Solutions to end-of-chapter problems

Engineering Economy, 7th edition

Chapter 2 Factors: How Time and Interest Affect Money

2.1 (1) (P/F, 6%, 8) = 0.6274(2) (A/P, 10%, 10) = 0.16275(3) (A/G, 15%, 20) = 5.3651(4) (A/F, 2%, 30) = 0.02465(5) (P/G, 35%, 15) = 7.5974**2.2** P = 21,300(P/A,10%,5)= 21,300(3.7908)= \$80,744 **2.3** Cost now = 142(0.60)= \$85.20 Present worth at regular cost = 142(P/F, 10%, 2)= 142(0.8264)= \$117.35 Present worth of savings = 117.35 - 85.20= \$32.15 **2.4** F = 100,000(F/P,10%,3) + 885,000= 100,000(1.3310) + 885,000= \$1,018,100 **2.5** F = 50,000(F/P,6%,14)= 50,000(2.2609)= \$113,045 **2.6** F = 1,900,000(F/P,15%,3)F = 1,900,000(1.5209)= \$2,889,710 **2.7** A = 220,000(A/P,10%,3)= 220,000(0.40211)= \$88,464 **2.8** P = 75,000(P/F,12%,4)= 75,000(0.6355)= \$47,663

2.9 F = 1.3(F/P, 18%, 10)= 1.3(5.2338) = 6.80394 (\$6,803,940)

 $\begin{aligned} \textbf{2.10 P} &= 200,000(P/F,15\%,1) + 300,000(P/F,15\%3) \\ &= 200,000(0.8696) + 300,000(0.6575) \\ &= \$371,170 \end{aligned}$

2.11 Gain in worth of building after repairs = (600,000/0.75 - 600,000) - 25,000 = 175,000

F = 175,000(F/P,8%,5)= 175,000(1.4693)= \$257,128

- **2.12** F = 100,000(F/P,8%,4) + 150,000(F/P,8%,3)= 100,000(1.3605) + 150,000(1.2597) = \$325,005
- **2.13** P = (110,000* 0.3)(P/A,12%,4)= (33,000)(3.0373) = \$100,231
- 2.14 P = 600,000(0.04)(P/A,10%,3)= 24,000(2.4869)= \$59,686
- **2.15** A = 950,000(A/P,6%,20) = 950,000(0.08718) = \$82,821

2.16 A = 434(A/P,8%,5) = 434(0.25046) = \$108.70

- **2.17** F = (0.18 0.04)(100)(F/A,6%,8)= 14(9.8975) = \$138.57
- **2.18** $F_{difference} = 10,500(F/P,7\%,18) 10,500(F/P,4\%,18)$ = 10,500(3.3799) - 10,500(2.2058) = \$12,328
- 2.19 F = (200 90)(F/A, 10%, 8)= 110(11.4359) = \$1,257,949

2.20 A = 350,000(A/F,10%,3) = 350,000(0.30211) = \$105,739

2.21 (a) 1. Interpolate between i = 12% and i = 14% at n = 15.

$$1/2 = x/(0.17102 - 0.14682)$$

x = 0.0121
(A/P,13%,15) = 0.14682 + 0.0121

$$= 0.15892$$

2. Interpolate between i = 25% and i = 30% at n = 10.

$$2/5 = x/(9.9870 - 7.7872)$$

x = 0.8799

$$(P/G,27\%,10) = 9.9870 - 0.8799 = 9.1071$$

(b) 1.
$$(A/P, 13\%, 15) = [0.13(1+0.13)^{15}]/[(1+0.13)^{15}-1]$$

= 0.15474

2. $(P/G,27\%,10) = [(1+0.27)^{10} - (0.27)(10) - 1]/[0.27^2(1+0.27)^{10}]$ = 9.0676

2.22 (a) 1. Interpolate between n = 60 and n = 65:

$$2/5 = x/(4998.22 - 2595.92)$$

x = 960.92

$$(F/P, 14\%, 62) = 4998.22 - 960.92$$
$$= 4037.30$$

2. Interpolate between n = 40 and n = 48: 5/8 = x/(0.02046 - 0.01633)x = 0.00258

$$(A/F,1\%,45) = 0.02046 - 0.00258 = 0.01788$$

(b) 1.
$$(F/P, 14\%, 62) = (1+0.14)^{62} - 1$$

= 3373.66

2.
$$(A/F,1\%,45) = 0.01/[(1+0.01)^{45} - 1]$$

= 0.01771

(c) 1. = -FV(14%, 62, 1) displays 3373.66

3. = PMT(1%, 45, 1) displays 0.01771

2.23 Interpolated value: Interpolate between n = 40 and n = 45:

$$3/5 = x/(72.8905 - 45.2593)$$

x = 16.5787

(F/P,10%,43) = 45.2593 + 16.5787= 61.8380

Formula value: $(F/P, 10\%, 43) = (1+0.10)^{43} - 1 = 59.2401$

% difference = [(61.8380 - 59.2401)/ 59.2401]*100 = 4.4%

2.24 Interpolated value: Interpolate between n = 50 and n = 55: 2/5 = x/(14524 - 7217.72)x = 2922.51

(F/A, 15%, 52) = 7217.72 + 2922.51 = 10,140

Formula value: $(F/A, 15\%, 52) = [(1+0.15)^{52} - 1]/0.15 = 9547.58$

% difference = [(10,140 - 9547.58)/ 9547.58](100) = 6.2%

2.25 (a) Profit in year 5 = 6000 + 1100(4) = \$10,400

(b)
$$P = 6000(P/A,8\%,5) + 1100(P/G,8\%,5)$$

= 6000(3.9927) + 1100(7.3724)
= \$32,066

2.26 (a) G = (241 - 7)/9 = \$26 billion per year

(b) Loss in year 5 = 7 + 4(26) = \$111 billion

(c) A = 7 + 26(A/G,8%,10)= 7 + 26(3.8713) = \$107.7 billion

2.27 A = 200 - 5(A/G, 8%, 8)= 200 - 5(3.0985)= \$184.51

- **2.28** P = 60,000(P/A,10%,5) + 10,000(P/G,10%,5)= 60,000(3.7908) + 10,000(6.8618) = \$296,066
- **2.29** (a) $CF_3 = 70 + 3(4) = \$82$ (\$82,000)
 - (b) P = 74(P/A, 10%, 10) + 4(P/G, 10%, 10)= 74(6.1446) + 4(22.8913) = \$546.266 (\$546, 266)
 - F = 546.266(F/P,10%,10)= 521.687(2.5937) = \$1416.850 (\$1,416,850)
- **2.30** 601.17 = A + 30(A/G, 10%, 9)601.17 = A + 30(3.3724)A = \$500
- **2.31** P = 2.1B (P/F, 18%, 5)= 2.1B (0.4371)= \$917,910,000
 - 917,910,000 = 50,000,000(P/A,18%,5) + G(P/G,18%,5) 917,910,000 = 50,000,000(3.1272) + G(5.2312) G = \$14,557,845
- **2.32** 75,000 = 15,000 + G(A/G,10%,5)75,000 = 15,000 + G(1.8101)G = \$33,147
- 2.33 First find P_g (using equation) and then convert to A

For n = 1: $P_g = \{1 - [(1 + 0.04)/(1 + 0.10)]^1\}/(0.10 - 0.04)$ = 0.90909 A = 0.90909(A/P,10%,1) = 0.90909(1.1000) = 1.0000 For n = 2: $P_g = \{1 - [(1 + 0.04)/(1 + 0.10)]^2\}/(0.10 - 0.04)$ = 1.7686 A = 1.7686(A/P,10%,2) = 1.7686(0.57619) = 1.0190

2.34
$$P_g = 50,000\{1 - [(1 + 0.06)/(1 + 0.10)]^8\}/(0.10 - 0.06)$$

= \$320,573

2.35
$$P_{g1} = 10,000\{1 - [(1 + 0.04)/(1 + 0.08)]^{10}\}/(0.08 - 0.04)$$

= \$78,590

$$P_{g2} = 10,000\{1 - [(1 + 0.06)/(1 + 0.08)]^{11}\}/(0.08 - 0.06)$$

= \$92,926

Difference = \$14,336

2.36
$$P_g = 260\{1 - [(1 + 0.04)/(1 + 0.06)]^{20}\}/(0.06 - 0.04)$$

= 260(15.8399)
= \$4118.37 per acre-ft

- **2.37** P = 30,000[10/(1 + 0.06)] = \$283,019
- **2.38** 18,000,000 = 3,576,420(P/A,i,7) (P/A,i,7) = 5.0330

From interest tables in P/A column and n = 7, i = 9% per year.

Can be solved using the RATE function = RATE(7,3576420,18000000).

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2.39 813,000 = 170,000(F/P,i,15)
813,000 = 170,000(1 + i)<sup>15</sup>
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 $\begin{array}{l} \log 4.78235 = (15) \log \left(1 + i\right) \\ 0.6796 / 15 = \log \left(1 + i\right) \\ \log \left(1 + i\right) = 0.04531 \end{array}$

1 + i = 1.11i = 11 % per year

Can be solved using the RATE function = RATE(15,,-170000,813000).

2.40 100,000 = 210,325(P/F,i,30) (P/F,i,30) = 0.47545

Find i by interpolation between 2% and 3%, by solving the P/F equation for i, or by spreadsheet. By spreadsheet function = RATE(30, 100000, -210325), i = 2.51%.

2.41 (1,000,000 - 1,900,000) = 200,000(F/P,i,4)(F/P,i,4) = 4.5

> Find i by interpolation between 40% and 50%, by solving F/P equation, or by spreadsheet. By spreadsheet function = RATE(4, -200000, 900000), i = 45.7% per year.

2.42 800,000 = 250,000(P/A,i,5)(P/A,i,5) = 3.20

Interpolate between 16% and 18% interest tables or use a spreadsheet. By spreadsheet function, $i = 16.99\% \approx 17\%$ per year.

2.43 87,360 = 24,000(F/A,i,3) (F/A,i,3) = 3.6400

For n = 3 in F/A column, 3.6400 is in 20% interest table. Therefore, i = 20% per year.

2.44 48,436 = 42,000 + 4000(A/G,i,5) 6436 = 4000(A/G,i,5) (A/G,i,5) = 1.6090

For n = 5 in A/G column, value of 1.6090 is in 22% interest table.

2.45 600,000 = 80,000(F/A,15%,n) (F/A,15%,n) = 7.50

Interpolate in the 15% interest table or use a spreadsheet function. By spreadsheet, n = 5.4 years.

2.46 Starting amount = 1,600,000(0.55) = \$880,000

1,600,000 = 880,000(F/P,9%,n) (F/P,9%,n) = 1.8182

Interpolate in 9% interest table or use the spreadsheet function = NPER(9%,,-880000,1600000) to determine that $n = 6.94 \approx 7$ years.

2.47 200,000 = 29,000(P/A,10%,n) (P/A,10%,n) = 6.8966

Interpolate in 10% interest table or use a spreadsheet function to display n = 12.3 years.

2.48 1,500,000 = 18,000(F/A,12%,n) (F/A,12%,n) = 83.3333

Interpolate in 12% interest table or use the spreadsheet function

= NPER(12%, -18000, 1500000) to display n = 21.2 years. Time from now is

21.2 - 15 = 6.2 years.

2.49 350,000 = 15,000(P/A,4%,n) + 21,700(P/G,4%,n)

Solve by trial and error in 4% interest table between 5 and 6 years to determine $n\approx 6$ years

2.50 16,000 = 13,000 + 400(A/G,8%,n)(A/G,8%,n) = 7.5000

Interpolate in 8% interest table or use a spreadsheet to determine that n = 21.8 years.

2.51 $140(0.06 - 0.03) = 12\{1 - [(0.97170)]^x\}$ $4.2/12 = 1 - [0.97170]^x$ $0.35 - 1 = -[0.97170]^x$ $0.65 = [0.97170]^x$

$$log 0.65 = (x)(log 0.97170)$$

x = 15 years

2.52 135,300 = 35,000 + 19,000(A/G,10%,n)100,300 = 19,000(A/G,10%,n)(A/G,10%,n) = 5.2789

From A/G column in 10% interest table, n = 15 years.

2.53 88,146 = 25,000{1 - $[(1 + 0.18)/(1 + 0.10)]^{n}$ }/(0.10 - 0.18) 3.52584 = {1 - $[(1.18)/(1.10)]^{n}$ }/(-.08) -0.28207 = {1 - $[(1.18)/(1.10]^{n}$ } -1.28207 = $-[(1.18)/(1.10]^{n}$ 1.28207 = $[(1.07273]^{n}$

log 1.28207 = n log 1.072730.10791 = n(0.03049) n = 3.54 years

2.54 P = 30,000(P/F,12%,3)= 30,000(0.7118) = \$21,354

Answer is (d)

2.55 30,000 = 4200(P/A,8%,n)(P/A,8%,n) = 7.14286

n is between 11 and 12 years

Answer is (c)

2.56 A = 22,000 + 1000(A/G,8%,5) = \$23,847

Answer is (a)

- **2.57** Answer is (d)
- **2.58** A = 800 100(A/G, 4%, 6) = \$561.43

Answer is (b)

- **2.59** Answer is (b)
- **2.60** F = 61,000(F/P,4%,4)= 61,000(1.1699) = \$71,364

Answer is (c)

 $2.61 P = 90,000(P/A,10\%,10) \\= 90,000(6.1446) \\= $553,014$

Answer is (d)

2.62 A = 100,000(A/P,10%,7)= 100,000(0.20541)= \$20,541

Answer is (b)

2.63 A = 1,500,000(A/F,10%,20) = 1,500,000(0.01746) = \$26,190

Answer is (a)

2.64 In \$1 million units A = 3(10)(A/P, 10%, 10) = 30(0.16275) $= $4.8825 \quad (\approx $4.9 million)$

Answer is (c)

2.65 75,000 = 20,000(P/A,10%,n) (P/A,10%,n) = 3.75

By interpolation or NPER function, n = 4.9 years

Answer is (b)

2.66 50,000(F/A,6%,n) = 650,000 (F/A,6%,n) = 13.0000

By interpolation or NPER function, n = 9.9 years

Answer is (d)

2.67 40,000 = 13,400(P/A,i,5) (P/A,i,5) = 2.9851

By interpolation or RATE function, i = 20.0 % per year

Answer is (a)

2.68 P = 26,000(P/A,10%,5) + 2000(P/G,10%,5)= 26,000(3.7908) + 2000(6.8618)= \$112,284

Answer is (b)

2.69 F = [5000(P/A, 10%, 20) + 1000(P/G, 10%, 20)](F/P, 10%, 20)= [5000(8.5136) + 1000(55.4069)](6.7275)= \$659, 126

Answer is (d)

2.70 A = 300,000 - 30,000(A/G,10%,4)= 300,000 - 30,000(1.3812)= \$258,564

Answer is (b)

2.71 F = {
$$5000[1 - (1.03/1.10)^{20}]/(0.10 - 0.03)$$
}(F/P,10%,20)
= { $5000[1 - (1.03/1.10)^{20}]/(0.10 - 0.03)$ }(6.7275)
= \$ $351,528$

Answer is (c)

Solution to Case Study, Chapter 2

There is no definitive answer to case study exercises. The following are examples only.

Time Marches On; So Does the Interest Rate

1. <u>Si</u>	tuation	А	В	С	D
Inter	rest rate	6% per year	6% per year	15% per year	Simple: 780% per year Comp'd: 143,213% per year
C: 2 million = $300,000(P/A,i\%,65)$ (P/A,i%,64) = 6.6666667 i = 15%					
D: $30/200 = 15\%$ per week					
Simple: $15\%(52 \text{ weeks}) = 780\%$ per year					
Compound: $(1.15)^{52} - 1 = 143,213\%$ per year					
2. A:	Start S	\$24			
	End I	$F = 24(1.06)^{385} = S$	\$132 billion		
B:	B: Start \$2000 per year or \$20,000 total over 10 years				
	End I	$F_{32} = A(F/A, 6\%, 1)$	0) = \$26,361.60		
	I	$F_{70} = F_{32}(F/P, 6\%, 3)$	38) = \$241,320		
C:	Start S	52 million			
	End 300,000(65) = \$19.5 million over 65 years				
	Ι	$F_{65} = 300,000 (F/A)$.,15%,65) = \$17.6	billion (equival	ent)
D:	<u>Simple in</u> Start	nterest \$200			
	End	(0.15)(12)(200) +	200 = \$1760		
	<u>Compou</u> Start	<u>ind interest</u> \$200			

End -- $200(1.15)^{52} = $286,627$