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(a) First, from a free-body diagram of the entire frame, the equations of equilibrium give

$$\rightarrow \Sigma F_x = 0: \quad D_x - 400 = 0$$

$$\uparrow \Sigma F_y = 0: \quad A + D_y - 1000 = 0$$

$$\circlearrowleft \Sigma M_D = 0: \quad 8(400) + 2(1000) - 10A = 0$$

$$A = 520 \text{ lb}$$

$$D_x = 400 \text{ lb} \quad D_y = 480 \text{ lb}$$

Next, from a free-body diagram of bar $ABCD$, the equations of equilibrium give

$$\rightarrow \Sigma F_x = 0: \quad (400) - B_x + F_{CE} \cos \theta = 0$$

$$\uparrow \Sigma F_y = 0: \quad (520) + B_y - F_{CE} \sin \theta + 480 = 0$$

$$\circlearrowleft \Sigma M_B = 0: \quad 8(480) - 2(520) - 6(F_{CE} \sin \theta) = 0$$

$$\sin \theta = 4/5 \quad \cos \theta = 3/5$$

$$F_{CE} = 583.333 \text{ lb}$$

$$B_x = 750 \text{ lb} \quad B_y = -533.333 \text{ lb}$$

Next, from a free-body diagram of the lower end of bar BEF , the equations of equilibrium give

$$\Sigma F_x = 0: \quad P_a + 750 \cos \theta + 533.333 \sin \theta = 0$$

$$\Sigma F_y = 0: \quad V_a - 750 \sin \theta + 533.333 \cos \theta = 0$$

$$\circlearrowleft \Sigma M_B = 0: \quad M_a + 2.5(750 \sin \theta) - 2.5(533.333 \cos \theta) = 0$$

$$P_a = -876.667 \text{ lb} \cong 877 \text{ lb (C)} \quad \text{Ans.}$$

$$V_a = 280 \text{ lb} \quad \text{Ans.}$$

$$M_a = -700 \text{ lb} \cdot \text{ft} \quad \text{Ans.}$$

(b) Finally, from a free-body diagram of the left end of bar $ABCD$, the equations of equilibrium give

$$\Sigma F_x = 0: \quad P_b - 750 = 0$$

$$\Sigma F_y = 0: \quad V_b + 520 - 533.333 = 0$$

$$\circlearrowleft \Sigma M_B = 0: \quad M_b + 3(533.333) - 5(520) = 0$$

$$P_b = 750 \text{ lb (T)} \quad \text{Ans.}$$

$$V_b = 13.33 \text{ lb} \quad \text{Ans.}$$

$$M_b = 1000 \text{ lb} \cdot \text{ft} \quad \text{Ans.}$$

