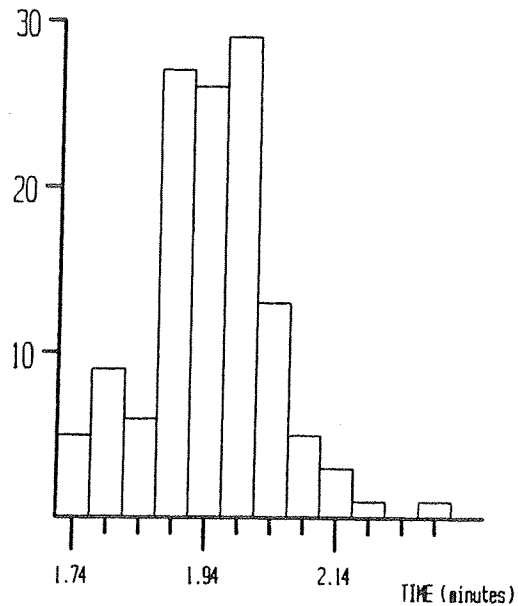
4.  $2.84 \times 10^2$ , 22, 0.64, 0.8937, 0.9

5. 66.4, 379.1, 5, 4.652,  $6.2 \times 10^2$

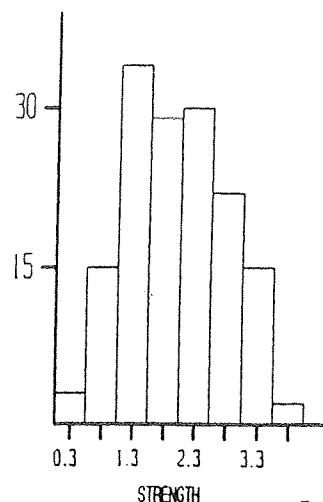


8.

| <u>Cell Boundaries</u> | <u>Cell Midpoint</u> | <u>Frequency</u> |
|------------------------|----------------------|------------------|
| 1.72-1.76              | 1.74                 | 5                |
| 1.77-1.81              | 1.79                 | 9                |
| 1.82-1.86              | 1.84                 | 6                |
| 1.87-1.91              | 1.89                 | 27               |
| 1.92-1.96              | 1.94                 | 26               |
| 1.97-2.01              | 1.99                 | 29               |
| 2.02-2.06              | 2.04                 | 13               |
| 2.07-2.11              | 2.09                 | 5                |
| 2.12-2.16              | 2.14                 | 3                |
| 2.17-2.21              | 2.19                 | 1                |
| 2.22-2.26              | 2.24                 | 0                |
| 2.27-2.31              | 2.29                 | 1                |



| 9. | Cell<br>Boundaries | Cell<br>Midpoints | Frequency |
|----|--------------------|-------------------|-----------|
|    | 0.05-0.54          | 0.3               | 3         |
|    | 0.55-1.04          | 0.8               | 15        |
|    | 1.05-1.54          | 1.3               | 34        |
|    | 1.55-2.04          | 1.8               | 29        |
|    | 2.05-2.54          | 2.3               | 30        |
|    | 2.55-3.04          | 2.8               | 22        |
|    | 3.05-3.54          | 3.3               | 15        |
|    | 3.55-4.04          | 3.8               | 2         |



10.

| Scores | Freq.     | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|--------|-----------|-------------------|---------------------|---------------------------------|
| 6      | 1         | 1/70 = 0.014      | 0+1 = 1             | 1/70 = 0.014                    |
| 7      | 1         | 1/70 = 0.014      | 1+1 = 2             | 2/70 = 0.029                    |
| 8      | 0         | 0/70 = 0          | 2+0 = 2             | 2/70 = 0.029                    |
| 9      | 2         | 2/70 = 0.029      | 2+2 = 4             | 4/70 = 0.057                    |
| 10     | 3         | 3/70 = 0.043      | 4+3 = 7             | 7/70 = 0.100                    |
| 11     | 2         | 2/70 = 0.029      | 7+2 = 9             | 9/70 = 0.129                    |
| 12     | 4         | 4/70 = 0.057      | 9+4 = 13            | 13/70 = 0.186                   |
| 13     | 10        | 10/70 = 0.143     | 13+10 = 23          | 23/70 = 0.329                   |
| 14     | 11        | 11/70 = 0.157     | 23+11 = 34          | 34/70 = 0.486                   |
| 15     | 16        | 16/70 = 0.229     | 34+16 = 50          | 50/70 = 0.714                   |
| 16     | 13        | 13/70 = 0.186     | 50+13 = 63          | 63/70 = 0.900                   |
| 17     | 3         | 3/70 = 0.043      | 63+3 = 66           | 66/70 = 0.943                   |
| 18     | 2         | 2/70 = 0.029      | 66+2 = 68           | 68/70 = 0.971                   |
| 19     | 1         | 1/70 = 0.014      | 68+1 = 69           | 69/70 = 0.986                   |
| 20     | 1         | 1/70 = 0.014      | 69+1 = 70           | 70/70 = 1.000                   |
|        | <u>70</u> | <u>1.00</u>       |                     |                                 |

Graph not shown, but similar to Problem 13

11.

| Weights | Freq.      | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|---------|------------|-------------------|---------------------|---------------------------------|
| 5.94    | 1          | 1/110 = 0.9%      | 0+1 = 1             | 1/110 = 0.9%                    |
| 5.95    | 2          | 2/110 = 1.8       | 1+2 = 3             | 3/110 = 2.7                     |
| 5.96    | 4          | 4/110 = 3.6       | 3+4 = 7             | 7/110 = 6.4                     |
| 5.97    | 8          | 8/110 = 7.3       | 7+8 = 15            | 15/110 = 13.6                   |
| 5.98    | 16         | 16/110 = 14.5     | 15+16 = 31          | 31/110 = 28.2                   |
| 5.99    | 24         | 24/110 = 21.8     | 31+24 = 55          | 55/110 = 50.0                   |
| 6.00    | 20         | 20/110 = 18.2     | 55+20 = 75          | 75/110 = 68.2                   |
| 6.01    | 17         | 17/110 = 15.5     | 75+17 = 92          | 92/110 = 83.6                   |
| 6.02    | 13         | 13/110 = 11.8     | 92+13 = 105         | 105/110 = 95.4                  |
| 6.03    | 3          | 3/110 = 2.7       | 105+3 = 108         | 108/110 = 98.2                  |
| 6.04    | 1          | 1/110 = 0.9       | 108+1 = 109         | 109/110 = 99.1                  |
| 6.05    | 1          | 1/110 = 0.9       | 109+1 = 110         | 110/110 = 100.0%                |
|         | <u>110</u> | <u>99.9%</u>      |                     |                                 |

Graph not shown, but similar to Problem 13

12.

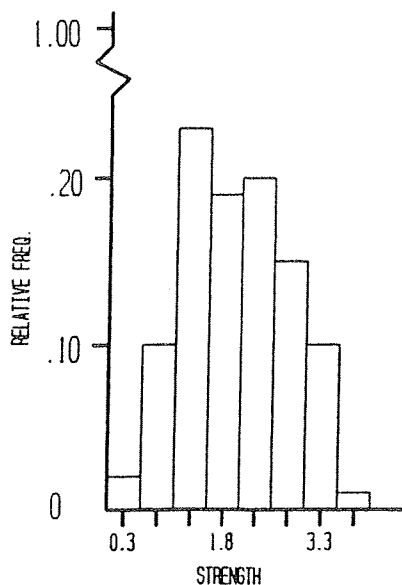
| Cell<br>Midpoint | Freq.      | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|------------------|------------|-------------------|---------------------|---------------------------------|
| 1.74             | 5          | $5/125 = 0.040$   | $0+5 = 5$           | $5/125 = 0.040$                 |
| 1.79             | 9          | $9/125 = 0.072$   | $5+9 = 14$          | $14/125 = 0.112$                |
| 1.84             | 6          | $6/125 = 0.048$   | $14+6 = 20$         | $20/125 = 0.160$                |
| 1.89             | 27         | $27/125 = 0.216$  | $20+27 = 47$        | $47/125 = 0.376$                |
| 1.94             | 26         | $26/125 = 0.208$  | $47+26 = 73$        | $73/125 = 0.584$                |
| 1.99             | 29         | $29/125 = 0.232$  | $73+29 = 102$       | $102/125 = 0.816$               |
| 2.04             | 13         | $13/125 = 0.104$  | $102+13 = 115$      | $115/125 = 0.920$               |
| 2.09             | 5          | $5/125 = 0.040$   | $115+5 = 120$       | $120/125 = 0.960$               |
| 2.14             | 3          | $3/125 = 0.024$   | $120+3 = 123$       | $123/125 = 0.984$               |
| 2.19             | 1          | $1/125 = 0.008$   | $123+1 = 124$       | $124/125 = 0.992$               |
| 2.24             | 0          | $0/125 = 0$       | $124+0 = 124$       | $124/125 = 0.992$               |
| 2.29             | 1          | $1/125 = 0.008$   | $124+1 = 125$       | $125/125 = 1.000$               |
|                  | <u>125</u> | <u>1.000</u>      |                     |                                 |

Graph not shown, but similar to Problem 13

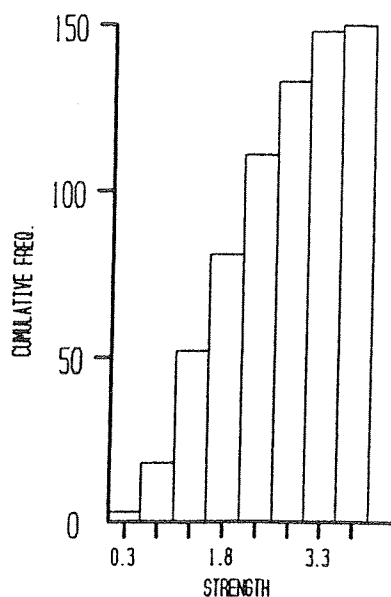
13.

| Cell<br>Midpoint | Freq.      | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|------------------|------------|-------------------|---------------------|---------------------------------|
| 0.3              | 3          | $3/150 = 0.020$   | $0+3 = 3$           | $3/150 = 0.020$                 |
| 0.8              | 15         | $15/150 = 0.100$  | $3+15 = 18$         | $18/150 = 0.120$                |
| 1.3              | 34         | $34/150 = 0.227$  | $18+34 = 52$        | $52/150 = 0.347$                |
| 1.8              | 29         | $29/150 = 0.193$  | $52+29 = 81$        | $81/150 = 0.540$                |
| 2.3              | 30         | $30/150 = 0.200$  | $81+30 = 111$       | $111/150 = 0.740$               |
| 2.8              | 22         | $22/150 = 0.147$  | $111+22 = 133$      | $133/150 = 0.888$               |
| 3.3              | 15         | $15/150 = 0.100$  | $133+15 = 148$      | $148/150 = 0.987$               |
| 3.8              | 2          | $2/150 = 0.013$   | $148+2 = 150$       | $150/150 = 1.000$               |
|                  | <u>150</u> | <u>1.000</u>      |                     |                                 |

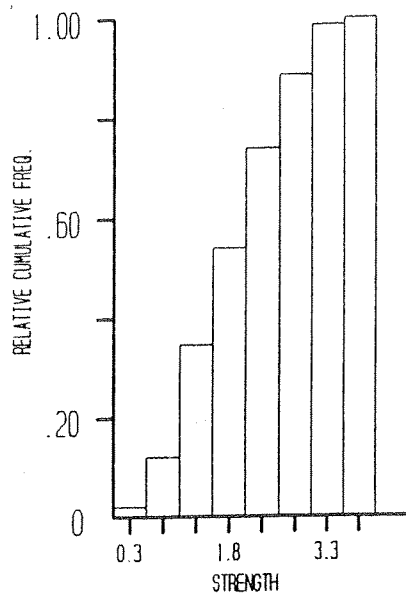
13a



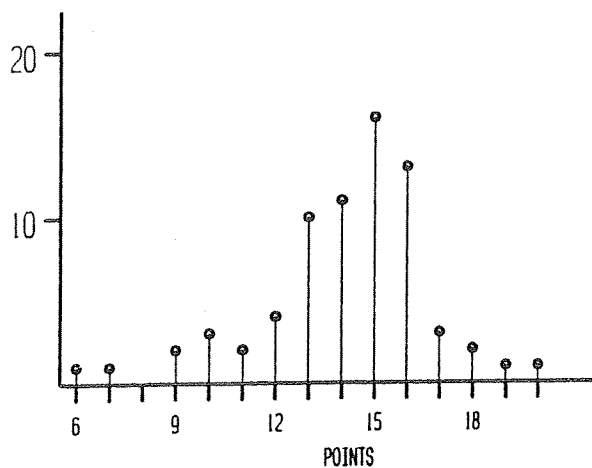
13b



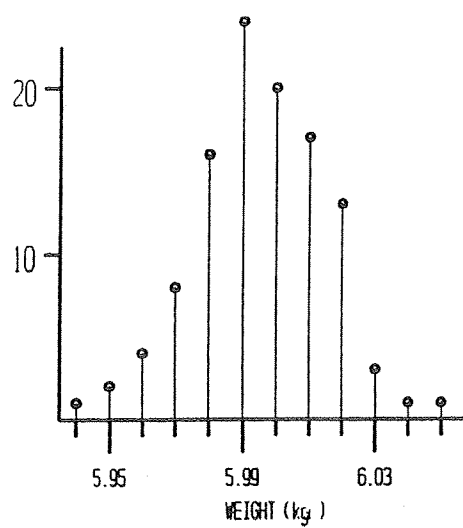
13c



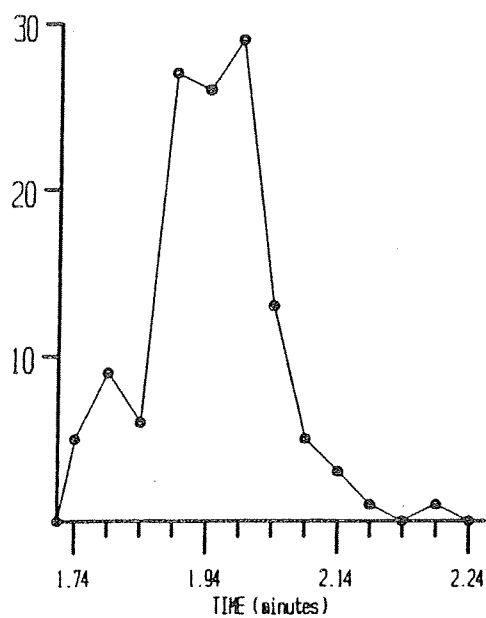
14a



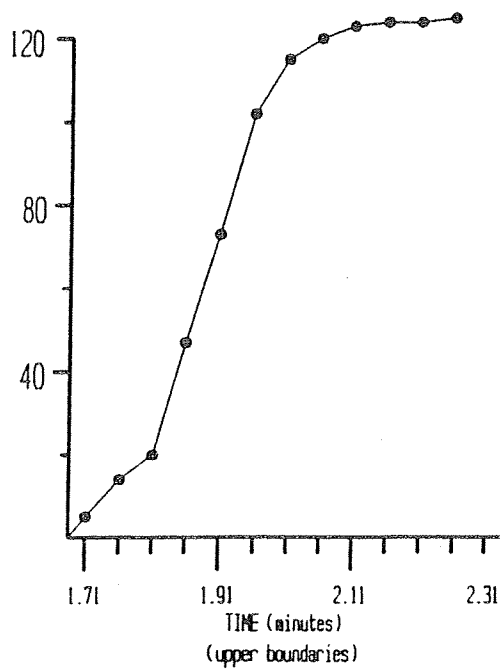
14b



15a

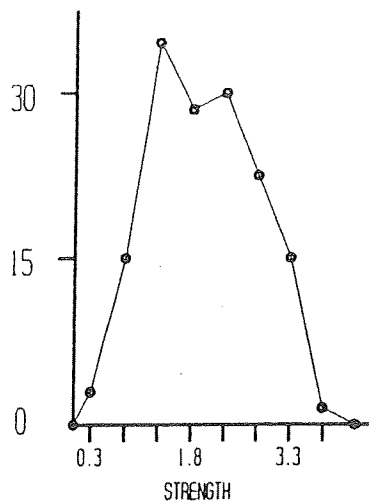


15b

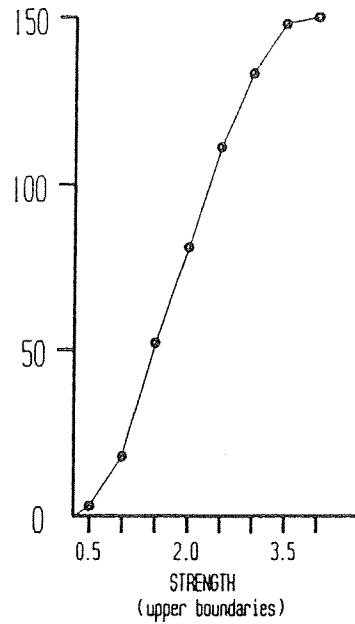




16a



16b



$$17. \quad \bar{X} = \frac{\sum x}{n} = \frac{115 + 113 + 121 + 115 + 116}{5} = 116 \text{ volts}$$

$$18. \quad \bar{X} = \frac{\sum x}{n} = \frac{25.6 + 24.8 + 22.6 + 21.3 + 19.6 + 18.5 + 16.2 + 15.5}{8} = 20.5 \text{ m}$$

| $x$ | $f$        | $fx$          | $\bar{X} = \frac{\sum fx}{n}$ $= \frac{19,508}{206}$ $= 95 \text{ db}$ |
|-----|------------|---------------|--|
| 148 | 2          | 296           |  |
| 139 | 3          | 417           |  |
| 130 | 8          | 1,040         |  |
| 121 | 11         | 1,331         |  |
| 112 | 27         | 3,024         |  |
| 103 | 35         | 3,605         |  |
| 94  | 43         | 4,042         |  |
| 85  | 33         | 2,805         |  |
| 76  | 20         | 1,520         |  |
| 67  | 12         | 804           |  |
| 58  | 6          | 348           |  |
| 49  | 4          | 196           |  |
| 40  | 2          | 80            |  |
|     | <u>206</u> | <u>19,508</u> |  |

| $x$ | $f$       | $fx$         | $\bar{X} = \frac{\sum fx}{n}$ $= \frac{276.7}{65}$ $= 4.3 \text{ kg}$ |
|-----|-----------|--------------|---|
| 3.5 | 6         | 21.0         |   |
| 3.8 | 9         | 34.2         |   |
| 4.1 | 18        | 73.8         |   |
| 4.4 | 14        | 61.6         |   |
| 4.7 | 13        | 61.1         |   |
| 5.0 | 5         | 25.0         |   |
|     | <u>65</u> | <u>276.7</u> |   |

$$21. \quad \bar{X}_w = \frac{\sum w\bar{X}}{\sum w}$$

$$= \frac{(3)(3320) + (2)(3180)}{3 + 2}$$

$$= 3264 \text{ h}$$

$$22. \bar{x}_w = \Sigma w\bar{x} / \Sigma w$$

$$= \frac{(24)(1.75) + (18)(1.79) + (29)(1.68)}{24 + 18 + 29}$$

$$= 1.73 \text{ m}$$

$$23. \text{ a. } 8, 11, 15, 18, 22; \text{ Md} = 15$$

$$\text{ b. } 28, 33, 35, 36, 38, 43; \text{ Md} = \frac{35 + 36}{2} = 35.5$$

$$24. \text{ a. } \text{Md} = L + \left( \frac{\frac{n}{2} - cf}{f} \right) i = 1.915 + \left( \frac{\frac{125}{2} - 47}{26} \right) 0.05 = 1.94$$

$$\text{ b. } \text{Md} = 1.55 + \left( \frac{\frac{150}{2} - 52}{29} \right) 0.5 = 1.95$$

$$\text{ c. } \text{Md} = 90 + \left( \frac{\frac{206}{2} - 77}{43} \right) 9 = 95 \text{ db}$$

$$\text{ d. } \text{Md} = 4.0 + \left( \frac{\frac{65}{2} - 15}{18} \right) .3 = 4.3$$

$$\text{ e. } \text{Md} = 1.60 + \left( \frac{\frac{88}{2} - 39}{12} \right) 0.3 = 1.73$$

$$\text{ f. } \text{Md} = 1450 + \left( \frac{\frac{77}{2} - 19}{22} \right) 300 = 1716$$

$$25. 55, \text{ none}, 14 \text{ and } 17$$

$$26. 15, 5.99, 1.99, 1.3, 94, 4.1$$

$$27. \text{ a. } R = H - L = 25 - 14 = 11$$

$$\text{ c. } R = H - L = 20 - 6 = 14$$

$$\text{ b. } R = 45 - 39 = 6$$

$$\text{ d. } R = 6.05 - 5.94 = 0.11$$

$$28. s = \sqrt{\frac{n\Sigma x^2 - (\Sigma x)^2}{n(n-1)}} = \sqrt{\frac{5(7152350) - (5980)^2}{5(5-1)}} = 8.2 \text{ vib/sec}$$

$$29. s = \sqrt{\frac{4(0.024) - (.308)^2}{4(4-1)}} = 0.004 \text{ mm}$$

30.

| Mid-point<br>(x) | Freq.<br>(f) | (fx)         | (fx <sup>2</sup> ) |
|------------------|--------------|--------------|--------------------|
| 5                | 1            | 5            | 0.3                |
| .8               | 16           | 12.8         | 10.2               |
| 1.1              | 12           | 13.2         | 14.5               |
| 1.4              | 10           | 14.0         | 19.6               |
| 1.7              | 12           | 20.4         | 34.7               |
| 2.0              | 18           | 36.0         | 72.0               |
| 2.3              | 16           | 36.8         | 84.6               |
| 2.6              | 3            | 7.8          | 20.3               |
|                  | <u>88</u>    | <u>141.5</u> | <u>256.2</u>       |

$$s = \sqrt{\frac{n\sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{88(256.2) - (141.5)^2}{88(88-1)}}$$

$$= .57\%$$

31a.

| Mid-point<br>(x) | Freq.<br>(f) | (fx)       | (fx <sup>2</sup> ) |
|------------------|--------------|------------|--------------------|
| 0.3              | 3            | 0.9        | 0.27               |
| 0.8              | 15           | 12.0       | 9.60               |
| 1.3              | 34           | 44.2       | 57.46              |
| 1.8              | 29           | 52.2       | 93.96              |
| 2.3              | 30           | 69.0       | 158.70             |
| 2.8              | 22           | 61.6       | 172.48             |
| 3.3              | 15           | 49.5       | 163.35             |
| 3.8              | <u>2</u>     | <u>7.6</u> | <u>28.88</u>       |
|                  | 150          | 297.0      | 684.70             |

$$s = \sqrt{\frac{n\sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{150(684.7) - (297.0)^2}{150(150-1)}}$$

$$= 0.8$$

31b

| Mid-point<br>(x) | Freq.<br>(f) | (fx)      | (fx <sup>2</sup> ) |
|------------------|--------------|-----------|--------------------|
| 148              | 2            | 296       | 43,808             |
| 139              | 3            | 417       | 57,963             |
| 130              | 8            | 1,040     | 135,200            |
| 121              | 11           | 1,331     | 161,051            |
| 112              | 27           | 3,024     | 338,688            |
| 103              | 35           | 3,605     | 371,315            |
| 94               | 43           | 4,042     | 379,948            |
| 85               | 33           | 2,805     | 238,425            |
| 76               | 20           | 1,520     | 115,520            |
| 67               | 12           | 804       | 53,868             |
| 58               | 6            | 348       | 20,184             |
| 49               | 4            | 196       | 9,604              |
| 40               | <u>2</u>     | <u>80</u> | <u>3,200</u>       |
|                  | 206          | 19,508    | 1,928,774          |

$$s = \sqrt{\frac{n\sum fX^2 - (\sum fX)^2}{n(n-1)}}$$

$$= \sqrt{\frac{206(1,928,774) - (19,508)^2}{206(206-1)}}$$

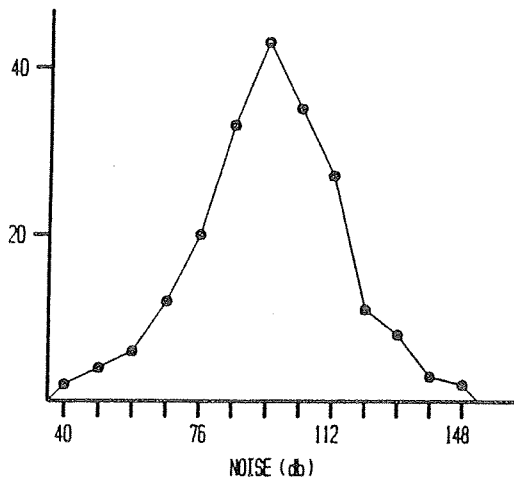
$$= 20 \text{ db}$$

| Mid-point<br>( $\chi$ ) | Freq.<br>( $f$ ) | ( $f\chi$ )         | ( $f\chi^2$ )       |
|-------------------------|------------------|---------------------|---------------------|
| 1000                    | 6                | 6000                | $6.00 \times 10^6$  |
| 1300                    | 13               | 16900               | $21.97 \times 10^6$ |
| 1600                    | 22               | 35200               | $56.32 \times 10^6$ |
| 1900                    | 17               | 32300               | $61.37 \times 10^6$ |
| 2200                    | 11               | 24200               | $53.24 \times 10^6$ |
| 2500                    | 8                | 20000               | $50.00 \times 10^6$ |
|                         | 77               | $134.6 \times 10^3$ | $248.9 \times 10^6$ |

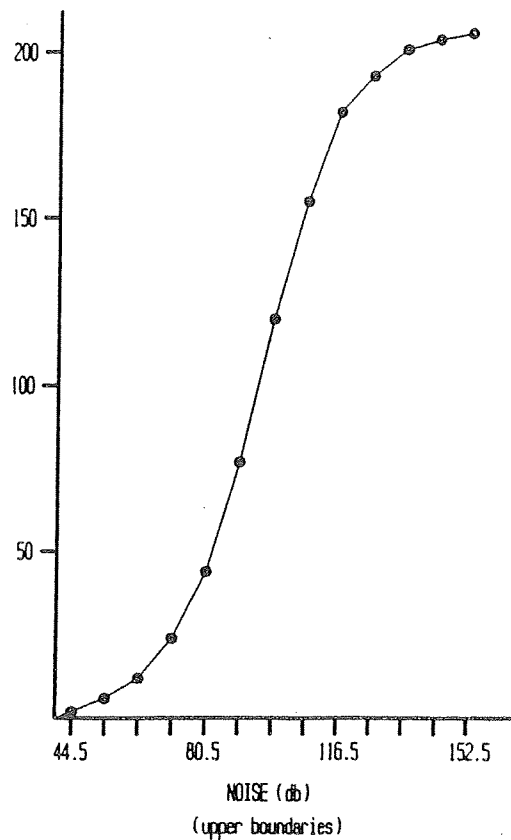
$$\bar{\chi} = \Sigma f\chi/n = 134.6 \times 10^3/77 = 1748 \text{ inspections}$$

$$s = \sqrt{\frac{n\Sigma f\chi^2 - (\Sigma f\chi)^2}{n(n-1)}} = \sqrt{\frac{77(248.9 \times 10^6) - (134.6 \times 10^3)^2}{77(77-1)}} = 423$$

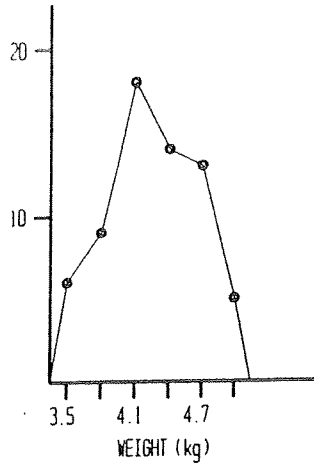
33a



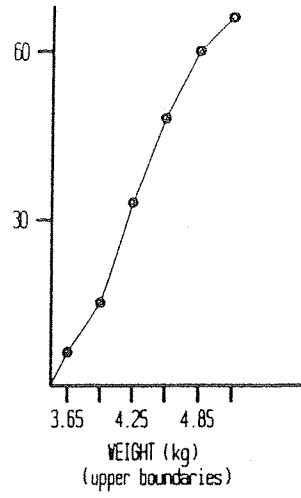
33b



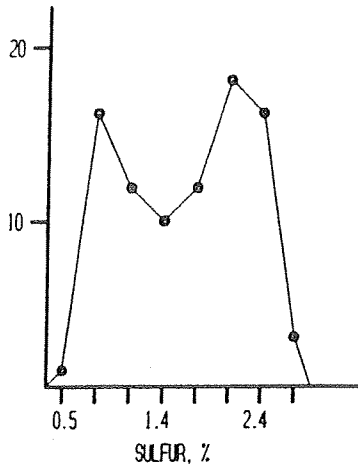
34a



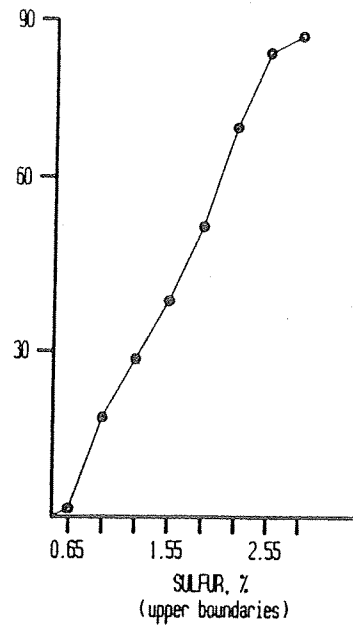
34b



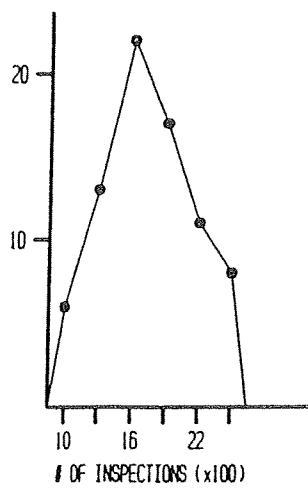
35a



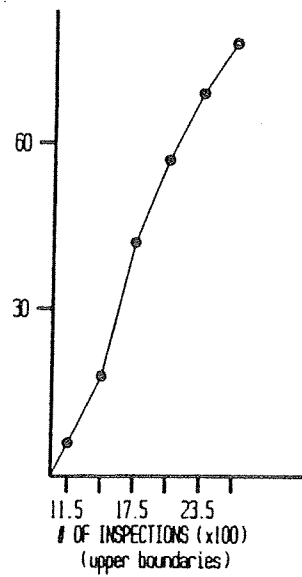
35b



36a



36b



| 37. Cell<br>Mid-<br>point | Freq.      | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|---------------------------|------------|-------------------|---------------------|---------------------------------|
| 40                        | 2          | $2/206 = 0.010$   | $0+2 = 2$           | $2/206 = 0.010$                 |
| 49                        | 4          | $4/206 = 0.019$   | $2+4 = 6$           | $6/206 = 0.029$                 |
| 58                        | 6          | $6/206 = 0.029$   | $6+6 = 12$          | $12/206 = 0.058$                |
| 67                        | 12         | $12/206 = 0.058$  | $12+12 = 24$        | $24/206 = 0.117$                |
| 76                        | 20         | $20/206 = 0.097$  | $24+20 = 44$        | $44/206 = 0.214$                |
| 85                        | 33         | $33/206 = 0.160$  | $44+33 = 77$        | $77/206 = 0.374$                |
| 94                        | 43         | $43/206 = 0.209$  | $77+43 = 120$       | $120/206 = 0.583$               |
| 103                       | 35         | $35/206 = 0.170$  | $120+35 = 155$      | $155/206 = 0.752$               |
| 112                       | 27         | $27/206 = 0.131$  | $155+27 = 182$      | $182/206 = 0.883$               |
| 121                       | 11         | $11/206 = 0.053$  | $182+11 = 193$      | $193/206 = 0.937$               |
| 130                       | 8          | $8/206 = 0.039$   | $193+8 = 201$       | $201/206 = 0.976$               |
| 139                       | 3          | $3/206 = 0.015$   | $201+3 = 204$       | $204/206 = 0.990$               |
| 148                       | 2          | $2/206 = 0.010$   | $204+2 = 206$       | $206/206 = 1.000$               |
|                           | <u>206</u> | <u>1.000</u>      |                     |                                 |

| 38. Cell<br>Mid-<br>point | Freq.     | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|---------------------------|-----------|-------------------|---------------------|---------------------------------|
| 3.5                       | 6         | $6/65 = 0.092$    | $0+6 = 6$           | $6/65 = 0.092$                  |
| 3.8                       | 9         | $9/65 = 0.138$    | $6+9 = 15$          | $15/65 = 0.231$                 |
| 4.1                       | 18        | $18/65 = 0.277$   | $15+18 = 33$        | $33/65 = 0.508$                 |
| 4.4                       | 14        | $14/65 = 0.215$   | $33+14 = 47$        | $47/65 = 0.723$                 |
| 4.7                       | 13        | $13/65 = 0.200$   | $47+13 = 60$        | $60/65 = 0.923$                 |
| 5.0                       | 5         | $5/65 = 0.077$    | $60+5 = 65$         | $65/65 = 1.000$                 |
|                           | <u>65</u> | <u>0.999</u>      |                     |                                 |

| 39. Cell<br>Mid-<br>point | Freq.     | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|---------------------------|-----------|-------------------|---------------------|---------------------------------|
| 0.5                       | 1         | $1/88 = 0.011$    | $0+1 = 1$           | $1/88 = 0.010$                  |
| 0.8                       | 16        | $16/88 = 0.182$   | $1+16 = 17$         | $17/88 = 0.156$                 |
| 1.1                       | 12        | $12/88 = 0.136$   | $17+12 = 29$        | $29/88 = 0.330$                 |
| 1.4                       | 10        | $10/88 = 0.114$   | $29+10 = 39$        | $39/88 = 0.443$                 |
| 1.7                       | 12        | $12/88 = 0.136$   | $39+12 = 51$        | $51/88 = 0.580$                 |
| 2.0                       | 18        | $18/88 = 0.205$   | $51+18 = 69$        | $69/88 = 0.784$                 |
| 2.3                       | 16        | $16/88 = 0.182$   | $69+16 = 85$        | $85/88 = 0.966$                 |
| 2.6                       | 3         | $3/88 = 0.034$    | $85+3 = 88$         | $88/88 = 1.000$                 |
|                           | <u>88</u> | <u>1.000</u>      |                     |                                 |

| 40. Cell<br>Mid-<br>point | Freq.     | Relative<br>Freq. | Cumulative<br>Freq. | Relative<br>Cumulative<br>Freq. |
|---------------------------|-----------|-------------------|---------------------|---------------------------------|
| 1000                      | 6         | $6/77 = 0.078$    | $0+6 = 6$           | $6/77 = 0.078$                  |
| 1300                      | 13        | $13/77 = 0.169$   | $6+13 = 19$         | $19/77 = 0.247$                 |
| 1600                      | 22        | $22/77 = 0.286$   | $19+22 = 41$        | $41/77 = 0.532$                 |
| 1900                      | 17        | $17/77 = 0.221$   | $41+17 = 58$        | $58/77 = 0.753$                 |
| 2200                      | 11        | $11/77 = 0.143$   | $58+11 = 69$        | $69/77 = 0.896$                 |
| 2500                      | 8         | $8/77 = 0.104$    | $69+8 = 77$         | $77/77 = 1.000$                 |
|                           | <u>77</u> | <u>1.001</u>      |                     |                                 |

| 41a | $\chi$ | $f_i$    | $(\chi_i - \bar{\chi})$ | $f(\chi_i - \bar{\chi})^3$ | $f(\chi_i - \bar{\chi})^4$ |
|-----|--------|----------|-------------------------|----------------------------|----------------------------|
|     | 6      | 1        | -8.13                   | -537.37                    | 4,368.80                   |
|     | 7      | 1        | -7.13                   | -362.47                    | 2,584.39                   |
|     | 8      | 0        | -6.13                   | 0                          | 0                          |
|     | 9      | 2        | -5.13                   | -270.01                    | 1,385.16                   |
|     | 10     | 3        | -4.13                   | -211.33                    | 872.81                     |
|     | 11     | 2        | -3.13                   | - 61.33                    | 191.96                     |
|     | 12     | 4        | -2.13                   | - 38.65                    | 82.33                      |
|     | 13     | 10       | -1.13                   | - 14.43                    | 16.30                      |
|     | 14     | 11       | -0.13                   | - 0.02                     | 0                          |
|     | 15     | 16       | 0.87                    | 10.54                      | 9.17                       |
|     | 16     | 13       | 1.87                    | 85.01                      | 158.97                     |
|     | 17     | 3        | 2.87                    | 70.92                      | 203.54                     |
|     | 18     | 2        | 3.87                    | 115.92                     | 448.62                     |
|     | 19     | 1        | 4.87                    | 115.50                     | 562.49                     |
|     | 20     | <u>1</u> | <u>5.87</u>             | <u>202.26</u>              | <u>1,187.28</u>            |
|     |        | 70       |                         | -895.46                    | 12,071.82                  |

$$\bar{\chi} = 14.13 \quad s = 2.53$$

$$a_3 = \frac{\Sigma f(\chi_i - \bar{\chi})^3/n}{s^3} = \frac{-895.46/70}{2.53^3} = -0.79$$

$$a_4 = \frac{\Sigma f(\chi_i - \bar{\chi})^4/n}{s^4} = \frac{12071.82/70}{2.53^4} = 4.21$$

Distribution is very peaked and quite skewed to the left.

| 41b. | $\chi$ | $f$      | $(\chi_i - \bar{\chi})$ | $f(\chi_i - \bar{\chi})^3$ | $f(\chi_i - \bar{\chi})^4$ |
|------|--------|----------|-------------------------|----------------------------|----------------------------|
|      | -6     | 1        | -5.54                   | -170.03                    | 941.97                     |
|      | -5     | 2        | -4.54                   | -187.15                    | 849.68                     |
|      | -4     | 4        | -3.54                   | -177.45                    | 628.16                     |
|      | -3     | 8        | -2.54                   | -131.10                    | 332.99                     |
|      | -2     | 16       | -1.54                   | - 58.44                    | 89.99                      |
|      | -1     | 24       | -0.54                   | - 3.78                     | 2.04                       |
|      | 0      | 20       | .46                     | 1.95                       | .90                        |
|      | 1      | 17       | 1.46                    | 40.45                      | 59.06                      |
|      | 2      | 13       | 2.46                    | 193.53                     | 476.08                     |
|      | 3      | 3        | 3.46                    | 124.26                     | 429.96                     |
|      | 4      | 1        | 4.46                    | 88.72                      | 395.68                     |
|      | 5      | <u>1</u> | <u>5.46</u>             | <u>162.77</u>              | <u>888.73</u>              |
|      |        | 110      |                         | -116.27                    | 5,171.72                   |

Note:  $\chi$  is coded from 6.00.

$$\bar{\chi} = -0.46 \quad \text{True } \bar{\chi} = 5.9954 \quad s = 1.97$$

$$a_3 = \frac{\Sigma f(\chi_i - \bar{\chi})^3/n}{s^3} = \frac{-116.27/110}{1.97^3} = -0.14$$

$$a_4 = \frac{\Sigma f(\chi_i - \bar{\chi})^4/n}{s^4} = \frac{5171.72/110}{1.97^4} = 3.11$$

Distribution is slightly skewed to the left and not quite as peaked as normal.

| 41c | $x$  | $f$        | $(x_i - \bar{x})$ | $f(x_i - \bar{x})^3 \times 10^3$ | $f(x_i - \bar{x})^4 \times 10^3$ |
|-----|------|------------|-------------------|----------------------------------|----------------------------------|
|     | 1.74 | 5          | -.2032            | -41.9509                         | 8.5244                           |
|     | 1.79 | 9          | -.1532            | -32.3608                         | 4.9577                           |
|     | 1.84 | 6          | -.1032            | - 6.5946                         | .6806                            |
|     | 1.89 | 27         | -.0532            | - 4.0654                         | .2163                            |
|     | 1.94 | 26         | -.0032            | - .0009                          | nil                              |
|     | 1.99 | 29         | .0468             | 2.9726                           | .1391                            |
|     | 2.04 | 13         | .0968             | 11.7915                          | 1.1414                           |
|     | 2.09 | 5          | .1468             | 15.8179                          | 2.3221                           |
|     | 2.14 | 3          | .1968             | 12.8663                          | 4.5001                           |
|     | 2.19 | 1          | .2468             | 15.0326                          | 3.7101                           |
|     | 2.24 | 0          | .2968             | 0                                | 0                                |
|     | 2.29 | 1          | .3468             | 41.7097                          | 14.4649                          |
|     |      | <u>125</u> |                   | <u>+25.218 x 10<sup>3</sup></u>  | <u>40.6567 x 10<sup>3</sup></u>  |

$$\bar{x} = 1.9432$$

$$s = .096249$$

$$a_3 = \frac{\sum f(x_i - \bar{x})^3/n}{s^3} = \frac{25.218 \times 10^3/125}{.096249^3} = +0.23$$

$$a_4 = \frac{\sum f(x_i - \bar{x})^4/n}{s^4} = \frac{40.6567 \times 10^3/125}{.096249^4} = 3.79$$

Distribution is slightly skewed to the right and somewhat peaked.

| 41d | $x$ | $f$        | $(x_i - \bar{x})$ | $f(x_i - \bar{x})^3$ | $f(x_i - \bar{x})^4$ |
|-----|-----|------------|-------------------|----------------------|----------------------|
|     | 0.3 | 3          | -1.68             | -14.2249             | 23.8978              |
|     | 0.8 | 15         | -1.18             | -24.6455             | 29.0816              |
|     | 1.3 | 34         | -0.68             | -10.6907             | 7.2697               |
|     | 1.8 | 29         | -0.18             | - .1691              | .0304                |
|     | 2.3 | 30         | .32               | .9830                | .3146                |
|     | 2.8 | 22         | .82               | 12.1301              | 9.9467               |
|     | 3.3 | 15         | 1.32              | 34.4995              | 45.5394              |
|     | 3.8 | 2          | 1.82              | 12.0571              | 21.9439              |
|     |     | <u>150</u> |                   | <u>9.9395</u>        | <u>138.0242</u>      |

$$\bar{x} = 1.98$$

$$s = 0.8053512$$

$$a_3 = \frac{\sum f(x_i - \bar{x})^3/n}{s^3} = \frac{9.9395/150}{.8053512^3} = +.13$$

$$a_4 = \frac{\sum f(x_i - \bar{x})^4/n}{s^4} = \frac{138.0242/150}{.8053512^4} = 2.19$$

Slightly skewed to the right and flatter than normal.



| 41e | $\bar{x}$ | $f$       | $(x_i - \bar{x})$ | $f(x_i - \bar{x})^3$ | $f(x_i - \bar{x})^4$ |
|-----|-----------|-----------|-------------------|----------------------|----------------------|
|     | 3.5       | 6         | -0.7569           | -2.6018              | 1.96927              |
|     | 3.8       | 9         | -0.4569           | - .8584              | .3922                |
|     | 4.1       | 18        | -0.1569           | - .0695              | .0109                |
|     | 4.4       | 14        | 0.1431            | .0410                | .0059                |
|     | 4.7       | 13        | 0.4431            | 1.1310               | .5011                |
|     | 5.0       | 5         | 0.7431            | 2.0517               | 1.5246               |
|     |           | <u>65</u> |                   | <u>-0.306</u>        | <u>4.4040</u>        |

$$\bar{x} = 4.2569$$

$$s = 0.4212961$$

$$a_3 = \frac{\sum f(x_i - \bar{x})^3/n}{s^3} = \frac{-0.306/65}{0.4212961^3} = -0.06$$

$$a_4 = \frac{\sum f(x_i - \bar{x})^4/n}{s^4} = \frac{4.4040/65}{0.4212961^4} = 2.15$$

Distribution is essentially symmetrical and much flatter than normal.

| 41f | $\bar{x}$ | $f$       | $(x_i - \bar{x})$ | $f(x_i - \bar{x})^3 \times 10^6$ | $f(x_i - \bar{x})^4 \times 10^9$ |
|-----|-----------|-----------|-------------------|----------------------------------|----------------------------------|
|     | 1000      | 6         | -748              | -2511                            | 1878                             |
|     | 1300      | 13        | -448              | -1169                            | 523                              |
|     | 1600      | 22        | -148              | - 71                             | 11                               |
|     | 1900      | 17        | +152              | 60                               | 9                                |
|     | 2200      | 11        | +452              | 1015                             | 459                              |
|     | 2500      | 8         | +752              | 3402                             | 2558                             |
|     |           | <u>77</u> |                   | <u>+ 726 x 10<sup>6</sup></u>    | <u>5438 x 10<sup>9</sup></u>     |

$$\bar{x} = 1748$$

$$s = 423$$

$$a_3 = \frac{\sum f(x_i - \bar{x})^3/n}{s^3} = \frac{726 \times 10^6/77}{423^3} = +0.10$$

$$a_4 = \frac{\sum f(x_i - \bar{x})^4/n}{s^4} = \frac{5438 \times 10^9/77}{423^4} = 2.21$$

Distribution is essentially symmetrical and much flatter than normal.

42. Max. of 134.5 db ( $X_i$ )  
 from 17  $\bar{X} = 94.7$   
 $\sigma = 19.925$

$$z_1 = \frac{X_i - \mu}{\sigma}$$

$$z_1 = \frac{134.5 - 94.7}{19.925}$$

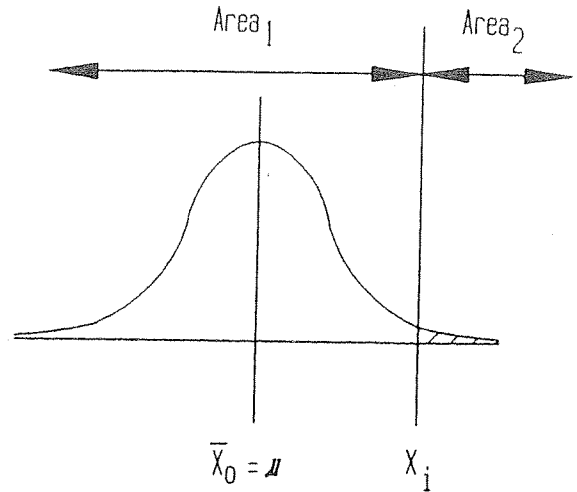
$$z_1 = 2.00$$

$$\text{Area}_1 = 0.9773$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.00 - 0.9773$$

$$\text{Area}_2 = 0.0227 \text{ or } 2.8\%$$



43. Min. of 3.65 ( $X_i$ )

Max. of 4.85 ( $X_i$ )

from 18  $\bar{X} = 4.25$

$$\sigma = .4213$$

$$z_1 = \frac{X_i - \mu}{\sigma}$$

$$z_1 = \frac{3.65 - 4.26}{.4213}$$

$$z_1 = -1.45$$

$$\text{Area}_1 = 0.0734$$

$$z_2 = \frac{X_i - \mu}{\sigma}$$

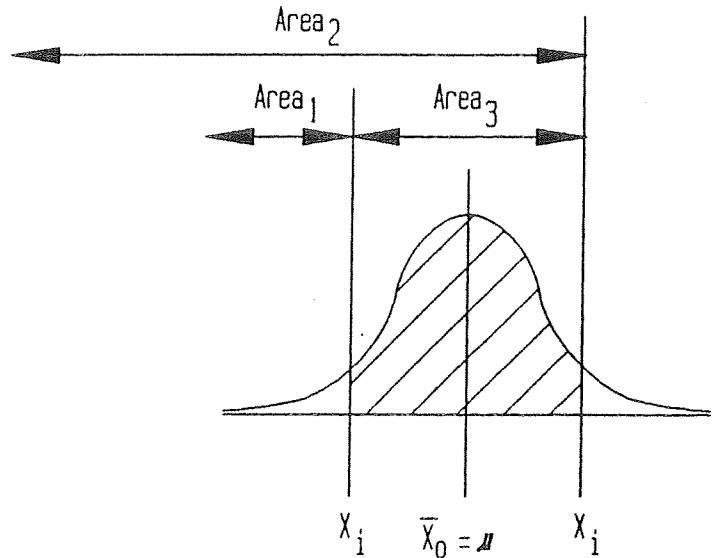
$$z_2 = \frac{4.85 - 4.26}{.4213}$$

$$z_2 = 1.40 \quad \text{Area}_2 = 0.9192$$

$$\text{Area}_3 = \text{Area}_2 - \text{Area}_1$$

$$\text{Area}_3 = 0.9192 - 0.0735$$

$$\text{Area}_3 = 0.8457 \text{ or } 84.6\%$$



44. Max. of 2.25 ( $x_i$ )

From 28  $\bar{x} = 1.65$

$\sigma = 0.617$

$$z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{2.25 - 1.65}{0.617}$$

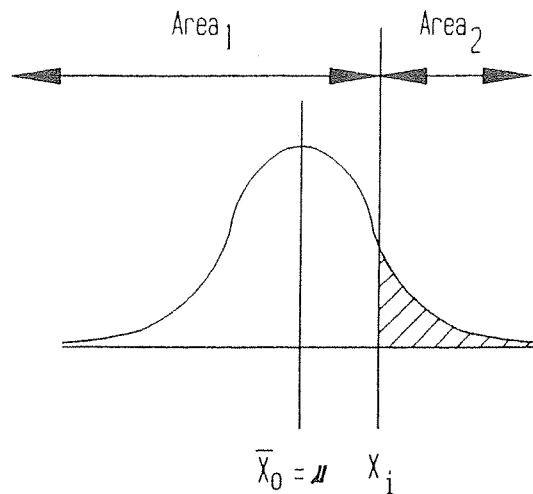
$$z_1 = 0.97$$

$$\text{Area}_1 = 0.8340$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.8340$$

$$\text{Area}_2 = 0.166 \text{ or } 16.6\%$$



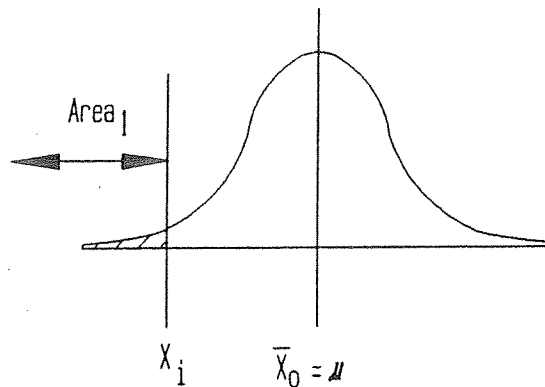
45a  $z = \frac{x_i - \mu}{\sigma}$

$$z = \frac{8.30 - 9.07}{0.40}$$

$$z = -1.93 \text{ Rounded}$$

From Table A<sub>1</sub>

$$\text{Area}_1 = 0.0268 \text{ or } 2.68\%$$



45b  $z_1 = \frac{x_i - \mu}{\sigma}$

$$z_1 = \frac{10.00 - 9.07}{0.40}$$

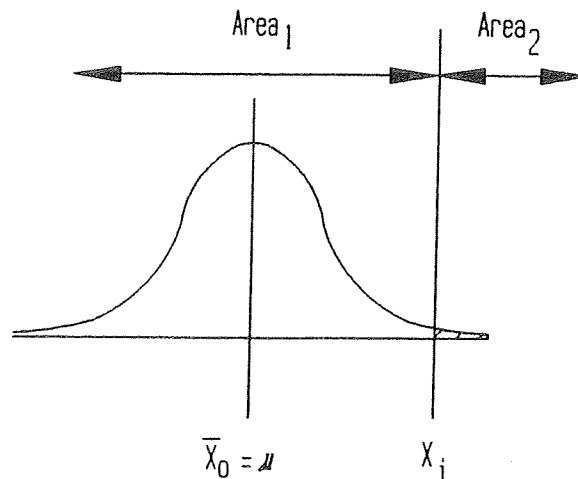
$$z_1 = +2.33 \text{ Rounded}$$

$$\text{Area}_1 = 0.9901$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.9901$$

$$\text{Area}_2 = 0.0099 \text{ or } 0.99\%$$



$$45c \quad z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{8.00 - 9.07}{0.40}$$

$$z_1 = -2.68$$

$$\text{Area}_1 = 0.0037$$

$$z_2 = \frac{x_i - \mu}{\sigma}$$

$$z_2 = \frac{10.10 - 9.07}{0.40}$$

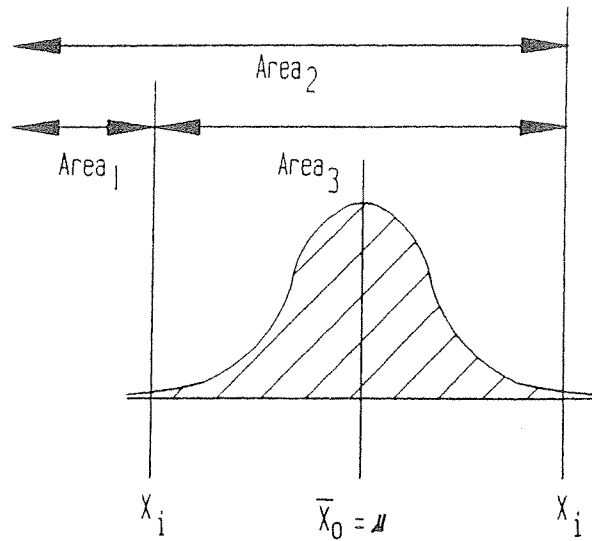
$$z_2 = +2.58$$

$$\text{Area}_2 = 0.9951$$

$$\text{Area}_3 = \text{Area}_2 - \text{Area}_1$$

$$\text{Area}_3 = 0.9951 - 0.0037$$

$$\text{Area}_3 = 0.9914 \text{ or } 99.14\%$$

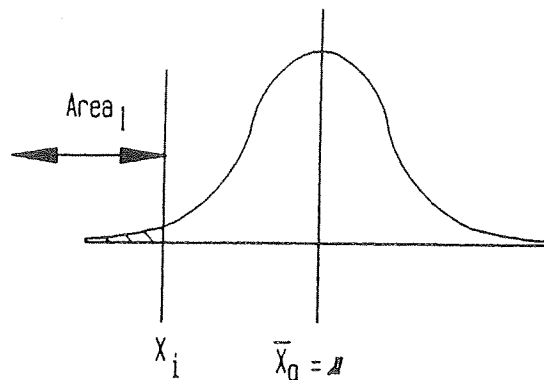


$$46a. \quad z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{13 - 16}{1.5}$$

$$z_1 = -2.00$$

$$\text{Area}_1 = 0.0228 \text{ or } 2.28\%$$



$$46b. \quad z_1 = \frac{x_i - \mu}{\sigma}$$

$$z_1 = \frac{20 - 16}{1.5}$$

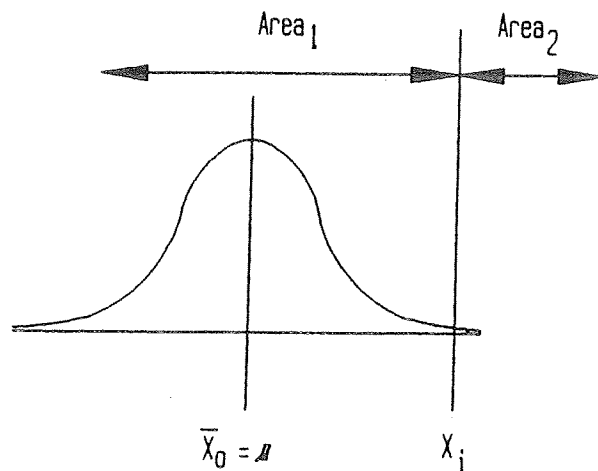
$$z_1 = +2.67$$

$$\text{Area}_1 = 0.9962$$

$$\text{Area}_2 = 1.000 - \text{Area}_1$$

$$\text{Area}_2 = 1.000 - 0.9962$$

$$\text{Area}_2 = 0.0038 \text{ or } 0.38\%$$



46c  $Area_1 = 0.0228$

$$z_2 = \frac{x_i - \mu}{\sigma}$$

$$z_2 = \frac{20.5 - 16}{1.5}$$

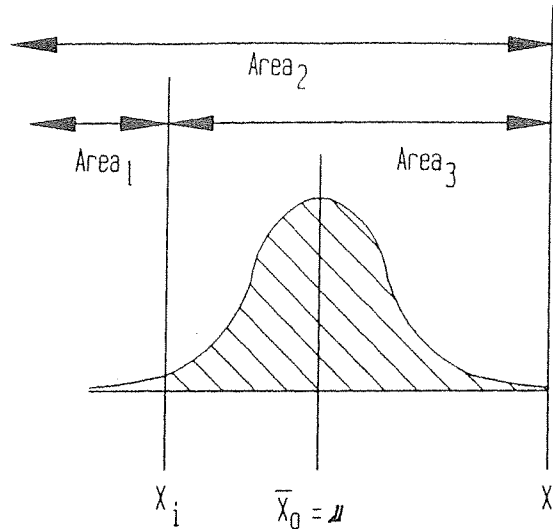
$$z_2 = +3.00$$

$$Area_2 = 0.99865$$

$$Area_3 = Area_2 - Area_1$$

$$Area_3 = 0.99865 - 0.0228$$

$$Area_3 = 0.9759 \text{ or } 97.59\%$$



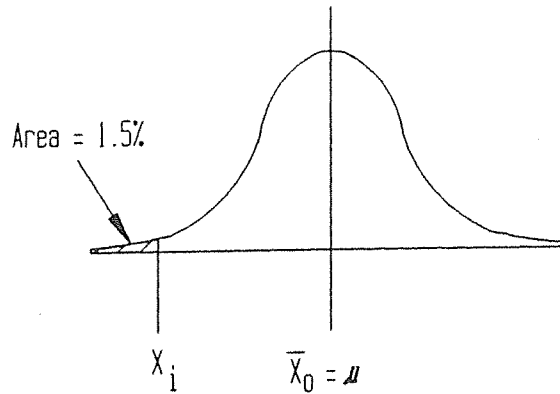
47. From Table A

For 1.5%,  $z_1 = -2.17$

$$z_1 = \frac{x_i - \mu}{\sigma}$$

$$-2.17 = \frac{0.567 - \bar{x}_0}{0.018}$$

$$\bar{x}_0 = .606 \text{ g}$$

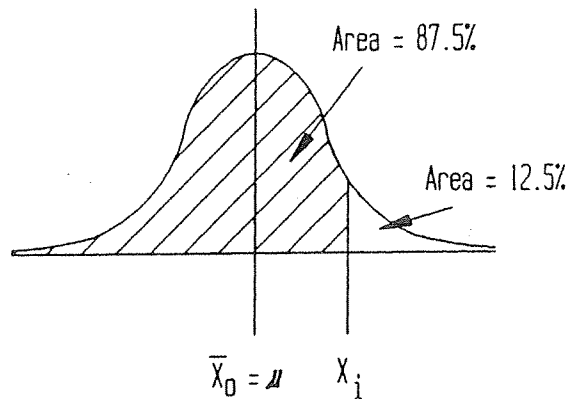


48. If rework % is 12.5%, Area to the left is 87.5% and has a Z value of +1.15.

$$z_1 = \frac{x_i - \mu}{\sigma}$$

$$1.15 = \frac{25.38 - \bar{x}_0}{0.01}$$

$$\bar{x}_0 = 25.37 \text{ mm}$$



49a Not normal

49b Normal

49c Not normal

49d Not normal, but symmetrical

49e Not normal, but symmetrical

49f Not normal, but symmetrical