#### Solutions to Practice Problems in the Text

#### **Chapter One: Fundamentals of Mathematical Modeling**

#### Practice Set 1-2

d = rt1. 125 = 50t[Divide both sides by 50.] t = 2.5 hours 2. d = rt170 = r(2.5)[Divide both sides by 2.5.] 68 mph = r3. I = PrtI = (\$5000)(0.05)(2) = \$5004. I = Prt616 = (2800)r(4)616 = 11200r0.055 = r5.  $A = \pi r^2$  $A = \pi(3)^2 = (3.14)(9) = 28.26 \text{ in}^2$ 6.  $A = \pi r^2$  $12.56 = (3.14)r^2$  $4 = r^{2}$  $\sqrt{4} = 2$  ft = r 7.  $A = \frac{1}{2}bh$  $36 = \frac{1}{2}(8)h$ 36 = 4h9 in = h8.  $A = \frac{1}{2}bh$  $150 = \frac{1}{2}b(40)$ 150 = 20b7.5 cm = b9.  $A = \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{15(15-5)(15-12)(15-13)} =$  $\sqrt{15(10)(3)(2)} = \sqrt{900} = 30 \text{ in}^2$ 10.  $A = \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{6(6-3)(6-4)(6-5)} =$  $\sqrt{6(3)(2)(1)} = \sqrt{36} = 6 \text{ in}^2$ 

# INSTRUCTO<sup>423</sup> USE ONLY

11. 
$$C = \frac{5}{9}(F - 32) = \frac{5}{9}(68 - 32) = \frac{5}{9}(36) = 20^{\circ} C$$
  
12.  $C = \frac{5}{9}(F - 32) = \frac{5}{9}(-4 - 32) = \frac{5}{9}(-36) = -20^{\circ} C$   
13.  $F = \frac{9}{5}C + 32 = \frac{9}{5}(-10) + 32 = -18 + 32 = 14^{\circ} F$   
14.  $F = \frac{9}{5}C + 32 = \frac{9}{5}(100) + 32 = 180 + 32 = 212^{\circ} F$   
15.  $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - (-4)}{-1 - 2} = \frac{-3 + 4}{-1 - 2} = \frac{1}{-3} = -\frac{1}{3}$   
16.  $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 0}{-3 - (-1)} = \frac{-2}{-3 + 1} = \frac{-2}{-2} = 1$   
17.  $z = \frac{x - \bar{x}}{s} = \frac{95 - 100}{15} = \frac{-5}{15} = -\frac{1}{3}$   
18.  $z = \frac{x - \bar{x}}{s} = \frac{25.2 - 17.3}{7.9} = \frac{7.9}{7.9} = 1$   
19.  $a^2 + b^2 = c^2$   
 $3^2 + 4^2 = c^2$   
 $9 + 16 = c^2$   
 $25 = c^2$   
 $\sqrt{25} = 5 = c$   
20.  $a^2 + b^2 = c^2$   
 $12^2 + 5^2 = c^2$   
 $144 + 25 = c^2$   
 $169 = c^2$   
**INSTRUCTO**<sup>42</sup>**RUSE ONLY**

 $\sqrt{169} = 13 = c$ 

21. 
$$M = P\left(1 + \frac{r}{n}\right)^{nt} = 5000\left(1 + \frac{0.045}{12}\right)^{12*10} = 5000\left(1 + \frac{0.045}{12}\right)^{120} = \$7834.96$$

22. 
$$M = P\left(1 + \frac{r}{n}\right)^{nt} = 12,000\left(1 + \frac{0.0325}{12}\right)^{12^{*5}} = 12,000\left(1 + \frac{0.0325}{12}\right)^{60} = \$14,114.28$$

23. 
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-5 \pm \sqrt{(5)^2 - 4(1)(-6)}}{2(1)} = \frac{-5 \pm \sqrt{25 + 24}}{2} = \frac{-5 \pm \sqrt{25 + 24}}{2} = \frac{-5 \pm \sqrt{49}}{2} = \frac{-5 \pm \sqrt{49}}{2} = \frac{-5 \pm \sqrt{49}}{2} = \frac{-12}{2} = -6$$
24. 
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-9) \pm \sqrt{(-9)^2 - 4(2)(-5)}}{2(2)} = \frac{9 \pm \sqrt{81 + 40}}{4} = \frac{-9 \pm \sqrt{121}}{4} = \frac{9 \pm \sqrt{121}}{4} = \frac{9 \pm \sqrt{121}}{4} = \frac{9 \pm \sqrt{121}}{4} = \frac{9 \pm \sqrt{121}}{4} = \frac{-2}{4} = -0.5$$

25. 
$$y = Ae^{rn} = 1,500,000e^{0.055*7} = 1,500,000e^{0.385} = 2,204,421$$
 bacteria

26.  $y = Ae^{rn} = 45,000e^{0.015*10} = 45,000e^{0.15} = 52,282.5 = 52,283$  people

27. I = Prt  $\frac{I}{Pt} = \frac{Prt}{Pt}$  [Divide both sides by Pt.]  $\frac{I}{Pt} = r$ 

28. V = lwh $\frac{V}{lh} = \frac{lwh}{lh}$  [Divide both sides by *lh*.]

INSTRUCTOR USE ONLY

 $\frac{V}{lh} = w$ 

- 29.  $A = \frac{1}{2}bh$  2A = bh [Multiply both sides by 2.]  $\frac{2A}{h} = b$  [Divide both sides by h to solve for b.]
- 30.  $V = \frac{1}{3}Bh$  3V = Bh [Multiply both sides by 3.]  $\frac{3V}{B} = h$  [Divide both sides by *B* to solve for *h*.]

31. 
$$P = 2L + 2W$$

$$P - 2W = 2L + 2W - 2W$$
[Subtract 2W from both sides.]
$$P - 2W = 2L$$

$$\frac{P - 2W}{2} = L$$
[Divide both sides by 2.]

32. 
$$P = 2L + 2W$$

$$P - 2L = 2L + 2W - 2L$$
[Subtract 2L from both sides.]
$$P - 2L = 2W$$

$$\frac{P - 2L}{2} = W$$
[Divide both sides by 2.]

33. 
$$A = \frac{1}{2}(B + b)h$$
  

$$2(A) = 2[\frac{1}{2}(B + b)h]$$
 [Multiply both sides by 2.]  

$$2A = (B + b)h$$
  

$$2A = Bh + bh$$
 [Use the Distributive Property.]  

$$2A - bh = Bh + bh - bh$$
 [Subtract *bh* from both sides.]

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$$\frac{2A - bh}{h} = B$$
[Divide both sides by *h* to solve for *B*.]

34. 
$$A = \frac{1}{2}(B + b)h$$
  

$$2(A) = 2[\frac{1}{2}(B + b)h]$$
 [Multiply both sides by 2.]  

$$2A = (B + b)h$$
  

$$\frac{2A}{B + b} = h$$
 [Divide both sides by  $(B + b)$  to solve for  $h$ .]

35. 
$$2x + 3y = 6$$
  

$$2x + 3y - 2x = 6 - 2x$$
 [Subtract 2x from both sides.]  

$$3y = 6 - 2x$$
  

$$y = 2 - \frac{2}{3}x$$
 [Divide both sides by 3 to solve for y.]

36. 
$$2x - y = 10$$
  

$$2x - y - 2x = 10 - 2x$$
 [Subtract 2x from both sides.]  

$$-y = 10 - 2x$$
  

$$y = -10 + 2x$$
 [Divide both sides by -1.]

37. 
$$A = \frac{x+y}{2}$$
  

$$2A = x + y$$
 [Multiply both sides by 2.]  

$$2A - y = x + y - y$$
 [Subtract y from both sides.]  

$$2A - y = x$$

38. 
$$A = \frac{x+y}{2}$$
  
 $2A = x+y$  [Multiply both sides by 2.]  
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$$2A - x = x + y - x$$
$$2A - x = y$$

[Subtract *x* from both sides.]

39.

$$5F = 9C + 160$$
  

$$5F - 160 = 9C + 160 - 160$$
  

$$5F - 160 = 9C$$
  

$$\frac{5}{9}F - \frac{160}{9} = C$$
  

$$\frac{5}{9}(F - 32) = C$$

 $F = \frac{9}{5}C + 32$ 

[Multiply through by 5.] [Subtract 160 from both sides.]

[Divide both sides by 9.]

$$\frac{5}{9}(F-32)=C$$

 $C = \frac{5}{-1}(F - 32)$ 

[Factor out 
$$\frac{5}{9}$$
.]

40.

$$C = \frac{5}{9}F - \frac{160}{9}$$

$$C + \frac{160}{9} = \frac{5}{9}F - \frac{160}{9} + \frac{160}{9}$$

$$C + \frac{160}{9} = \frac{5}{9}F$$

$$\frac{9}{5}C + 32 = F$$

[Use the distributive property.]

[Add 
$$\frac{160}{9}$$
 to both sides.]

[Multiply through by  $\frac{9}{5}$ .]

41. BMI = 
$$\frac{W}{H^2} \cdot 703 = \frac{140}{73^2} \cdot 703 = 18.4687... = 18.5$$
, Normal

42. BMI = 
$$\frac{W}{H^2} \cdot 703 = \frac{160}{60^2} \cdot 703 = 31.2444... = 31.2$$
, Obese

#### **Practice Set 1-3**

1.  $\frac{45\min}{2hr} = \frac{45\min}{120\min} = \frac{3}{8}$ 

**INSTRUCTOR USE ONLY** 

2.	$\frac{1hr}{35\min} = \frac{60\min}{35\min} = \frac{12}{7}$
3.	$\frac{4 in}{4 ft} = \frac{4 in}{48 in} = \frac{1}{12}$
4.	$\frac{3 ft}{60 in} = \frac{36 in}{60 in} = \frac{3}{5}$
5.	$\frac{6 ft}{3 yd} = \frac{6 ft}{9 ft} = \frac{2}{3}$
6.	$\frac{2 \ yd}{12 \ ft} = \frac{6 \ ft}{12 \ ft} = \frac{1}{2}$
7.	$\frac{8 weeks}{16 days} = \frac{56 days}{16 days} = \frac{7}{2}$
8.	$\frac{5  days}{1  week} = \frac{5  days}{7  days} = \frac{5}{7}$
9.	$\frac{25 \ mL}{1 \ L} = \frac{25 \ mL}{1000 \ mL} = \frac{1}{40}$
10.	$\frac{2400 \ mL}{2 \ L} = \frac{2400 \ mL}{2000 \ mL} = \frac{6}{5}$
11.	$\frac{304miles}{9.5gal} = 32\text{mi./gal.}$
12.	$\frac{450miles}{20gal} = 22.5\mathrm{mi./gal.}$
13.	$\frac{\$3.50}{10\min} = \$0.35/\min.$
14.	$\frac{\$86.40}{720kWh}$ = \\$0.12/kWh
15.	$\frac{\$48}{10  days} = \$4.80/day$
16.	$\frac{\$340}{40hr}$ = \\$8.50 / hr
	2411

17.  $\frac{24lb}{15 \, people} = 1.6 \, \text{lb./person}$ 

INSTRUCTOR<sup>429</sup> USE ONLY

18. $\frac{5.5 lb}{12 \ people} = 0.458\overline{3} \ lb./person$	
19. $\frac{x}{5} = \frac{3}{4}$ 4x = (3)(5) 4x = 15 $x = \frac{15}{4}$	[cross-multiplication property]
20. $\frac{9}{2x} = \frac{6}{4}$ (4)(9) = (2x)(6) 36 = 12x 3 = x	[cross-multiplication property]
21. $\frac{30}{126} = \frac{5}{3x}$ (3x)(30) = 5(126) 90x = 630 x = 7	[cross-multiplication property]
22. $\frac{2x}{7} = \frac{8}{14}$ (2x)(14) = (7)(8) 28x = 56 x = 2	[cross-multiplication property]
23. $\frac{3x+6}{35} = \frac{2x-18}{5}$ $5(3x+6) = 35(2x-18)$ $15x+30 = 70x-630$ $15x+30-70x = 70x-630-70x$ $-55x+30 = -630$ $-55x+30 = -630 - 30$ $-55x = -660$ $x = 12$	[cross-multiplication property] [distributive property]
24. $\frac{x-2}{7} = \frac{2x+2}{28}$ $28(x-2) = 7(2x+2)$ $28x - 56 = 14x + 14$ $28x - 56 - 14x = 14x + 14 - 14x$ $14x - 56 = 14$ $14x - 56 + 56 = 14 + 56$	[cross-multiplication property] [distributive property]
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[cross-multiplication property]

[cross-multiplication property]

[distributive property]

[distributive property]

 $\begin{array}{c} 14x=70\\ x=5 \end{array}$ 

25.	$\frac{15}{x-1} = \frac{x-1}{x-1}$
	18 x
	(15)(x) = 18(x - 1)
	15x = 18x - 18
	15x - 18x = 18x - 18 - 18x
	-3x = -18
	x = 6

26.  $\frac{3}{x+4} = \frac{5}{2x+3}$  3(2x+3) = 5(x+4) 6x+9 = 5x+20 6x+9-5x = 5x+20-5x x+9 = 20 x+9-9 = 20-9 x = 11

27. 
$$\frac{3}{x+1} = \frac{18}{9x-3}$$

$$3(9x-3) = 18(x+1)$$

$$27x - 9 = 18x + 18$$

$$9x - 9 = 18x + 18 - 18x$$

$$9x - 9 = 18$$

$$9x - 9 = 18 + 9$$

$$9x = 27$$

$$x = 3$$
28. 
$$\frac{x+8}{6} = \frac{2x-8}{3}$$

$$3(x+8) = 6(2x-8)$$

$$3x + 24 = 12x - 48$$

$$3x + 24 = 12x - 48 - 12x$$

$$-9x + 24 = -48$$

$$-9x + 24 = -48 - 24$$

$$-9x = -72$$

$$x = 8$$
29. Unit rate equals cost divided by the number of square feet.

 $2235 \div 1500 \text{ ft}^2 = \$1.49/\text{ft}^2$ 

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- 30. Unit rate equals cost divided by the number of yards.  $$47.80 \div 4 \text{ yd} = $11.95/\text{yd}$
- 31. Cost per ounce =  $\$8.99 \div 16 \text{ oz} = \$0.561875 \text{ per ounce}$

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**USE ONLY** 

- 32. Cost per can =  $7.14 \div 6$  cans = 1.19 per can
- 33. Brand X: \$1.49 ÷ 8 oz = \$0.18625/ ounce
  Brand Z: \$2.12 ÷ 12 oz = \$0.1766.../ounce
  Brand Z is the better buy because it costs less per ounce.
- 34. five 2-L colas: \$4.95 ÷ 5 = \$0.99/bottle three 2-L colas: \$2.99 ÷ 3 = \$0.99666../bottle Purchasing five 2-L colas for \$4.95 is a better buy.

4 cup reup	
$(1)(120) = \sqrt[3]{4x} $ [Cross multiply.]	
$120 = \frac{3}{4}x$	
160 calories = x [Multiply both sides by	4/3.]

36. Let 
$$\frac{8 oz}{90 cal} = \frac{28 oz}{x}$$
.  

$$8x = (90)(28)$$
 [Cross multiply.]  

$$8x = 2520$$
  

$$x = 315$$
 calories

37. Let 
$$\frac{2.5 \, dozen}{1.25 \, cups} = \frac{x \, dozen}{3 \, cups}.$$
(3)(2.5) = 1.25x
(3)(2.5) = 1.25x
(7.5 = 1.25x
6 = x
Answer is 6 dozen or 72 muffins.

38. If each of 30 students has 2 cookies, then 60 cookies are needed.  $60 \div 12 = 5$  doz.

Let  $\frac{3 \text{ dozen}}{2.5 \text{ cups}} = \frac{5 \text{ dozen}}{x}$  3x = (5)(2.5) 3x = 12.5  $x = 4.16666... = 4\frac{1}{6} \text{ cups}$ [Cross multiply.]

39. Let  $\frac{5 \text{ ft 4 in}}{10.5 \text{ ft}} = \frac{x}{20 \text{ ft}}$ . Convert the measurements to inches as follows: 5 ft 4 in = 5(12)

+ 4 = 64 inches; 10.5 ft =  $10.5 \times 12$  in = 126 inches; 20 ft =  $20 \times 12$  in = 240 inches. Now substitute:

$$\frac{64 \ in}{126 \ in} = \frac{x}{240 \ in}$$
(64)(240) = 126x

INSTRUCTOR USE ONLY

15360 = 126x121.9 inches = x Converting to feet and inches: 121.9 inches  $\div 12$ in/ft = 10 ft. 1.9 in. 40. Let  $\frac{5 ft 10 in}{8 ft 9 in} = \frac{x}{14 ft}$ . Convert the measurements to inches as follows: 5 ft 10 in = 5(12) +10 = 70 inches, 8 ft 9 in = 8(12) + 9 = 105 inches, and 14 ft = 14(12) = 168 inches. Now substitute:  $\frac{70 \text{ in}}{x} = \frac{x}{x}$  $105 in^{-168}$  in (70)(168) = 105x[Cross multiply.] 11760 = 105x112 inches = x(112 inches = 9 feet 4 inches)41. Let  $\frac{1.8A}{18V} = \frac{5.4A}{x}$ . (18)(5.4) = 1.8A[Cross multiply.] 97.2 = 1.8A54 V = A42. Let  $\frac{10A}{50V} = \frac{25A}{x}$ [Cross multiply.] 10x = (25)(50)10x = 1250x = 125 V43. Let  $\frac{110 lb}{19.4 lb} = \frac{200 lb}{x}$ 110x = (19.4)(200)[Cross multiply.] 110x = 3880x = 35.2727... or approximately 35.3 lb. 44. Let  $\frac{110 lb}{19.4 lb} = \frac{155 lb}{x}$ 110x = (19.4)(155)[Cross multiply.] 110x = 3007x = 27.336363... or approximately 27.3 lb. 45. Let  $\frac{10lb}{400 ft^2} = \frac{x}{500 ft^2}$ (10)(500) = 400x[Cross multiply.] 5000 = 400xINSTRUCTO<sup>43</sup> USE ONLY

[2 gallons = 256 oz.]

[Cross multiply.]

[Cross multiply.]

12.5 lb = x 46. Let  $\frac{20}{1} = \frac{256 oz}{x}$ 

20x = (256)(1) 20x = 256 x = 12.8 oz.  $47. \text{ Let } \frac{\$240}{1200 \text{ words}} = \frac{x}{1500 \text{ words}} \cdot (240)(1500) = 1200x$  360,000 = 1200x \$300 = x

48. Let  $\frac{1500 \text{ doughnuts}}{9 \text{ hours}} = \frac{300 \text{ doughnuts}}{x}$  1500x = (9)(300) [Cross multiply.] 1500x = 2700x = 1.8 hr.

49. Let  $\frac{1 \text{ adult}}{15 \text{ children}} = \frac{3 \text{ adults}}{x}$  x = (3)(15) [Cross multiply.] x = 45 children

50. Let  $\frac{1 \text{ adult}}{6 \text{ infants}} = \frac{x}{15 \text{ infants}}$  15 = 6x [Cross multiply.] 2.5 adults = x Therefore, 3 adults are needed for 15 infants.

51. Let  $\frac{1 \text{ inch}}{8 \text{ feet}} = \frac{2.75 \text{ inches}}{x}$  x = (8)(2.75) x = 22 feet[Cross multiply.] x = 22 feetLet  $\frac{1 \text{ inch}}{8 \text{ feet}} = \frac{1.9375 \text{ inches}}{x}$  x = (8)(1.9375) x = 15.5 feetDimensions are 22 ft × 15.5 ft

**INSTRUCTOR USE ONLY** 

52.	Let $\frac{1 \text{ inch}}{10 \text{ miles}} = \frac{x}{185 \text{ miles}}$ $(1)(185) = 10x$ $18.5 \text{ in} = x$	[Cross multiply.]
53.	Let $\frac{Mach1}{761.2 mph} = \frac{Mach3.1}{x}$ 1x = (3.1)(761.2) x = 2359.72 mph	[Cross multiply.]
54.	Let $\frac{Mach1}{761.2 mph} = \frac{x}{1903 mph}$ 761.2x = (1)(1903) x = 2.5 (Mach 2.5)	[Cross multiply.]
55.	Let $\frac{400 ft}{1 day} = \frac{1000 ft}{x}$ (1)(1000) = 400x 1000 = 400x 2.5 days = x	[Cross multiply.]
56.	Let $\frac{8 \text{ sq} / \text{day}}{1 \text{ roofer}} = \frac{x}{2 \text{ roofers}}$ (2)(8 sq/day) = x 16 sq/day = x Since 2 roofers can do 16 squares per d	[Cross multiply.] ay, they can do 32 squares in 2 days.
57.	Let $\frac{40 mg}{1 mL} = \frac{60 mg}{x}$ . $40x = (1)(60)$ $40x = 60$ $x = 1.5 mL$	[Cross multiply.]
58.	Let $\frac{100 mg}{1 kg} = \frac{x}{9.3 kg}$ . (100)(9.3) = 1x 930 mg = x	[Cross multiply.]
59.	Let $\frac{1.8  mi}{30  \min} = \frac{x}{45  \min}$ $(1.8)(45) = 30x$ $81 = 30x$ $2.7  \text{miles} = x$	[Cross multiply.]
IN	STRUCTO	<sup>435</sup> USE ONI

60. Let  $\frac{1mph}{1.609 kph} = \frac{x}{98 kph}$ (1)(98) = 1.609x 98 = 1.609x 60.9 mph = x

#### Practice Set 1-.4

- 1. 2x + 6
- 2. 2x 3
- 3. 7x 2
- 4. 3 + 4x
- 5. 3(4 + x)
- 6. 2(x-6)
- 7.  $\frac{1}{3}x-5$
- 8.  $x \frac{3}{4}x$
- 9. Let Bill's salary = x. Then, Ann's salary = x + \$5000
- 10. Let Monday's attendance = x. Then, Friday's is  $\frac{1}{2}x + 3$
- 11. Let the width = x. Then, the length = 2x + 5.
- 12. Let the short rod = x. Then, each subsequent rod is 1 inch longer: x + 1 and x + 2.
- 13. 5x + 5 = 2x 10 5x + 5 - 2x = 2x - 10 - 2x 3x + 5 = -10 3x + 5 - 5 = -10 - 5 3x = -15x = -5
- 14. 8x 16 = 808x - 16 + 16 = 80 + 168x = 96x = 12
- 15. Emily has saved x. Elena has saved 2x (twice as much).
  - x + 2x = 72
    - 3x = 72
      - x = 24 so Emily has saved \$24 and Elena has saved 2(\$24) = \$48.

INSTRUCTOR USE ONLY

16. Let the lower grade = x. The higher grade is x + 56. x + (x + 56) = 128 2x + 56 = 128 2x + 56 - 56 = 128 - 56 2x = 72x = 36 so the lower grade is 36 and the higher is 36 + 56 = 92.

17. Let x = the shorter piece. The longer piece will be 2x. x + 2x = 60 meters 3x = 60 meters x = 20 meters The shorter piece is 20 meters long and the longer piece is 2(20) = 40 meters long.

- 18. Let Joshua's age = x and Mario's age be x + 18.
  - x + (x + 18) = 46 2x + 18 = 46 2x + 18 - 18 = 46 - 18 2x = 28x = 14

So, Joshua is 14 years old and Mario is 14 + 18 = 32 years old.

19. Using the definition of an average, let x equal the missing grade.

$$\frac{88+91+95+x}{4} = 90$$

$$88+91+95+x = 4(90)$$

$$274+x = 360$$

$$274-274+x = 360-274$$

$$x = 86$$

In order to have a 90 average, she must make 86 on the last test.

20. Using the definition of an average, let *x* equal the missing grade.

$$\frac{60+92+78+89+x}{5} = 84$$

$$60+92+78+89+x = 5(84)$$

$$319+x = 420$$

$$319-319+x = 420-319$$

$$x = 101$$

In order to have a B average, she must make 101 on the last test. On a normal grading scale, this will be impossible.

21. Let x = the number of kilowatt-hours. Write the equation and solve. \$20.00 + \$0.14x = \$85.78 20.00 - 20.00 + 0.14x = 85.78 - 20.000.14x = 65.78

# INSTRUCTOR USE ONLY

 $x = \frac{65.78}{0.14} = 470 \, kWh$  (rounded)

22. Let x = number of "out of area" minutes.

\$29.95 + \$9.95 + \$0.40x = \$69.90 39.90 + 0.40x = 69.90 39.90 - 39.90 + 0.40x = 69.90 - 39.90 0.40x = 30 x = 75She was charged for 75 "out of area" minutes.

23. Let x = the taxi fare. Since 1/11 of a mile costs \$0.20, the cost of one mile =  $0.20 \times 11 = 2.20$ .

x = \$3.20 + 18(\$2.20/mile) + \$1.20 = \$44.00

24. Let x = the taxi fare. Since 1/5 of a mile costs \$0.40, the cost of one mile =  $0.40 \times 5 = 2.00$ .

$$x = $2.50 + 16($2.00/mile) = $34.50$$

25. The opponent scored x points in the game. Mighty Mites scored 39 points. This amount (39) is 2x - 1.

$$2x - 1 = 39$$
  

$$2x - 1 + 1 = 39 + 1$$
  

$$2x = 40$$
  

$$x = 20$$

The opponent scored 20 points.

26. Let the number of games Jim won = x and the number that Gaylord won = x + 99.

$$x + (x + 99) = 529$$
  

$$2x + 99 = 529$$
  

$$2x + 99 - 99 = 529 - 99$$
  

$$2x = 430$$
  

$$x = 215$$

Jim won 215 games and Gaylord won 215 + 99 = 314 games.

27. Let the integers be x, x + 1 and x + 2. Write the equation for the sum and solve. x + (x + 1) + (x + 2) = 87 3x + 3 = 87 3x + 3 - 3 = 87 - 3

> x = 28The integers are x = 28, x + 1 = 29 and x + 2 = 30.

3x = 84

**INSTRUCT**<sup>438</sup>

28. Let the integers be x, x + 1 and x + 2. Write the equation for the sum and solve. x + (x + 1) + (x + 2) = 100

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$$3x + 3 = 100$$
  

$$3x + 3 - 3 = 100 - 3$$
  

$$3x = 97$$
  

$$x = 32.333...$$

Since this number is not an integer, there is not a set of consecutive integers that satisfies the requirements of this problem.

29. Let the odd integers be x, x + 2, and x + 4. Write the equation for the sum and solve. x + (x + 2) + (x + 4) = -273

$$3x + 6 = -273$$
  

$$3x + 6 - 6 = -273 - 6$$
  

$$3x = -279$$
  

$$x = -93$$
  
The three integers are x = -93, x + 2 = -91, and x + 4 = -89

30. Let the odd integers be x, x + 2, and x + 4. Write the equation for the sum and solve. x + (x + 2) + (x + 4) = 1503 3x + 6 = 1503 3x + 6 - 6 = 1503 - 6 3x = 1497x = 499

The three integers are x = 499, x + 2 = 501, and x + 4 = 503.

31. Let x = the value of the lot. Then, 6.5x = the value of the house.

x + 6.5x = \$175,0007.5x = \$175,000 x = \$23,333.33

So, the lot is worth approximately \$23,333 and the house is worth about \$151,667.

32. Let x = the value of the lot. Then, 7x = the value of the house. x + 7x = \$164,000 8x = \$164,000x = \$20,500

So, the lot is worth approximately \$22,500 and the house is worth about \$143,500.

33.  $x = \frac{949 \text{ yen}}{146 \text{ yen} / \text{ dollar}} = $6.50.$ 

34.  $x = \frac{65 \text{ pounds}}{0.549 \text{ pounds / dollar}} = $118.40$ 

35.  $time = \frac{distance}{speed} = \frac{500mi}{170.265mi/hr} = 2.936598831hr = about 2 hr 56 min$ 

INSTRUCTOR USE ONLY

- 36. x = 500 miles  $\div$  74.602 mph = 6.702 hours. Convert 0.702 to minutes by multiplying 0.702(60) = 42.12 to give the answer of approximately 3 hours and 42 minutes.
- 37. Let the number of males and females at the beginning of the semester = x.If 8 males drop the class, there are x 8 males remaining. Now the number of females is twice the number of males remaining.

$$x = 2(x - 8)$$
  

$$x = 2x - 16$$
  

$$x - 2x = 2x - 16 - 2x$$
  

$$-x = -16$$
  

$$x = 16$$

There were 16 males and 16 females at the beginning of the semester.

38. Let x = the number of Democrats and the number of Republicans in the Senate.

$$x + x + 2 = 100$$
  

$$2x + 2 = 100$$
  

$$2x + 2 - 2 = 100 - 2$$
  

$$2x = 98$$
  

$$x = 49$$

There were 49 Democrats and 49 Republicans in the Senate.

39. Let x = the number of bags of apples. 5x + 2x = 252

$$-2x = 252$$
  
 $7x = 252$   
 $x = 36$ 

There are 36 bags containing 5 lb. of apples and 36 bags containing 2 lb. of apples.

40. Let x = the number of seats in Theater B, x + 150 = the number of seats in Theater A. (x + 150) + x + 270 = 800 2x + 420 = 800 2x + 420 - 420 = 800 - 420 2x = 380 x = 190

The number of seats in Theater A is x + 150 = 190 + 150 = 340.

41. Let x = profit from the automotive division. Then x - 273 represents the profit from financial services.

x + (x - 273 million) = 483 million2x - 273 million = 483 million2x - 273 million + 273 million = 483 million + 273 million2x = 756 millionx = 378 million

The profit from the automotive division was 378 million and from financial services

INSTRUCTOR USE ONLY

was 378 million - 273 million = 105 million.

42. Let x = salary of Palmisano and x - 3.91 million = Moonvie's salary.x + x - 3.91 million = 56.73 million 2x - 3.91 million + 3.91 million = 56.73 million + 3.91 million 2x = 60.64 million x = 30.32 million Therefore, Palmisano made 30.32 million and Moonvie made 26.41 million in 2010.

43. Let x = attendance at the Ohio State game and x - 1044 = attendance at the Penn State game. Total attendance for the two teams in 2010 was 209,512.

x + x - 1044 = 209,512 2x - 1044 = 209,512 2x - 1044 + 1044 = 209,512 + 1044 2x = 210,556x = 105,278

Therefore, the attendance at the Ohio State game was 105,278 and the attendance at the Penn State game was 105,278 - 1044 = 104,234.

44. Let x = the middle-sized piece. The longest is 3x and the shortest is 3x - 23. The total length of the pipe is 40 inches. Therefore,

$$3x + x + 3x - 23 = 40$$
  

$$7x - 23 = 40$$
  

$$7x - 23 + 23 = 40 + 23$$
  

$$7x = 63$$
  

$$x = 9$$

Therefore, the middle sized piece is 9 in., the longest is 3(9) = 27 in. and the shortest is 3x - 23 = 3(9) - 23 = 4 in.

45. Let x = the original price of the radio. Savings = 15% of retail price or 0.15x. x - 0.15x = \$127.46 0.85x = \$127.46x = \$149.95

The original price of the radio was \$149.95.

46. Let x = the original price of the watch. Savings = 25% of retail price or 0.25x. x - 0.25x = \$168.75 0.75x = \$168.75x = \$225

The original price of the watch was \$225.00.

47. Let x = the wholesale price of the shoes. The markup amount is 65% times x. x + 0.65x = \$125.40

$$x = 0.03x = $125.40$$
  
 $1.65x = $125.40$   
 $x = $76$ 

The wholesale price of the shoes was \$76.00.

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48. Let x = the wholesale price of the shoes. The markup amount is 40% times x.

$$0.40x = \$63$$
  
 $1.4x = \$63$   
 $x = \$45$ 

The wholesale price of the shoes was \$45.00.

 $\mathbf{X}$  +

49. Let x = Drema's contributions. The company's contributions = 20% of x. x + 0.20x = \$1200 1.2x = \$1200x = \$1000

Drema deposited \$1000 into the account.

50. Let x = the population four years ago. The growth of the population is 5% of x. x + 0.05x = 882

$$+ 0.05x = 882$$
  
 $1.05x = 882$   
 $x = 840$ 

There were 840 people in the town four years ago.

51. BMI = 
$$\frac{W}{H^2} \cdot 703 = \frac{120}{60^2} \cdot 703 = 23.4333... = 23.4$$
, Normal

52. BMI = 
$$\frac{W}{H^2} \cdot 703 = \frac{195}{67^2} \cdot 703 = 30.53798... = 30.5$$
, Obese

#### **Chapter 1 Review Problems**

- 1.. I = Prt $t = \frac{I}{Pr}$  [Divide both sides by Pr.]
- 2. 2x + 3y = 9 3y = -2x + 9 [Subtract 2x from both sides.]  $y = -\frac{2}{3}x + 3$  [Divide all terms by 3.]
- 3.  $C = \pi d$  $d = \frac{C}{\pi}$  [Divide both sides by  $\pi$ .]
- 4. a+b+c=Pc=P-a-b

[Subtract *a* and *b* from both sides.]

5.  $\frac{27 \min}{3 hr} = \frac{27 \min}{180 \min} = \frac{3}{20}$ 

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- 6.  $\frac{4 \text{ weeks}}{21 \text{ days}} = \frac{28 \text{ days}}{21 \text{ days}} = \frac{4}{3}$
- 7.  $\frac{6 in}{5 ft} = \frac{6 in}{60 in} = \frac{1}{10}$

8. 
$$\frac{\$60}{5 hr} = \$12/\text{hour}$$

9.  $\frac{44 \text{ bushels}}{8 \text{ trees}} = 5.5 \text{ bushels/tree}$ 

10. 
$$\frac{\$12.80}{3.5 \, lb} = \$3.66/lb.$$

11.  $\frac{x}{3} = \frac{4}{7}$ 7x = 12 $x = \frac{12}{7}$ 

12. 
$$\frac{2}{3} = \frac{8}{2x}$$
$$4x = 24$$
$$x = 6$$

13. 
$$\frac{x-3}{8} = \frac{3}{4}$$
$$4x - 12 = 24$$
$$4x - 12 + 12 = 24 + 12$$
$$4x = 36$$
$$x = 9$$

14. 
$$\frac{4x-3}{7} = \frac{2x-1}{3}$$

$$12x - 9 = 14x - 7$$

$$12x - 9 - 14x = 14x - 7 - 14x$$

$$-2x - 9 + 9 = -7 + 9$$

$$-2x = 2$$

$$x = -1$$

15.  $A = \frac{1}{2}bh$ . Substitute:  $A = \frac{1}{2}(3 \text{ in})(4 \text{ in}) = 6 \text{ in}^2$ 

INSTRUCTOR USE ONLY

16. Let  $\frac{2400 L}{50 \min} = \frac{x}{30 \min}$ . Cross multiply. 72000 = 50x1440 liters = x17. Let  $\frac{3}{4} = \frac{x}{92}$ . Cross multiply. 276 = 4x69 dentists = x18. Let *x* = total number of minutes that you talk. Then, \$1.24 + (x - 4)(\$0.28) = \$3.761.24 + 0.28x - 1.12 = 3.760.12 + 0.28x = 3.760.12 + 0.28x - 0.12 = 3.76 - 0.120.28x = 3.64x = 13 The call was 13 minutes long. 19. Let x = number of minutes per month. Then, 50 + 0.36x = 99.68. 0.36x = 99.68 - 500.36x = 49.68x = 138 minutes 20. Let x = labor time (per hour). Then, \$40 + \$30x = \$11540 + 30x - 40 = 115 - 4030x = 75x = 2.5 hours 21. Let the shorter piece be x and the longer be x + 3. Then, x + (x + 3) = 332x + 3 = 332x + 3 - 3 = 33 - 32x = 30x = 15 in (short piece) and x + 3 = 15 + 3 = 18 in (long piece) 22. Let the short piece = x, the middle-sized piece = x + 14, and the long piece = 3x. Then, x + (x + 14) + 3x = 795x + 14 = 795x + 14 - 14 = 79 - 145x = 65x = 13 cm (short) x + 14 = (13) + 14 = 27 cm (middle) 3x = 3(13) = 39 cm (long) 23. Let the calculator be x and the cassette player be x + 140. Then, x + (x + 140) = 2082x + 140 = 208**USE ONLY** INSTR

2x + 140 - 140 = 208 - 1402x = 68x = \$34.00 which is the cost of the calculator

24. Let n = the number of nickels and 2n - 2 = the number of dimes. Then, n + (2n - 2) = 52. 3n - 2 = 52 3n - 2 + 2 = 52 + 2 3n = 54n = 18 There are 18 nickels and 34 dimes in the bank for a total of \$4.30.

25. Use the formula d = rt and substitute values. 182 mi = (52 mph)(t)t = 3.5 hours

- 26. T = UN + F Substitute the given values and solve. \$16,750 = \$15N + \$2500 16750 - 2500 = 15N + 2500 - 2500 14250 = 15NN = 950 units produced
- 26. First remove the parentheses by use of the distributive property, then add 2 to the 12. 2+3(2x+4) = 2+6x+12 = 6x+14.
- 28. 5x + 3 = 6x5x + 3 - 5x = 6x - 5x3 = x
- 29. for any triangle,  $A + B + C = 180^{\circ}$ Let A = the first angle The second angle, B = 3AThe third angle,  $C = \frac{2}{3}(3A) = 2A$  $A + 3A + 2A = 180^{\circ}$  $6A = 180^{\circ}$  $A = 30^{\circ}$ ,  $B = 3(30^{\circ}) = 90^{\circ}$ ,  $C = 2(30^{\circ}) = 60^{\circ}$
- 30.First convert all the measurements to the same units, like inches.<br/>5 ft 3 in = 63 in, 10 ft 6 in = 126 in, and 52 ft = 624 in<br/>Now set up a proportion like: $\frac{63in}{126in} = \frac{x}{624in}$ <br/>Cross multiply:<br/>Divide by 126in:(63in)(624in) = (126in)(x)<br/>x = 312in = 26ft

# INSTRUCTOR USE ONLY

#### **Chapter 1 Test**

- 1. V = lwh $w = \frac{V}{lh}$  [Divide both sides by *lh*.]
- 2.  $h = vt 16t^{2}$  $h + 16t^{2} = vt$  [Add  $16t^{2}$  to both sides.] $\frac{h + 16t^{2}}{t} = v$  [Divide both sides by t.]
- 3.  $\frac{4 hr}{1 day} = \frac{4 hr}{24 hr} = \frac{1}{6}$
- 4.  $\frac{10 \ ft}{160 \ in} = \frac{120 \ in}{160 \ in} = \frac{3}{4}$
- 5.  $\frac{\$413.20}{4 \ days} = \$103.30/day$
- 6.  $\frac{7.5 \ lb}{6 \ people} = 1.25 \ lb / person$
- 7.  $\frac{50 \ eggs}{10 \ chickens} = 5 \ eggs / chicken$
- 8.  $\frac{7}{12} = \frac{3x}{10}$ 70 = 36x  $\frac{70}{36} = \frac{35}{18} = x$
- 9.  $\frac{x-4}{8} = \frac{2x+3}{9}$ 9(x - 4) = 8(2x + 3) 9x - 36 = 16x + 24 9x - 36 - 16x = 16x + 24 - 16x -7x - 36 = 24 -7x - 36 + 36 = 24 + 36 -7x = 60 x = -\frac{60}{7}

# INSTRUCTOR USE ONLY

10. Let x = defective bulbs. Then,  $\frac{3}{85} = \frac{x}{510}$ . 85x = 1530x = 18 bulbs

- 11. Let x = parts produced. Then,  $\frac{300 \text{ parts}}{20 \text{ min}} = \frac{x}{45 \text{ min}}$ . 20x = 13500x = 675 parts
- 12. Given P = 2L + 2W. Substitute the given values into the formula. P = 2(20 ft.) + 2(12 ft.) = 64 ft.
- 13. Company A Plan: \$20 + 0.10m (where m = miles driven) Company B Plan: \$10 + 0.30m To find the number of miles where the two costs are equal, set these two expressions equal.

$$\$20 + 0.10m = \$10 + 0.30m$$
  
20 + 0.10m - 0.10m = 10 + 0.30m - 0.10m  
20 = 10 + 0.20m  
20 - 10 = 10 + 0.20m - 10  
10 = 0.20m  
50 = m, so at 50 miles the costs are the same for both plans

- 14. Let the number of passengers on one ship = x. The second ship holds twice as many passengers = 2xWrite the equation x + 2x = 2250 and solve. 3x = 2250x = 750 so the smaller ship holds 750 passengers
- 15. Let Sarah's age be x. Then, Michelle's age is 5x 10. Write the equation and solve. x + 5x - 10 = 44 6x - 10 = 44
  - 6x 10 = 11 6x - 10 + 10 = 44 + 10 6x = 54x = 9 so Sarah is 9 years and Michelle is 5(9)-10 = 35 years.

16. Let the short board = x and the longer one be 3x + 1. Write the equation.

 $\begin{array}{l} x + 3x + 1 = 21 \\ 4x + 1 = 21 \\ 4x + 1 - 1 = 21 - 1 \\ 4x = 20 \\ x = 5 \text{ so the short board is 5 ft. and the longer is } 3(5) + 1 = 16 \text{ ft.} \end{array}$ 

17. x + 12.3% of x is now \$2.83 per gallon x + 0.123x = \$2.83

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1.123x = \$2.83x = \$2.52 per gallon

18. P - 22% of P is now 28,000 people, after 8 years P - 0.22P = 28,000
0.78P = 28,000
P = 35,897.4359 = 35,898 whole people 8 years ago Now divide the amount of decrease in population by 8 years to get a rough average yearly decrease in population: 35,898 - 28,000 = 7898 people in 8 years 7898/8 = 987.25 or about 988 people per year decrease in population

75 + 82 + 80 + x = 336237 + x = 336x = 99 is the least the student can make an have an overall average of 84

20. Let L = lot value, H = house value = 7.5L L + 7.5L = \$152,000 8.5L = \$152,000 L = \$17,882.35294 or about \$17,882 for the lot H = 7.5L = \$134,117.6471 or about \$138,118 for the house

# INSTRUCTOR USE ONLY

#### Chapter 2

#### Practice Set 2-1

- 1. Let L = 360 ft and W = 160 ft.
  - P = 2L + 2W

P = 2(360 ft) + 2(160 ft) = 720 ft + 320 ft = 1040 ft

- 2. Let d = 8 ft
  - $C = \pi d$
  - $C = \pi(8) = (3.14159)(8) \approx 25.1 \text{ ft}$
- 3. Let L = 15 ft and W = 11 ft.

 $A = LW = (15 \text{ ft})(11 \text{ ft}) = 165 \text{ ft}^2$ 

1  $yd^2 = 9$  ft<sup>2</sup> so divide by 9 to convert to square yards.

 $165 \text{ ft}^2 \div 9 \text{ ft}^2/\text{yd}^2 = 18.3 \text{ yd}^2$ 

4. Let r = 10 ft.

 $A = \pi r^2 = \pi (10 \text{ ft})^2 \approx 314.159 \text{ ft}^2$ 

Since this is half a circle, divide this answer by 2.

314.159  $\text{ft}^2 \div 2 \approx 157.1 \text{ ft}^2$ 

- 5. A square has 4 equal sides. P = 4L = 54 in., so L = 13.5 in per side. The area of a square is given by the formula:  $A = L^2 = (13.5 \text{ in})^2 = 182.25 \text{ in}^2$ .
- $6. \quad A = lw$

```
65 \text{cm}^2 = (13 \text{cm})(\text{w})
```

5 cm = w

- P = 2l + 2w = 2(13cm) + 2(5cm) = 36cm
- 7. Use the formula for the area of a rectangle to calculate the size of the area to be planted.

 $A = lw = (8.75 \text{ ft})(4.5 \text{ ft}) = 39.375 \text{ ft}^2$ 

Since she needs four plants for every square foot, you should multiply this answer by 4. This gives 39.375 \* 4 = 157.5 plants. In a practical sense, using this answer means you should buy 158 plants. If you round the area off to 40 ft<sup>2</sup> and multiply by 4, you would get 160 plants.

8. Find the circumference of the circular walkway with a diameter = 50 ft.

 $C = \pi d$