

# SOLUTIONS MANUAL

Second Edition

# ADVANCED MECHANICS OF MATERIALS

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## List of Final Answers

For details, and where proofs are required, see following worked-out solutions

- 1.4-1 [Proof required]  
 1.4-2  $P = 2kv(a - L)/a$  where  $a^2 = L^2 + v^2$   
 1.4-3  $p = (\alpha_a - \alpha_s)TtE_aE_s/[R(E_a - E_s)]$   
 1.5-1 [Proof required]  
 1.5-2  $\tau_{zx} = (P/A) - (Pd/J)y$ ,  $\tau_{yz} = (Pd/J)x$ , where  $J = I_x + I_y$   
 1.6-1 Consider equilibrium; note that  $M = 0$  at inflection point  
 1.6-2 [Proof required]  
 1.6-3(a,b) [Proof required]  
 (c)  $\epsilon = ky$  if cross sections warp identically  
 1.6-4 Surfaces:  $\sigma_t = 3M(1 + \sqrt{R})/bh^2\sqrt{R}$ ,  $\sigma_c = -\sqrt{R}\sigma_t$ , where  $R = E_c/E_t$   
 1.6-5  $M_{\max} = F^2/2q$   
 1.6-6(a)  $F_a = 2EI/\rho L$  (b)  $s = L - 2EI/\rho F_b$   
 1.6-7  $h_L/h_0 = 3$ , stress ratio = 9/8  
 1.7-1  $\sigma_A = -\tau L/c$ ,  $\sigma_B = 2\tau L/c$ ,  $v_C = -\tau L^3/2Ec^2$   
 1.7-2  $v_C = -5hPL^2/48EI$   
 1.7-3  $v_C = \alpha L^2\Delta T/2c$   
 1.7-4 Doubtful, unless  $P$  is very small. Links become inclined.  
 1.7-5  $u_0 = L - \rho \sin\theta$ ,  $v_0 = \rho(1 - \cos\theta)$ ; where  $\theta = L/\rho$ ,  $\rho = EI/M_0$   
 1.7-6  $a/b = 2.00$   
 1.7-7  $a/b = 0.732$   
 1.7-8(a)  $y = Fx^3/3EI$  (b)  $y = Fx^2(L - x)^2/3EIL$   
 1.7-9  $R_x = R + P(x^4 - 2Lx^3 + L^3x)/12EIL$   
 1.8-1(a)  $u_D = 0$ ,  $v_D = 4QL/\sqrt{3}AE$   
 (b)  $u_D = PL/2.30AE$ ,  $v_D = 0$   
 (c)  $u_D = 1.188\alpha L\Delta T$ ,  $v_D = 0$   
 1.8-2  $T/\theta = 9GJ/20L$   
 1.8-3  $0.0169PL^3/EI$  at load,  $0.0039PL^3/EI$  at point opposite  
 1.8-4 Angle =  $TL^3/8EI[3R(R + L) + L^2]$   
 1.8-5(a)  $v = 5qL^4/384EI$  (b)  $v = M_L L^2/16EI$ ,  $\theta_L = M_L L/3EI$   
 (c)  $v = PL^3/192EI$  (d)  $v = qL^4/768EI$   
 1.8-6 Consider equilibrium. Match strain & curvature at interface.  
 1.8-7  $\sigma = 3Et(D + t)/L^2$   
 1.8-8  $L^4 = 72EID/q$   
 1.8-9  $\Delta T = \theta h/\alpha L$   
 1.9-1(a)  $P = \sigma_Y AL/b$  (b)  $P_{fp} = 2A\sigma_Y$   
 (c)  $\sigma_{res} = \sigma_Y(L - 2b)/L = \sigma_Y(2a - L)/L$   
 1.9-2(a)  $\sigma_1 = \sigma_Y$ ,  $\sigma_2 = \sigma_Y/2$   
 (b)  $(\sigma_1)_{res} = -\sigma_Y/2$ ,  $(\sigma_2)_{res} = -\sigma_Y/4$ ,  $u_{res} = \sigma_Y L/4E$

- 1.9-3  $P_Y = 2.30\sigma_Y A$  at  $u_D = \sigma_Y L/E$   
 $P_{fp} = 2.73\sigma_Y A$  at  $u_D = 4\sigma_Y L/3E$
- 2.3-1 (a) Pure shear  
 (b) Hydrostatic in a plane, or uniaxial stress  
 (c) Fully hydrostatic (3D)
- 2.3-2 (a)  $\sigma_1 = 82.1, \sigma_2 = 0, \sigma_3 = -52.1$  (in MPa)  
 (b)  $\sigma_1 = 127.6, \sigma_2 = -12.9, \sigma_3 = -195$  (in MPa)  
 (c)  $\sigma_1 = 114, \sigma_2 = 68.4, \sigma_3 = -163$  (in MPa)  
 (d)  $\sigma_1 = 297, \sigma_2 = 99.6, \sigma_3 = -177$  (in MPa)  
 (e)  $\sigma_1 = 22.4, \sigma_2 = 0, \sigma_3 = -22.4$  (in MPa)  
 (f)  $\sigma_1 = 74.6, \sigma_2 = -19.4, \sigma_3 = -55.2$  (in MPa)  
 (g)  $\sigma_1 = 200, \sigma_2 = -100, \sigma_3 = -100$  (in MPa)
- 2.3-3 }  $\begin{matrix} l_1 & m_1 & n_1 & l_2 & m_2 & n_2 & n_3 = n_1 \times n_2 \end{matrix}$
- 2.3-4 } (a) 0 0.973 0.230 0 -0.230 0.973  
 (b) 0.080 0.792 0.605 0.787 -0.423 0.449  
 (c) -0.309 0.925 0.223 0.911 0.219 0.353  
 (d) 0.806 -0.582 0.111 0.427 0.700 0.573  
 (e) 0.632 0.707 0.316 -0.447 0 0.894  
 (f) 0.651 0.502 0.570 -0.083 0.793 -0.604  
 (g) 0.577 0.577 0.577 [any normal to  $n_1$ ]
- 2.3-5  $\sigma_1 = \sigma_2 = 0, \sigma_3 = -80$  MPa
- 2.4-1 (a,b) [Proof required]
- 2.5-1 (a,b) [Proof required] (c)  $B = E/3(1 - 2\nu)$   
 (d) [Proof required]
- 2.5-2  $\epsilon_1 = 0.000457, \epsilon_2 = -0.000066, \epsilon_3 = -0.000303$
- 2.5-3  $A = \text{tr}_i / (1 - \nu)$
- 2.5-4  $\Delta T = 347^\circ\text{C}$
- 2.5-5 [Set of equations required]
- 2.5-6  $\tan \theta = \sqrt{\nu}, \sigma_x = E\epsilon_s / (1 - \nu)$
- 2.5-7  $p = 2Et(r - a) / [(1 - \nu)r^2]$ , maximum at  $r = 2a$
- 2.6-1 Case 1 (a)  $\sigma_1 = 30$  MPa,  $\sigma_2 = 20$  MPa,  $\sigma_3 = -20$  MPa  
 (b)  $n_1 = 1, l_2 = m_2 = -l_3 = m_3 = 0.707$   
 (c)  $\tau_{\text{Oct}} = 21.6$  MPa,  $\tau_{\text{max}} = 25$  MPa  
 (d)  $\tau_e = 45.8$  MPa  
 (e)  $U_{\text{od}} = 350/G$  N·mm/mm<sup>3</sup> (G in MPa)
- Case 2 (a)  $\sigma_1 = 35.1$  MPa,  $\sigma_2 = 7.1$  MPa,  $\sigma_3 = -27.2$  MPa  
 (b)  $l_1 = 0.636, m_1 = 0.384, n_1 = 0.669$   
 $l_2 = 0.240, m_2 = 0.725, n_2 = -0.645$   
 (c)  $\tau_{\text{Oct}} = 25.5$  MPa,  $\tau_{\text{max}} = 31.2$  MPa  
 (d)  $\sigma_e = 54.1$  MPa  
 (e)  $U_{\text{od}} = 487/G$  N·mm/mm<sup>3</sup> (G in MPa)
- 2.6-2 (a) (b) (c) (d),  $s_x$  (e),  $s_1$  (f)
- |     |      |      |     |       |      |          |
|-----|------|------|-----|-------|------|----------|
| (a) | 67.1 | 55.2 | 117 | -10   | 72.1 | 2285/G   |
| (b) | 161  | 132  | 280 | -53.3 | 154  | 13,070/G |
| (c) | 138  | 121  | 257 | 48.3  | 107  | 11,000/G |

- |     |      |      |      |     |      |          |
|-----|------|------|------|-----|------|----------|
| (d) | 237  | 194  | 412  | 107 | 224  | 28,300/G |
| (e) | 22.4 | 18.3 | 38.7 | 0   | 22.4 | 250/G    |
| (f) | 64.9 | 54.7 | 116  | 0   | 74.6 | 2250/G   |
| (g) | 150  | 141  | 300  | 0   | 200  | 15,000/G |
- 2.7-1  $K_t = 2.0$  for small load,  $K_t \approx 1$  for large load  
2.7-2  $r/D = 1/4$ , stress ratio = 1.14  
2.7-3  $a/b = 2$ ,  $\sigma_{\max} = 1.5\sigma_1$   
2.7-4(a)  $\nu = 1/3$  (b)  $a/b = 1/\nu$ ,  $\sigma_A = \sigma_B = -(1 + \nu)\sigma_O$   
2.7-5(a) [Proof required] (b)  $\sigma_{\max} = 159T/D^3$  (c)  $T_{fp} = 0.05657\tau_Y D^3$   
2.7-6 Cut away a central strip of width  $w$   
2.7-7 Residual  $\sigma_B = \sigma_Y(1 - K_t)$  (compressive)  
2.8-1(a)  $p_O = 0.591\sqrt{PE/LR}$  (b)  $p_O = 0.418\sqrt{PE/LR}$  (c)  $p_O = 0.091\sqrt{PE/LR}$   
2.8-2(a)  $T = PR\phi$  (b)  $p_O = 0.296(\phi/R)\sqrt{PE}$  (c)  $\sigma = 298$  MPa  
2.8-3 [Argument resembles that of Problem 1.7-8]  
3.2-1(a) [Derivation required] (b)  $\tau = \sigma_{tf}\sigma_{cf}(\sigma_{tf} + \sigma_{cf})$   
3.2-2 Expand square in third quadrant of Fig. 3.3-1 to triple size  
3.2-3(a) -240 MPa to 40 MPa (b) -120 MPa to 25 MPa  
3.2-4  $T = 7.57$  kN·m  
3.2-5  $r = 61.4$  mm  
3.3-1 Results in first quadrant ( $\sigma_x > \sigma_y > 0$ ; then  $\sigma_y > \sigma_x > 0$ ):  
(a)  $45^\circ$  to  $x$  and  $z$  axes; then  $45^\circ$  to  $y$  and  $z$  axes  
(b)  $\sigma_x = \sigma_1$ ,  $\sigma_y = \sigma_2$ ,  $0 = \sigma_3$ ; then  $\sigma_y = \sigma_1$ ,  $\sigma_x = \sigma_2$ ,  $0 = \sigma_3$   
(c)  $\sigma_x = \sigma_y$ , then  $\sigma_y = \sigma_y$   
3.3-2(a)  $\sigma_x^2 + 4\tau_{xy}^2 = \sigma_y^2$  (b)  $\sigma_x^2 + 3\tau_{xy}^2 = \sigma_y^2$   
(c)  $\sigma_1^2 - \sigma_1\sigma_3 + \sigma_3^2 = \sigma_y^2$  (d)  $\sigma_x^2 - \sigma_x\sigma_y + \sigma_y^2 + 3\tau_{xy}^2 = \sigma_y^2$   
3.3-3(a) 1,3,2 (b) 1,3,2 (c) 3, 1 and 2 tied (d) 3,2,1  
3.3-4(a)  $\sigma_y = 110$  MPa (b)  $\sigma_y = 105.4$  MPa  
3.3-5(a) -120 MPa to 50 MPa (b) -137.6 MPa to 67.6 MPa  
3.3-6(a)  $\sigma_y = 400$  MPa ( $\tau_{\max}$  theory) or  $\sigma_y = 346$  MPa (von M. theory)  
(b)  $\sigma_y = 542$  MPa ( $\tau_{\max}$  theory) or  $\sigma_y = 542$  MPa (von M. theory)  
3.3-7  $P = 62.8$  N ( $\tau_{\max}$  theory) or  $P = 69.2$  N (von M. theory)  
3.3-8(a) SF = 3.73 (b) SF = 4.11  
3.3-9(a)  $t = 5.89$  mm (b)  $t = 5.89$  mm  
3.3-10(a)  $r = 9.66$  mm (b)  $r = 9.27$  mm  
3.3-11  $r = [4(SF)\sqrt{M^2 + kT^2}/\pi\sigma_y]^{1/3}$ :  $k = 1$  in (a),  $k = 0.75$  in (b)  
3.5-1  $a = 5.24$  mm  
3.5-2(a)  $P = 1.51$  MN (b)  $P = 4.52$  MN (c)  $P = 1.54$  MN  
3.5-3(a)  $P = 173$  kN (b)  $P = 59.2$  kN (c)  $M = 1.29$  kN·m  
3.5-4(a) SF = 0.779 (b) SF = 0.728 (c) SF = 0.917  
3.5-5(a)  $a = 28.1$  mm (b)  $a = 24.7$  mm (c)  $a = 20.3$  mm  
3.5-6(a)  $P = 12.4$  kN (b)  $P = 31.9$  kN (c)  $P = 17.9$  kN  
3.5-7 First quadrant of ellipse with aspect ratio 0.75  
3.5-8 [Rather lengthy expressions]  
3.5-9(a)  $T = 1.02$  MN·m (b)  $T = 1.15$  MN·m (c)  $T = 1.36$  MN·m  
3.6-1  $N \approx 1000$  cycles  
3.6-2  $2A = [(SF)(P_{\max} - P_{\min})/\sigma_{fs}] + [(P_{\max} + P_{\min})/\sigma_u]$   
3.6-3(a) SF = 1.08 (b) SF = 0.69

- 3.6-4 Depth = 77.3 mm based on stress, 88.6 mm based on deflection  
 3.6-5(a) SF = 0.95 (b) SF = 0.52  
 3.6-6 SF = 4.74  
 3.6-7(a) About 26,000 cycles (b) About 600 repetitions  
 3.6-8(a) Yes (b) No (c) No (d) No (e) Yes  
 4.1-1 Energy expended =  $w^2/4k$   
 4.1-2  $\theta = \arcsin(C/WL)$   
 4.1-3  $F_1 = k_1a\theta$ ,  $F_2 = 2k_2a\theta$ , where  $\theta = C/[a^2(k_1 + 4k_2)]$   
 4.1-4  $\theta = \arcsin(W/2kL)$   
 4.1-5  $F_A = P/7$ ,  $F_B = 2P/7$ ,  $F_C = 4P/7$   
 4.1-6  $\theta = 4W/9ka$ ,  $v = 13W/18k$   
 4.1-7  $U = (AEg^2/4L) + (P^2L/4AE)$   
 4.1-8(a)  $u = (F/2\pi GL)\ln(R/r)$  (b)  $\theta = (T/4\pi GL)(R^2 - r^2)/R^2r^2$   
 4.1-9  $T/\theta = 9GJ/20L$   
 4.2-1  $\theta = PL^2/2EI$   
 4.2-2 Change in length =  $Pvd/AE$   
 4.2-3(a)  $\Delta V = Fhr(1 - \nu)/2Et$  (b)  $\Delta V = Fr^2(2 - \nu)/Et$   
 4.2-4 [Proof required]  
 4.2-5 [Explanation required]  
 4.2-6 [Proof required]  
 4.2-7  $\Delta V = Fh(1 - 2\nu)/E$   
 4.3-1 [Proof required]  
 4.3-2 [Proof required]  
 4.3-3(a,b,c) [Proof required]  
 4.4-1  $\theta = qL^3/6EI$ ,  $v = 17qL^4/384EI$   
 4.5-1  $u_C = qL^2/2Eb$ ,  $v_C = 2qL^3/Ebh^2$   
 4.5-2(a)  $v_A = 14Fa^3/3EI$ ,  $\theta_A = 2Fa^2/EI$   
       (b)  $v_C = 5Fa^3/6EI$ ,  $\theta_C = 3Fa^2/2EI$   
       (c)  $\theta_{AC} = 23Fa^2/12EI$   
 4.5-3  $v_C = 5q_L L^4/768EI$ ,  $\theta_C = 7q_L L^3/5760EI$   
 4.5-4(a)  $u_A = 5QL^3/3EI$ ,  $v_A = QL^3/EI$ ,  $w_A = 0$   
       (b)  $u_A = 0$ ,  $v_A = 0$ ,  $w_A = (4FL^3/3EI) + (2FL^3/GK)$   
 4.5-5(a)  $v_C = (qb^4/8EI) + (qa^3b/3EI) + (qab^3/2GK)$   
       (b)  $w_D = (qb^3c/6EI) + (qab^2c/2GK)$   
       (c)  $\theta_{xC} = (qb^3/6EI) + (qab^2/2GK)$   
 4.5-6  $\alpha = \pi/8$  or  $\alpha = 5\pi/8$   
 4.5-7(a) 4.127PL/AE (rightward) (b) 8.954PL/AE (downward)  
       (c) 0.752PL/AE (rightward) (d) 12.504PL/AE (downward)  
       (e) 5.590PL/AE (separation)  
 4.6-1  $\theta_C = 1.15PR^2/EI$  at  $60.3^\circ$  clockwise from line AC  
 4.6-2 Exact:  $v_C = 0.0621PL^3/EI$   
       Simple approximation:  $v_C = 0.0519PL^3/EI$   
       Better approximation:  $v_C = 0.0644PL^3/EI$



- 4.6-3  $u_O = CRL/EI$ ,  $v_O = CL(R + L/2)/EI$ ,  
 $w_O = (CL/EI)(R + L/2) + \pi(CR^2/4EI) - (CR^2/GJ)(1 - \pi/4)$
- 4.6-4(a)  $u_A = 3\pi QR^3/EI$ ,  $v_A = 0$ ,  $w_A = 0$   
(b)  $u_A = 0$ ,  $v_A = 0$ ,  $w_A = (\pi FR^3/EI) + (3\pi FR^3/GJ)$
- 4.6-5 Spring constant =  $2EI/\pi R^3$
- 4.6-6  $u_A = 0$ ,  $v_A = 0$ ,  $w_A = \pi PR^3/GK$   
 $\theta_{xA} = -2PR^2/GK$ ,  $\theta_{yA} = 0$ ,  $\theta_{zA} = 0$
- 4.6-7(a)  $u_B = 2qR^4/3EI$  (b)  $v_C = -0.226qR^4/EI$
- 4.6-8(a)  $u_A = \pi^2 qR^4/EI$ ,  $v_A = -3\pi qR^4/2EI$ ,  $w_A = 0$   
(b)  $u_A = 9\pi R^4/2EI$ ,  $v_A = \pi^2 qR^4/EI$ ,  $w_A = 0$   
(c)  $u_A = 0$ ,  $v_A = 0$ ,  $w_A = 2\pi^2 qR^4/GJ$
- 4.6-9(a)  $\theta_{xA} = 0$ ,  $\theta_{yA} = 0$ ,  $\theta_{zA} = 0$   
(b)  $\theta_{xA} = 0$ ,  $\theta_{yA} = 0$ ,  $\theta_{zA} = 4\pi qR^3/EI$   
(c)  $\theta_{xA} = \pi qR^3(3/GJ + 1/EI)$ ,  $\theta_{yA} = 0$ ,  $\theta_{zA} = 0$
- 4.6-10(a)  $u_O = 0.163qR^4/EI$  (to right),  $v_O = 0.215qR^4/EI$  (down)  
(b)  $v_O = \pi qR^2/4EA$  (up)
- 4.6-11  $v = (FR^3/EI)[1 + \cos \phi + 0.5(\pi - \phi)\sin \phi]$
- 4.6-12(a) Use Eqs. 4.6-1; neglect effect of  $\alpha$  (b)  $w = 4PR^3n/Gc^4$   
(c)  $\theta = 4nRC(2 + \nu)/Ec^4$  (d)  $u = 2(2 + \nu)FH^3/3\pi Ec^4\alpha$
- 4.7-1  $a/b = 0.732$
- 4.7-2 Force = 0.85W
- 4.7-3 Separation =  $Pb^3(4a + b)/[12EI(a + b)]$
- 4.7-4  $H_B = qa^3/[8b(a + b)]$
- 4.7-5 Reaction =  $(5qa/4) - (6EIg/a^3)$
- 4.7-6  $v_A = 0.0709FL^3/EI$
- 4.7-7  $T = F/(2 + c)$ , where  $c = 6I/5AL^2$
- 4.7-8  $u_C = 20,900F/EL$
- 4.7-9 [Discussion required]
- 4.7-10  $M_C = (5Fa/16) + (qa^2/4)$
- 4.7-11 For  $EI = GK$ ,  $M_C = [Fa(a + 2b)/4 + qa^2(a + 3b)/6]/(a + b)$
- 4.7-12  $M_O = (FL/8) - (2\beta EI/L)$ ,  $v_C = (FL^3/192EI) + (\epsilon L/4)$
- 4.7-13(a)  $H \int_0^L y^2 ds = EI\alpha L\Delta T$  (b)  $M = 0$  everywhere
- 4.7-14 [Discussion required]
- 4.7-15  $\theta = 0.149CR/EI$
- 4.7-16(a)  $C = 0.307FR$  (b)  $v = 0.0704FR^3/EI$
- 4.7-17(a)  $M_C = 0.182PR$  (b)  $M_A = 0.242PR$   
(c)  $u_C = 0.0708PR^3/EI$  (d)  $M_C = 0.151PR$   
(e)  $u_B = -0.722PR^3/EI$  (f)  $v_C = -0.0260M_C R^2/EI$

- 4.7-18(a)  $v_C = 0.149PR^3/EI$  (b)  $\Delta_{BD} = -0.137PR^3/EI$   
(c)  $M_C = 0$ ,  $w_C = (\pi R^2 M_O/4)(1/GK + 1/EI)$  (d)  $T_C = M_O/\pi$   
(e)  $M_C = 2PR/\pi [1 + (GK/EI)]$  (f)  $M_B = 0.429 qR^2$   
(g)  $v_C = -\rho R^5 \omega^2/6EI$
- 4.7-19  $M_A = (2T_O a/b)[(bEI + aGK)/(bEI + 2aGK)]$
- 4.7-20  $M_C = qL^2/8$ ,  $Q = 5qL/8$
- 4.8-1  $w = 4PR^3 n/Gc^4$ ; lateral displacement increments cancel
- 4.10-1  $F_1 = -0.667P$ ,  $F_2 = 0.0833P$ ,  $F_3 = 0.750P$
- 4.10-2  $P = kL$ ;  $d^2\Pi/d\theta^2 < 0$  if  $P > kL$
- 4.10-3  $d^2\Pi/d\theta^2 > 0$  if  $h < 2R$
- 4.10-4  $u_D = 2.083L \propto \Delta T$ ,  $v_D = 0$ . Bar stresses are zero
- 4.11-1  $v_L = -qL^4/8EI$ ,  $M_O = -qL^2/2$
- 4.11-2(a)  $v_L = -FL^3/4EI$ ,  $M_O = -FL/2$  (b)  $v_L = -FL^3/3EI$ ,  $M_O = -FL$   
(c)  $v_L = -FL^3/12EI$ ,  $M_O = 0$  (d)  $v_L = -0.328FL^3/EI$ ,  $M_O = -0.813FL$
- 4.11-3  $\theta_L = M_L L/3EI$
- 4.11-4(a)  $v_C = -FL^3/64EI$ ,  $M_C = FL/8$   
(b)  $v_C = -qL^4/96EI$ ,  $M_C = qL^2/12$   
(c)  $v_C = -q_L L^4/192EI$ ,  $M_C = q_L L^2/24$
- 4.11-5  $v_L = -0.308F/k$
- 4.11-6(a)  $u = qLx/2EA$ ,  $\sigma = qL/2A$   
(b)  $u = (q/EA)(Lx - x^2/2)$ ,  $\sigma = q(L - x)/A$
- 4.11-7(a)  $v = ax^2(L - x)$  (b)  $v_W = -0.00549WL^3/EI$   
(b) Stable if  $EI > \gamma bL^4/420$
- 4.11-8  $P = 0.7222EA_0 u_L/L$  (0.12% high)
- 4.12-1  $v_O = 0.142FR^3/EI$ ,  $M_O = 4FR/3\pi$
- 4.12-2  $v_O = \rho R^5 \omega^2/18EI$ ,  $M_O = \rho R^3 \omega^2/9$
- 4.12-3 First term:  $v_L$  errs by -4.5%;  $M_O$  errs by -41%
- 4.12-4(a) First term:  $v_L/2$  errs by -1.45%;  $M_L/2$  errs by -18.9%  
(b) First term:  $v_L/2$  errs by +0.38%;  $M_L/2$  errs by +3.2%  
(c) First term:  $v_L/2$  errs by +0.38%;  $M_L/2$  errs by +3.2%
- 4.12-5 First term:  $u_L$  errs by +3.2%;  $\sigma_O$  errs by -18.9%
- 4.13-1 All results are exact
- 5.2-1 Deformation due to weight displaces equal weight of water.
- 5.2-2  $k = \rho g/l$
- 5.2-3 [Proof required]
- 5.2-4  $w = w_0 e^{-\beta x}$ , where  $\beta^2 = k/T$
- 5.2-5(a)  $\theta = -(T_0 \lambda/k)e^{-\lambda x}$ ,  $T = T_0 e^{-\lambda x}$ , where  $\lambda^2 = k/GJ$   
(b) Replace  $T$ ,  $\theta$ ,  $G$ ,  $J$  by  $P$ ,  $u$ ,  $E$ ,  $A$  respectively.  $\lambda^2 = k/EA$
- 5.3-1(a,b) [Proof required]
- 5.3-2(a)  $P_O = kw_O/\beta + k\theta_O/2\beta^2$ ,  $M_O = kw_O/2\beta^2 + k\theta_O/2\beta^3$

- (b)  $w = w_0 A_{\beta x} + (\theta_0/\beta) B_{\beta x}$ ,  $\theta = -2\beta w_0 B_{\beta x} + \theta_0 C_{\beta x}$ , etc.
- 5.3-3 Force =  $0.2169P_0 = 10.8$  kN
- 5.3-4(a)  $w_{\max}/w_{\min} = -0.2079$ ,  $M_{\max}/M_{\min} = -23.1$   
 (b)  $F_+ = 0.6448\beta M_0$ ,  $F_- = -0.6726\beta M_0$
- 5.3-5  $P_0 = 45.2$  kN. Upward  $w$ : initial uniform pressure decreases.
- 5.3-6  $\sigma = 190$  MPa, at  $x = 99.9$  mm from loaded end
- 5.3-7  $w = (2\beta^2 M_0/k) B_{\beta x}$ ,  $\theta = (2\beta^3 M_0/k) C_{\beta x}$ , etc.
- 5.3-8(a)  $a = 1/2\beta$   
 (b)  $M_{\max} = Fa$ , at  $x = 0$ .  $M_{\min} = -0.1040F/\beta$ , at  $\beta x = \pi/2$
- 5.3-9(a)  $a = 1/\beta = 490$  mm (b)  $F = 488$  N
- 5.3-10  $Q = 168$  kN
- 5.3-11  $w_B = P[(3EI/L^3) + (k/2\beta)]^{-1}$
- 5.3-12 Depth =  $104.5$  mm
- 5.3-13  $M_{\text{cusp}} = 2.71$  kN·m
- 5.3-14  $M_A = M_B = (\beta a - 1)P/4\beta$ . AB is simply supported for  $\beta a = 1$ .
- 5.4-1 [Proof required]  
 5.4-2 [Proof required]  
 5.4-3 [Proof required]  
 5.4-4 [Proof required]
- 5.4-5  $w_{\max} = P/K + Ps^3/192EI$ ,  $M_{\max} = Ps/8$
- 5.4-6 [Argument required]  
 5.4-7  $\theta = M_0 h/[4EI(1 + \beta h)]$
- 5.4-8 Force load: factors  $0.595, 0.841$   
 Moment load: factors  $0.707, 1.000$
- 5.4-9  $\sigma \approx 176$  MPa
- 5.5-1  $M = 13,860$  N·mm,  $\Delta\sigma = 141$  MPa
- 5.5-2 Depth =  $139$  mm
- 5.5-3 Maximum  $\sigma_{\text{long}} = 61.6$  MPa, maximum  $\sigma_{\text{cross}} = 45.1$  MPa
- 5.5-4 Separation =  $\pi/2\beta$
- 5.5-5  $k = 0.264(P^4/EI\alpha^4)^{1/3}$
- 5.5-6(a)  $s \approx 0.179/\beta$  (b)  $s = 0.0257/\beta$
- 5.5-7 Separation =  $1.86/\beta$
- 5.5-8(a)  $w_{\max} = 16.4$  mm,  $200$  mm left of load  $2P$   
 (b)  $M_{\max} = 4.38$  kN·m, beneath load  $2P$
- 5.5-9  $x = 5\pi/4\beta$ ,  $P_0 = 71.9\beta M_0$
- 5.5-10  $a = 1280$  mm,  $M = -4.73$  kN·m
- 5.5-11(a)  $w_{\max} = 4.07$  mm,  $\sigma_{\max} = 97.3$  MPa  
 (b)  $w_{\max} = 6.45$  mm (at center load),  
 $\sigma_{\max} = 70.0$  MPa (at side load)
- 5.5-12(a)  $\sigma = 0.0146P$  (b)  $\sigma = 0.0226P$  (c)  $\sigma = 0.0110P$
- 5.5-13(a)  $w = 0.297$  mm,  $M = 4.20$  kN·m  
 (b)  $w = 0.228$  mm,  $M = 0.622$  kN·m  
 (c)  $w = 0.170$  mm  
 (d)  $w = 0.223$  mm,  $M = 4.00$  kN·m at load  $P$
- 5.5-14 [Derivation required]

- 5.5-15 New couple is  $0.586M_0$  (acting on portion to right)
- 5.5-16 Bending moment =  $0.268F/\beta$
- 5.6-1(a)  $w = q(1 - D_{\beta x})/k$  (b)  $M = (q/2\beta^2)B_{\beta x}$   
 (c)  $w = q(1 - A_{\beta x})/k$  (d)  $M_{\max} = 0.104q/\beta^2$ ,  $M_{\min} = -q/2\beta^2$
- 5.6-2 [Sketches required]
- 5.6-3 [Proof required]
- 5.6-4(a)  $M_{\text{center}} = 8840q$  (b)  $M_{\text{ends}} = -582q$  (c)  $M_{\pi/4} = 27,847q$   
 (d)  $M_{\max} = 27,850q$  (e)  $M_{\min} = -29,149q$
- 5.6-5  $M_{\text{center}} = 126,200q$ ,  $M_{\text{supports}} = -215,000q$
- 5.6-6  $M_{\max} = 0.0806(q_2 - q_1)/\beta^2$
- 5.6-7  $w = (q/2k)(2 + B_{\beta l}C_{\beta a} - C_{\beta l}D_{\beta a} - D_{\beta b})$   
 $M = (q/4\beta^2)(B_{\beta b} + B_{\beta a}C_{\beta l} - B_{\beta l}A_{\beta a})$
- 5.7-1  $w = -EI(d^2w/dx^2) = 0$  @  $x = 0$ ,  $d^2w/dx^2 = d^3w/dx^3 = 0$  @  $x = L$
- 5.7-2 [Proof required]
- 5.7-3  $p = (2P/bL)(2 - 3a/L) + (6P/bL^2)(2a/L - 1)x$ ,  $w = p/k_0$
- 5.7-4(a)  $L/3 < a < 2L/3$  (b)  $w_{\max} = 4P/3k_0bL$ ,  $w_{\min} = P/k_0bL$
- 5.7-5  $P = 3kLw_0/8$
- 5.7-6(a)  $M = PL/8$  (b)  $M_{\min} = -4PL/27$ , at  $x = L/3$
- 5.7-7 Energy expended =  $3W^2/2k_0bL$
- 5.7-8(a)  $w_{\max} = (P/\pi R^2k_0)(1 + 4a/R)$  (b)  $a = R/4$
- 5.7-9(a)  $p = (F/4ab)(1 + 3x_0x/a^2 + 3y_0y/b^2)$   
 (b) Central "diamond;" edge in 1st quadrant:  $3x_0/a + 3y_0/b = 1$
- 6.1-1  $\tau = Gy(d\theta/d\phi)/(r_n - y)$
- 6.2-1 [Derivation required]
- 6.2-2 [Derivation required]
- 6.2-3 [Derivation required]
- 6.2-4 [Derivation required]
- 6.2-5(a)  $A$ , exact;  $\int dA/r$ ,  $-0.1\%$ ;  $R$ ,  $0.5\%$ ;  $r_n$ ,  $0.1\%$ ;  $e$ ,  $-0.7\%$   
 (b)  $A$ , exact;  $\int dA/r$ ,  $-0.02\%$ ;  $R$ ,  $\approx$  exact;  $r_n$ ,  $0.03\%$ ;  $e$ ,  $-0.2\%$
- 6.2-6  $e = c^2/4R$ ; [proof required]
- 6.2-7 For  $a/b = 1.2, 1.6, 3.0, \text{ and } 8.0$ :  
 (a)  $0.0102, 0.0264, 0.0617, 0.1129$   
 (b)  $0.0104, 0.0278, 0.0667, 0.1167$   
 (c)  $1.056, 1.166, 1.469, 2.276$   
 (d)  $0.922, 0.822, 0.656, 0.503$
- 6.2-8  $a/b \approx 2.65$
- 6.2-9  $b/a = 0.194$
- 6.3-1 At  $r = b$ ,  $\sigma_{\phi} = 101 \text{ MPa}$ . At  $r = a$ ,  $\sigma_{\phi} = -224 \text{ MPa}$
- 6.3-2 At  $r = b$ ,  $\sigma_{\phi} = 315 \text{ MPa}$ . At  $r = a$ ,  $\sigma_{\phi} = -77.5 \text{ MPa}$
- 6.3-3(a)  $13.3\%$  low (b)  $46.5\%$  low
- 6.3-4  $P = 62.5 \text{ kN}$
- 6.3-5  $F = 6.33 \text{ kN}$
- 6.3-6  $t_i = 116 \text{ mm}$
- 6.3-7  $s = 1.91 \text{ mm}$
- 6.3-8 Stress probably  $283 \text{ MPa}$  at most

- 6.4-1(a,b,c,d) [Derivation required]
- 6.4-2(a) Radial force (not radial stress) largest at  $r_1 = r_n$   
 (b) [Proof required] (c)  $r_1 = b \exp(1 - b/r_n)$
- 6.4-3  $\sigma_r = 14.7 \text{ MPa}$
- 6.4-4  $\tau_1 = 28.6 \text{ MPa}$ , in straight parts but not much beyond
- 6.4-5(a)  $\sigma_r \approx 21 \text{ MPa}$  (b)  $\sigma_r \approx -101 \text{ MPa}$   
 (c)  $\sigma_r = 3M/2Rht$  (d) 2.8% high
- 6.4-6  $\sigma_r = -0.00937P/t$
- 6.4-7(a)  $\sigma_r = 73.1 \text{ MPa}$  (b)  $\sigma_r = 39.4 \text{ MPa}$
- 6.4-8(a)  $\sigma_r = 34.4 \text{ MPa}$  (b)  $t = 18.9 \text{ mm}$
- 6.4-9 [Sketches required]
- 6.4-10  $\sigma_y = -2P^2x^2/E_f b^2 t h^3$
- 6.5-1 [Sketches required]
- 6.5-2  $\sigma_\phi = -107 \text{ MPa}$  (inner),  $\sigma_\phi = 169 \text{ MPa}$  (outer),  $\tau_{\max} = 218 \text{ MPa}$
- 6.5-3(a)  $\sigma_\phi = 13.0(10^{-6})M$ ,  $\sigma_z = \pm 19.7(10^{-6})M$  } MPa if M is N·mm  
 (b)  $\sigma_r = 4.5(10^{-6})M$  (c)  $\tau_{\max} = 16.3(10^{-6})M$   
 (d) Reduce flange width and increase its thickness
- 6.5-4(a)  $\sigma_\phi = 166 \text{ MPa}$  (inside),  $\sigma_\phi = -244 \text{ MPa}$  (outside)  
 (b)  $\sigma_z = \pm 234 \text{ MPa}$  (c) Deforming ÷ nondeforming = 0.83  
 (d)  $\sigma_r = 65.6 \text{ MPa}$  (e)  $\tau_{\max} = 200 \text{ MPa}$
- 6.5-5(a)  $\sigma_\phi = 338 \text{ MPa}$  (inside),  $\sigma_\phi = -110 \text{ MPa}$  (outside)  
 (b)  $\sigma_z = \pm 172 \text{ MPa}$  (c) Deforming ÷ nondeforming = 0.85  
 (d)  $\sigma_r = 36 \text{ MPa}$  (e)  $\tau_{\max} = 131 \text{ MPa}$
- 6.6-1 [Sketches required]
- 6.6-2(a)  $\sigma_r \approx 0.68 \text{ MPa}$  (b)  $\tau_{\max} \approx 4.5 \text{ MPa}$
- 6.7-1 [Derivation required]
- 6.7-2  $v_o = (FR/EA)(0.785 + 5.318 + 0.429 + 2.180)$ . Ratio = 1.53
- 6.7-3 With  $q = pta/R$ ,  $v_A = (\pi q R^2/2A)[3(R/e - 1)/E + k/G] = 1575p/E$
- 6.7-4(a) [Derivation required]  
 (b)  $v_r = \frac{PR}{EA} \left[ \frac{4}{\pi} - \frac{\pi}{4} - \frac{2e}{\pi R} + \left( \frac{\pi}{4} - \frac{2}{\pi} \right) \frac{R}{e} + \frac{\pi k(1+\nu)}{2} \right]$   
 (c) Ratio = 2.89
- 7.1-1  $A_s = A_p(E_p/E_s)x/(L - x)$
- 7.1-2(a)  $\sigma_x = q(L - x)/A$  (b)  $u = (q/EA)[Lx - (x^2/2)]$   
 (c)  $\sigma_x = q(L - x)/A$  (d)  $d(A\sigma_x)/dx + q = 0$ ;  $q = q(x)$
- 7.2-1  $\sigma_x = 0$ ,  $\sigma_y = 2Ea_1x$ ,  $\tau_{xy} = 0$  (pure bending)
- 7.2-2  $\epsilon_{x'} = \epsilon_x \cos^2\theta + \epsilon_y \sin^2\theta + \gamma_{xy} \sin\theta \cos\theta$   
 $\gamma_{x'y'} = 2(\epsilon_y - \epsilon_x) \sin\theta \cos\theta + \gamma_{xy}(\cos^2\theta - \sin^2\theta)$
- 7.2-3  $\sigma_x = (qy/2I)(x - L)^2/(1 - \nu^2)$ . M correct if  $\nu = 0$
- 7.3-1(a)  $\partial N_x/\partial x + \partial N_{xy}/\partial y + B_x t = 0$ , etc. (b) [Derivation required]
- 7.3-2(a) Equilibrium not satisfied (b) Valid  
 (c) Equilibrium not satisfied (d) Valid
- 7.3-3  $\tau_{xy} = (3P/4c)[1 - (y^2/c^2)]$

- 7.3-4  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{1+\nu}{1-\nu} \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 v}{\partial x \partial y} \right) = 0$ , etc.
- 7.3-5 [Sketches required]
- 7.3-6  $u = 0$  on  $x$  and  $y$  axes; top edge and curved edge free;  
 $\sigma_x = My/I$  on right edge. Set  $v = 0$  at some point.
- 7.4-1(a,b) [Derivation required]
- 7.4-2 Equilibrium satisfied, but not compatibility across  $x = 1$
- 7.4-3 [Sketches required]
- 7.4-4  $F = (a_1 y^3 + a_2 x^3)/6 + c_1 xy + c_2 y + c_3 x + c_4$ ,  $\tau_{xy} = -c_1$
- 7.4-5  $g(y) = 5 - 43.7y$ ,  $f = -16.3x - 6$ , compatibility satisfied
- 7.4-6 [Argument required]
- 7.5-1(a,b,c,d) [Proof required]
- 7.5-2 [Proof required]
- 7.5-3 [Proof required]
- 7.5-4 Add  $qx^2/2$  to right hand side of Eq. 7.5-7
- 7.5-5  $\tau_{xy} = (qx/2I)(c^2 - y^2)$ ,  $\sigma_y = -(c^2 y/2 - y^3/6 + c^3/3)q/I$   
 Compatibility not satisfied
- 7.5-6 [Discussion required]
- 7.6-1  $u = -\nu \rho g x(y - L)/E + c_1 y + c_2$   
 $v = \rho g(y^2 - 2Ly + \nu x^2)/2E - c_1 x + c_3$  }  $c_2 = c_3 = 0$   
 may set  $c_1 = 0$
- 7.6-2  $\sigma_x = \rho g x$ ,  $u = (\rho g/2E)[x^2 - L^2 + \nu(y^2 + z^2)]$ ,  
 $v = -\nu \rho g xy/E$ ,  $w = -\nu \rho g xz/E$
- 7.6-3  $u = [a_1 xy - a_2(y^2 + \nu x^2)/2]/E + a_3 y/G$   
 $v = [a_2 xy - a_1(x^2 + \nu y^2)/2]/E$
- 7.6-4  $u = P[3(x^2 - L^2)y + \nu y^3]/4Ec^3 + Py(3c^2 - y^2)/4Gc^3$   
 $v = P[L^2(3x - 2L) - x(x^2 - 3\nu y^2)]/4Ec^3$
- 7.7-1 [Proof required]
- 7.7-2  $\sigma_A = 42$  kPa,  $\sigma_B = -33.8$  kPa
- 7.7-3(a,b,c) [Proof required]
- 7.7-4 Uniaxial stress  $\sigma_y = 4a_1$  (in direction  $\theta = \pi/2$ )
- 7.7-5 Cylinder, internal pressure (Eqs. 8.2-2)
- 7.7-6(a) Stresses due to torque  $T = 2\pi C$   
 (b)  $F = A \sin 2\theta + B \cos 2\theta + C\theta + D$  ( $A, B, C, D = \text{constants}$ )
- 7.7-7(a)  $\sigma_r = \sigma_{\theta a} \ln(r/a)$  (b) [Proof required]  
 (c) [Derivation required] (d)  $|M| = (2a^3 \sigma_{za}/9) \sin(\alpha/2)$   
 (e) Green wood is stronger in tension than in compression
- 7.8-1  $g = a_5 r^4 + a_6 r^2 + a_7/r^2 + a_8$
- 7.8-2(a)  $F_y = 0$  (b)  $F_x = 9.9495 \sigma_0 b$
- 7.8-3(a) SCF = 2 (b) SCF = 4
- 7.8-4(a)  $\theta = \pm \pi/4$  or  $\pm 3\pi/4$  ( $\sigma_\theta > 0$ );  $\theta = 0$  or  $\pi$  ( $\sigma_\theta < 0$ )  
 (b) For example:  $\sigma_x = \sigma_0$ ,  $\sigma_y = 3\sigma_0$
- 7.8-5  $\sigma_\theta = 137$  MPa (max),  $\sigma_\theta = -97.1$  MPa (min;  $90^\circ$  away)
- 7.9-1(a) [Proof required] (b) [Proof required]  
 (c) Top surface:  $\sigma_r = 49.29P/r$ ,  $Mc/I = 48.99P/r$   
 Midline:  $\sigma_{r\theta} = 0$ ,  $VQ/It = 4.32P/r$
- 7.9-2  $\sigma_1 = -\sigma_3 = \sqrt{2} P/\pi a$ ,  $\sigma_2 = 0$

- 7.9-3  $\sigma_x = -\frac{2q}{\pi} \left[ \arctan \frac{a}{b} - \frac{ab}{a^2 + b^2} \right]$ ,  $\sigma_y = -\frac{2q}{\pi} \left[ \arctan \frac{a}{b} + \frac{ab}{a^2 + b^2} \right]$
- 7.9-4  $F = (M/\pi)(\theta + \sin \theta \cos \theta)$
- 7.9-5(a) [Proof required]  
 (b) E.g. at  $y = -c$ :  $\sigma_x = 2.68P/c$ ,  $Mc/I = 3.00P/c$
- 7.9-6(a)  $\sigma_r = (-P/r)[2.141 \cos \beta - 1.363 \sin \beta]$  (b) [Proof required]
- 7.9-7(a)  $\sigma_r = (2P/\pi r) \cos(\beta + \lambda)$  (b)  $\beta + \lambda = \pi/2$   
 (c) Line OA collinear with force P
- 7.9-8 [Proof required]
- 7.10-1 For  $T = T_0$ :  $a_1 = 0$ ,  $a_2 = E\alpha T_0$ .  
 For  $T = T_0 y/c$ :  $a_1 = E\alpha T_0/c$ ,  $a_2 = 0$
- 7.10-2  $\sigma_x = -E\alpha T_0 y/c = -E\alpha T$
- 7.10-3  $\sigma_x = \sigma_y = -E\alpha z/(1 - \nu)$ ,  $\sigma_z = 0$   
 $u = v = 0$ ,  $w = (\alpha a z^2/2)[(1 + \nu)/(1 - \nu)]$
- 7.10-4  $\sigma_\theta = \sigma_z = \pm (E\alpha/2)(T_a - T_b)/(1 - \nu)$ ; + inside, - outside
- 7.10-5(a,b,c) [Proof required]
- 7.10-6  $\sigma_r = E\alpha k(r^2 - a^2)/4$ ,  $\sigma_\theta = E\alpha k(3r^2 - a^2)/4$
- 7.10-7  $T = T_b + (T_a - T_b) \ln(r/b)/\ln(a/b)$
- 7.11-1(a,b) [Proof required]
- 7.11-2  $u = T(b^2 - a^2)yz/\pi G a^3 b^3$
- 7.12-1 [Proof required]
- 7.12-2  $\beta = (T/\pi a^3 b^3 G)(a^2 + b^2)/(1 - k^4)$ ,  $\tau_{\max} = (2T/\pi a b^2)/(1 - k^4)$
- 7.12-3(a)  $k = G\beta/2h$ ,  $\beta = 15\sqrt{3} T/Gh^4$ ,  $\tau_{\max} = 15\sqrt{3} T/2h^3$   
 (b) Fails;  $\nabla^2 \phi = -2G\beta$  not satisfied
- 7.12-4(a) [Proof required] (b) [Proof required]  
 (c) Stress ratio =  $4a(b - 2a)/(4a^2 - b^2)$ . SCF  $\rightarrow 2$  as  $b \rightarrow 0$
- 8.2-1 [Proof required]
- 8.2-2 At  $r = b$ :  $\sigma_\theta = p_i$  and  $\sigma_r = 1.5 p_i$  respectively
- 8.2-3(a)  $p_i = 87.2$  MPa (b)  $p_i = 101$  MPa
- 8.2-4  $p_i = 139$  MPa
- 8.2-5  $F_i = 11/16$  of total;  $W_i = 3/8$  of total
- 8.2-6(a)  $a^2 = b^2(\sigma_{\max} + p_i)/(\sigma_{\max} - p_i)$   
 (b)  $a^2 = b^2\sigma_Y/(\sigma_Y - 2p_i)$   
 (c)  $a^2 = b^2(\sigma_Y^2 + p_i\sqrt{4\sigma_Y^2 - 3p_i^2})/(\sigma_Y^2 - 3p_i^2)$   
 (d)  $a = 1.291b$ ,  $a = 1.414b$ ,  $a = 1.353b$
- 8.2-7(a)  $p_0 = (p_i/2)(1 + b^2/a^2)$ ,  $\sigma_\theta = -(p_i/2)(1 - b^2/a^2)$   
 (b)  $\tau_{\max} = p_i/2$  at  $r = b$
- 8.2-8  $1 < (p_i/p_0) < (3a^2/b^2 + 1)/(a^2/b^2 + 3)$
- 8.2-9(a)  $2(\sigma_t - \sigma_r) - r(d\sigma_r/dr) = 0$   
 (b)  $(d^2u/dr^2) + (2/r)(du/dr) - 2u/r^2 = 0$   
 (c)  $u = Ar + B/r^2$ ; A and B are integration constants
- 8.3-1 [Sketches required]
- 8.3-2  $p_i = 6 + 1.52p_c$

- 8.3-3 [Several equations constitute the required answers]
- 8.3-4(a)  $\Delta = (2a^2bp_C/E)/(a^2 - b^2)$   
 (b)  $\Delta L = (2va^2Lp_C/E)/(a^2 - b^2)$
- 8.3-5  $p_C = 9p_i/16$
- 8.3-6  $p_i = 1.215\bar{\sigma}_\theta$ ,  $p_C = 0.1947\bar{\sigma}_\theta$
- 8.3-7  $2\Delta = 0.0907 \text{ mm}$
- 8.3-8 [Proof required]
- 8.3-9  $\sigma_\theta = -144kp_O/[25 + 39k - 15(1 - k)\nu]$
- 8.3-10(a)  $p_C = 9.375 \text{ MPa}$  (b)  $p_i = 34.8 \text{ MPa}$
- 8.3-11 [Proof required]
- 8.3-12 [Proof required]
- 8.3-13 [Proof required]
- 8.3-14(a)  $\sigma_r = -87.3 \text{ MPa}$  (b)  $\sigma_\theta = 216 \text{ MPa}$  (c)  $\sigma_\theta = 216 \text{ MPa}$
- 8.3-15(a)  $a = 9.09 \text{ mm}$ ,  $c = 6.74 \text{ mm}$   
 (b)  $\sigma_e = 347 \text{ MPa}$  at  $r = b$ ,  $\sigma_e = 363 \text{ MPa}$  at  $r = c$   
 (c)  $\sigma_e = 351 \text{ MPa}$  at  $r = b$ ,  $\sigma_e = 349 \text{ MPa}$  at  $r = c$
- 8.3-16 Factor = 1.25 for both
- 8.3-17  $\tau_{\max} = 3\sqrt{3} p_i b/2a$  at  $r = c$ ,  $p_i = 0.1925\sigma_Y(a/b)$
- 8.4-1(a) [Proof required] (b)  $\rho_s/\rho = 3E_s/E$  (s for spokes)
- 8.4-2 [Proof required]
- 8.4-3 [Proof required]
- 8.4-4  $a/b = 1.08$
- 8.4-5 [Proof required]
- 8.4-6  $\sigma_r = -89.3 \text{ MPa}$ ,  $\sigma_\theta = 161 \text{ MPa}$
- 8.4-7  $T = 57.4(10^6) \text{ N}\cdot\text{mm}$ ,  $\tau_{\text{net}} = 85.8 \text{ MPa}$
- 8.4-8(a)  $\omega = 19,900 \text{ rpm}$  (b)  $\omega = 13,850 \text{ rpm}$
- 8.4-9 Yes (barely)
- 8.4-10(a)  $\sigma_O = (\rho\omega^2/6a)(c^3 - a^3)$  (b)  $\sigma_\theta = 91.7 \text{ MPa}$
- 8.4-11(a)  $\omega_O^2 = 8p_C/[(3 + \nu)\rho a^2(1 - b^2/a^2)]$  (b)  $\omega = \omega_O/\sqrt{3}$   
 (c)  $P = 4\pi\mu p_C b^2 h\omega_b/(3\sqrt{3})$
- 8.4-12(a)  $p_C = 42.15 \text{ MPa}$  (b)  $\omega = 6450 \text{ rpm}$
- 8.4-13 [Explanations required]
- 8.5-1  $h_O = 61.1 \text{ mm}$
- 8.5-2(a)  $h_O = 25.7 \text{ mm}$ ,  $h_{O.2} = 25.0 \text{ mm}$ ,  $h_{O.4} = 23.0 \text{ mm}$   
 (b)  $h_O = 54.7 \text{ mm}$ ,  $h_{O.2} = 48.9 \text{ mm}$ ,  $h_{O.4} = 35.0 \text{ mm}$   
 (c)  $h_O = 84.1 \text{ mm}$ ,  $h_{O.2} = 71.7 \text{ mm}$ ,  $h_{O.4} = 44.4 \text{ mm}$   
 (d)  $h_O = 141.3 \text{ mm}$ ,  $h_{O.2} = 113.7 \text{ mm}$ ,  $h_{O.4} = 59.3 \text{ mm}$
- 8.5-3(a)  $k = \rho\omega^2 \left[ \int_b^a hr^2 dr / \int_b^a \frac{h}{r} dr \right]$  where  $h = h(r)$   
 (b) Error = 14.2%
- 8.6-1(a)  $\sigma_r = \sigma_Y \ln(r/a)$ ,  $\sigma_\theta = \sigma_Y + \sigma_r$   
 (b)  $p_{fp} = \sigma_Y \ln(a/b)$
- 8.6-2(a)  $a = 317.5 \text{ mm}$   
 (b)  $a = 210 \text{ mm}$ ,  $W_b/W_a = 0.344$   
 (c)  $a = 184 \text{ mm}$ ,  $W_c/W_a = 0.226$



- 8.6-3  $p_{fp} = 352 \text{ MPa}$
- 8.6-4 Single: impossible. Compound:  $a/b = 4.93$ , wt. ratio = 5.92
- 8.6-5  $p_{fp} = 2\sigma_Y \ln(a/b)$
- 8.6-6  $p_{fp} = 605 \text{ MPa}$ . Yielding before new  $p_i$  reaches  $p_{fp}$
- 8.6-7  $p_{fp} = 316 \text{ MPa}$ . Yielding when new  $p_i$  reaches  $p_{fp}$
- 8.6-8 [Proof required]
- 8.6-9  $p_i = 0.9375\sigma_Y$ ,  $c = 16.94 \text{ mm}$
- 8.6-10(a)  $2(a/b)^2 \ln(a/b) / [(a/b)^2 - 1] = 1 + \beta$   
 (b)  $a/b = 1.548$  (c)  $a/b = 2.22$
- 8.7-1 [Derivation required]
- 8.7-2(a)  $\omega_{fp}^2 = 2\sigma_Y \ln(a/b) / [\rho(a^2 - b^2)]$  (b) Factor = 1.267
- 8.7-3(a)  $\sigma_r = \sigma_Y(1 - r^2/a^2)$ ,  $\sigma_\theta = \sigma_Y$  for all  $r$   
 (b)  $\sigma_r = \sigma_Y(1 - 0.9524b/r - 0.0476r^2/b^2)$ ,  $\sigma_\theta = \sigma_Y$  for all  $r$
- 8.7-4(a)  $\omega_{fp}^2 = 5.25\sigma_Y/\rho$  (b) Factor = 0.619 (c) No (SCF neglected)
- 8.7-5 [Proof required]
- 8.7-6  $a/b = 4.85$
- 9.2-1  $\beta = T/GJ$ ,  $\tau_{max} = TR/J$ , where  $J = \pi(R^4 - b^4)/2$
- 9.3-1 Error = 303% (high)
- 9.3-2(a)  $\tau = 3T/[2(1 + \pi)Rt^2]$ ,  $\beta = \tau/Gt$   
 (b)  $\tau$  ratio = 25.2,  $\beta$  ratio = 252
- 9.3-3  $c/h = 3/7$ ,  $\beta$  ratio = 4,  $T_{thicker} = 0.857T_{total}$
- 9.3-4  $GK = 63,280G \text{ N}\cdot\text{mm}^2$ ,  $\tau_{max} = 237(10^{-6})T \text{ MPa}$
- 9.3-5(a)  $\tau_{max} = 12T/a^2b$ ,  $\beta = 12T/Ga^3b$   
 (b) 100% error (high) for both
- 9.3-6  $\sigma = 3PL/2a^2t$ ,  $\tau = (3P/4t)(1/a + 1/t)$
- 9.4-1(a)  $\tau_{max} = 2T/\pi ab^2$  (b)  $T/\beta = 3.101Gab^3$
- 9.4-2(a) Ratio = 1.354 (b) Ratio = 0.678  
 (c) Square:  $T/\beta = 2.26Ga^4$  (table),  $T/\beta = 2.40Ga^4$  (equation)  
 Rectang.:  $T/\beta = 1.12Ga^4$  (table),  $T/\beta = 1.13Ga^4$  (equation)
- 9.4-3 Square:  $\tau = 4.81T/A^{1.5}$ ,  $\beta = 7.09T/GA^2$   
 Circle:  $\tau = 3.545T/A^{1.5}$ ,  $\beta = 6.28T/GA^2$
- 9.4-4 Allowable  $T = 144 \text{ kN}\cdot\text{mm}$ ,  $\theta = 1.85^\circ$
- 9.5-1 [Derivation required]
- 9.5-2(a)  $\tau$  ratio =  $(1 + \eta^2)/(1 + \eta)$ ,  $\beta$  ratio =  $2(1 + \eta^2)/(1 + \eta)^2$ ,  
 where  $\eta = b/a$   
 (b) [Plot required] (c) [Proof required]
- 9.5-3  $R = 3000 \text{ mm}$  for open tube. May buckle
- 9.5-4 [Derivation required]
- 9.5-5(a) [Proof required] (b)  $\tau$  ratio = 1.27,  $\beta$  ratio = 1.62
- 9.5-6(a)  $T/\beta = 9.07GR^3t_0$ ;  $\tau_{max} = 0.159T/R^2t_0$ , outside at  $\alpha = 0$   
 (b)  $T/\beta = 9.425GR^3t_0$ ;  $\tau_{max} = 0.106T/R^2t_0$ , outside at  $\alpha = 0$   
 (c)  $\tau_{max} = 0.255T/Rt_0^2$ , inside and very near  $\alpha = \pm \pi$
- 9.5-7  $F = Ts/2\pi R^2$
- 9.5-8  $\theta = \frac{T}{4\pi Gt} \left( \frac{L}{r_i - r_o} \right)^3 \frac{L(2H+L)}{H^2(H+L)^2}$

- 9.6-1 [Derivation required]
- 9.6-2  $l_i/t_i\Gamma_i$  same in all cells  $i$ ;  $l_i$  = length of outer cell wall
- 9.6-3 Factor = 200
- 9.6-4  $q$  decreases 4%,  $\beta$  increases less than 1%
- 9.6-5(a)  $T/\beta = 10.83Ga^3t$ ,  $q_{outer} = 0.0924T/a^2$ ,  $q_{inner} = 0.0653T/a^2$   
 (b)  $T/\beta = 2\pi Gt(a^3 + b^3)$ ,  $q_{outer} = Ta/[2\pi(a^3 + b^3)]$ ,  
 $q_{inner} = Tb/[2\pi(a^3 + b^3)]$
- 9.6-6  $T = 48,700 \text{ N}\cdot\text{mm}$ ,  $\beta = 3.53/G$  per mm
- 9.6-7  $\tau$  factor =  $\beta$  factor  $\approx 1.78$
- 9.7-1 Factor = 0.5;  $> 0.5$  if noncircular (restraint of warping)
- 9.7-2(a)  $\theta'''' - k^2\theta'' = -k^2Tq/GK$   
 (b) Free:  $\theta'' = 0$ ,  $\theta'''' - k^2\theta'' = 0$   
 Fixed:  $\theta = 0$ ,  $\theta' = 0$   
 Simply supported:  $\theta = 0$ ,  $\theta'' = 0$  }  $\theta' = \frac{d\theta}{dx}$ ,  $\theta'' = \frac{d^2\theta}{dx^2}$ , etc.
- 9.7-3(a,b)  $\sigma_x = 16.1 \text{ MPa}$ ,  $\theta = 9.02(10^{-3}) \text{ rad}$
- 9.7-4(a)  $\sigma = \pm 91.6 \text{ MPa}$  (b) 2.88 mm left, 0.45 mm up
- 9.7-5 Midspan:  $\sigma_x = 2130(10^{-6})P$   
 Ends:  $\tau_{zx} = 302(10^{-6})P$  in web,  $\tau_{xy} = 261(10^{-6})P$  in flanges
- 9.8-1 [Plots required]
- 9.8-2 [Plots required]
- 9.9-1(a)  $\omega = -1.261a^2$  at flange tips (b)  $J_\omega = 3.363a^5t$
- 9.9-2(a)  $\omega = \pm 8a^2/7$  at flange tips (b)  $J_\omega = 1.905a^5t$
- 9.9-3(a)  $\omega = \pm 2a^2$  at cut (b)  $J_\omega = 3.70a^5t$
- 9.9-4(a)  $\omega = (4R^2/\pi)\cos\alpha + R^2[\alpha - (\pi/2)]$  (b)  $J_\omega = 0.0374R^5t$
- 9.9-5  $J_\omega = 7b^5t/24 + b^4ht/16$
- 9.10-1  $u_A = u_C = 0$ ,  $u_B = u_D = (T/4Gb)(b/t_b - h/t_h)$
- 9.10-2 [Proof required]
- 9.10-3  $u = \pm 0.213 \text{ mm}$  on top,  $u = \pm 0.0838 \text{ mm}$  on bottom
- 9.10-4 [Proof required]
- 9.11-1  $f = (\alpha^2/2) + 2(1 - \cos\alpha) - \pi\alpha$
- 9.11-2  $q_{max}$  in flange =  $E(d^2\beta/dx^2)(0.653a^3t)$
- 9.12-1 At support:  $\sigma_x = 0.285P$  at slit,  $\sigma_x = -0.166P$  on top  
 At end:  $\tau = 0.0284P$ ,  $\theta_L = 0.000119P$
- 9.12-2  $T = 27,000 \text{ N}\cdot\text{mm}$   
 At ends:  $\sigma_x = 54.7 \text{ MPa}$  at flange tips,  $q_{max}/t = 2.82 \text{ MPa}$   
 At middle:  $\tau_{sv} = 7.67 \text{ MPa}$
- 9.12-3 At support:  $\sigma_x = 121 \text{ MPa}$ ,  $q_{max}/t = 4.11 \text{ MPa}$   
 At end:  $\tau_{sv} = 14.5 \text{ MPa}$ .  $\theta$  reduction factor = 0.0645
- 9.12-4  $\sigma_x = 0.286P$
- 9.12-5  $L/a = 8$
- 9.12-6 Four constants:  $\beta = 0$  at  $x = 0$ ,  $d\beta/dx = 0$  at  $x = a + b$ ,  
 $\beta$  and  $d\beta/dx$  must both match between parts at  $x = a$
- 9.13-1(a)  $\theta_L = -0.073B_L/Gt^4$ ,  $\sigma_x = \pm 82.0(10^{-6})B_L/t^4$

- (b)  $\theta_O = +0.075B_L/Gt^4$
- 9.13-2  $\tau/\sigma_x = 0.413$ ,  $\tau_q/\sigma_x = 0.0413$
- 9.13-3 [Explanations required]
- 9.13-4 [Proof required]
- 9.14-1  $\sigma_O = 102$  MPa,  $\sigma_x = 121$  MPa,  $\tau_{SV} = 32.7$  MPa
- 9.14-2  $T = 2470$  N·mm,  $\tau_{SV} = 154$  MPa
- 9.14-3(a) Factor = 3.60 (b)  $\tau_{SV} = 0.0379T$ ,  $\sigma_x = 0.127T$   
(c)  $\Delta = -0.0244TL/G$  (d)  $\Delta = 0.0332FL/G$
- 9.14-4(a) Factor = 3.11 (b)  $\sigma_O = -113$  MPa
- 9.15-1 [Proof required]
- 9.15-2 [Sketches required]
- 9.15-3(a,b)  $T_{fp} = (\tau_{yt}^2/2)[a + b - (4t/3)]$  (c)  $T_{fp} = 19.06\tau_y a^3$
- 9.15-4  $T = 31\pi\tau_y R^3/48$
- 9.15-5  $L/b = 8.3$
- 10.1-1(a) [Proof required] (b)  $h/b = 1$
- 10.1-2 [Proof required]
- 10.1-3  $\sigma_x = N/A + B\omega/J_\omega +$  (right hand side of Eq.10.1-5)
- 10.2-1(a) [Proof required]  
(b) Factor: 0.707 for  $h = b$ , 0.503 for  $h = 10b$
- 10.2-2 Diamond-shaped area with intercepts  $y = \pm b/6$ ,  $z = \pm h/6$
- 10.2-3  $\sigma_{xA} = 159$  MPa,  $\sigma_{xB} = -182$  MPa
- 10.2-4  $\beta = -22.4^\circ$ . Factor: 0.42 at A, 0.68 at B
- 10.2-5(a)  $\lambda = -7.04^\circ$ ;  $\sigma_{xA} = -105$ ,  $\sigma_{xB} = -42.7$ ,  $\sigma_{xC} = 148$  (all MPa)  
(b)  $\beta = 76.0^\circ$
- 10.2-6(a)  $\sigma_x = \pm 184$  MPa, at flange tips  
(b)  $\sigma_x = \pm 102$  MPa, at web-flange intersection  
(c)  $\sigma_x = 4.79$  MPa, at right web-flange intersection
- 10.2-7  $M = 2.06(10^6)$  N·mm at  $\beta = -60.9^\circ$
- 10.2-8  $R = 114$  mm
- 10.2-9  $\sigma_x = -127$  MPa at upper flange tip  
 $\sigma_x = 68.5$  MPa at lower corner
- 10.3-1(a)  $27.7PL/b^3 \leq (\sigma_x)_{tens} \leq 32.0PL/b^3$   
(b) Deflection of tip =  $18.48PL^3/Eb^4$  for all orientations
- 10.3-2  $9.48^\circ$  from horizontal
- 10.3-3  $P_y = -0.528P$ ,  $P_z = -0.849P$
- 10.3-4(a,b)  $\Delta = 0.340(10^6)q/E$ , at  $14.7^\circ$  to vertical
- 10.3-5(a)  $H = 244q$  (b)  $\Delta = 280,000q/E$  (parallel to z axis)
- 10.3-6  $\Delta = 7.66$  mm at  $31.4^\circ$  above negative y axis
- 10.3-7 [Arguments required]
- 10.3-8  $\Delta = 0.115PL^3/EI$  at  $34.6^\circ$  below positive y axis
- 10.4-1 [Proof required]
- 10.4-2(a,b) [Proof required]
- 10.4-3  $\tau_{ave}$  is  $P/th$  at  $x = 0$ ,  $0.444P/th$  at  $x = L/2$ ,  $P/4th$  at  $x = L$
- 10.4-4  $\alpha = 21.8^\circ$ ,  $\tau = 0.00332V$

- 10.4-5(a)  $q = V_z(1 - \cos \alpha)/\pi R$  (b)  $q_{\max} = 2V_z/\pi R$  at  $\alpha = \pi$
- 10.4-6(a)  $z = -h/12$  (b) [Proof required]  
(c)  $q_{\max} = 1.35V_y/h$  at  $y = 3h/20$  (d) [Proof required]
- 10.4-7  $q_{\max} = .00990V$  at the centroid
- 10.4-8(a)  $q = (3862 - 214.5z + 2.276z^2)10^{-6}V_y$   
(b)  $q = (10,300 - 1.788y^2)10^{-6}V_y$   
(c)  $q = 0$  at  $z = \pm 24.24$  mm on flanges  
(d) About 19% low
- 10.5-1 Respective  $e_y$ 's, relative to  $y = 0$ :  $-2R$ ,  $-b/\sqrt{3}$ ,  $-3\sqrt{2}b/4$
- 10.5-2  $e_y$  is  $2R[1 - (t/R)^2/3]$  left of origin
- 10.6-1 Rel. to vertical web (except as noted),  $|e_y|$  distances are:  
(a)  $3b^2(a^2 + c^2)/[2c^3 + 6b(a^2 + c^2)]$  (left)  
(b)  $3b^2(c^2 - a^2)/[2c^3 + 6b(a^2 + c^2)]$  (left)  
(c)  $3b^2/(6b + c)$  (right)  
(d)  $0.155c$  (left)  
(e)  $bc^3/(a^3 + c^3)$  (right of left flange)  
(f)  $(b/2)(3b + 4c)/(3b + 2c)$  (left)  
(g)  $(b/2)(3b + 4c)/(3b + 8c)$  (left)  
(h)  $\sqrt{3}c/2$  (right of left vertex)  
(i)  $\sqrt{3}h/4$  (left of left vertex)  
(j)  $2R$  (left of centroid)  
(k)  $2R(\sin \alpha - \alpha \cos \alpha)/(\alpha - \sin \alpha \cos \alpha)$  (left of cntr. of arc)  
(l)  $0.510R$  (left)
- 10.6-2  $e_y$  is  $\pi R/2$  right of center of arc
- 10.6-3 Force =  $3P/16$  on each weld, very localized near tip of beam
- 10.6-4(a) [Proof required]  
(b,c) [See answers for Problem 10.6-1, parts (e) and (h)]
- 10.6-5 Factor = 1.31
- 10.7-1 Relative to pole:  $e_y = 44.7$  mm,  $e_z = 164.9$  mm
- 10.7-2 [See answers already provided]
- 10.7-3 Relative to  $x = y = 0$ :  $0.026a$  left,  $1.021a$  below
- 10.8-1(a)  $0.611R$  right of vertical web (b)  $\beta = 2P/\pi^2 R^2 Gt$
- 11.2-1(a)  $P_c = 56.8$  kN (b)  $P_c = 24.0$  kN
- 11.2-2 Changes of slope at 0.7, 1.3, and 2.0 times  $P/\sigma_y A$
- 11.2-3  $P_c = 1.25A\sigma_y$
- 11.2-4(a)  $P_y = n\sigma_y A$  (b)  $P_c = 4n\sigma_y A/\pi$
- 11.3-1(a)  $f = 1.70$  (b)  $f = 1.27$  (c)  $f = 2.00$  (d)  $f = 2.34$
- 11.3-2  $f = 1.137$
- 11.3-3  $M_{fp} = bh^2\sigma_y/12$
- 11.3-4 Linear for  $0 < M < 3.60$  and for  $4.52 < M < 5.11$  (kN·m)
- 11.3-5 [Proof required]
- 11.3-6(a) [Sketch required] (b) [Proof required]  
(c)  $M = \sigma_y bc^2/3$  to yield again,  $M_{fp} = \sigma_y bc^2$
- 11.3-7(a,b) [Sketch required]
- 11.3-8(a)  $\rho = 7.143$  m (b) Residual  $\rho = 13.8$  m
- 11.3-9(a,b) R of mandrel = 22.0 mm